

# Hyperspectral remote sensing

## Theory Applications and Methods

August 23, 2010

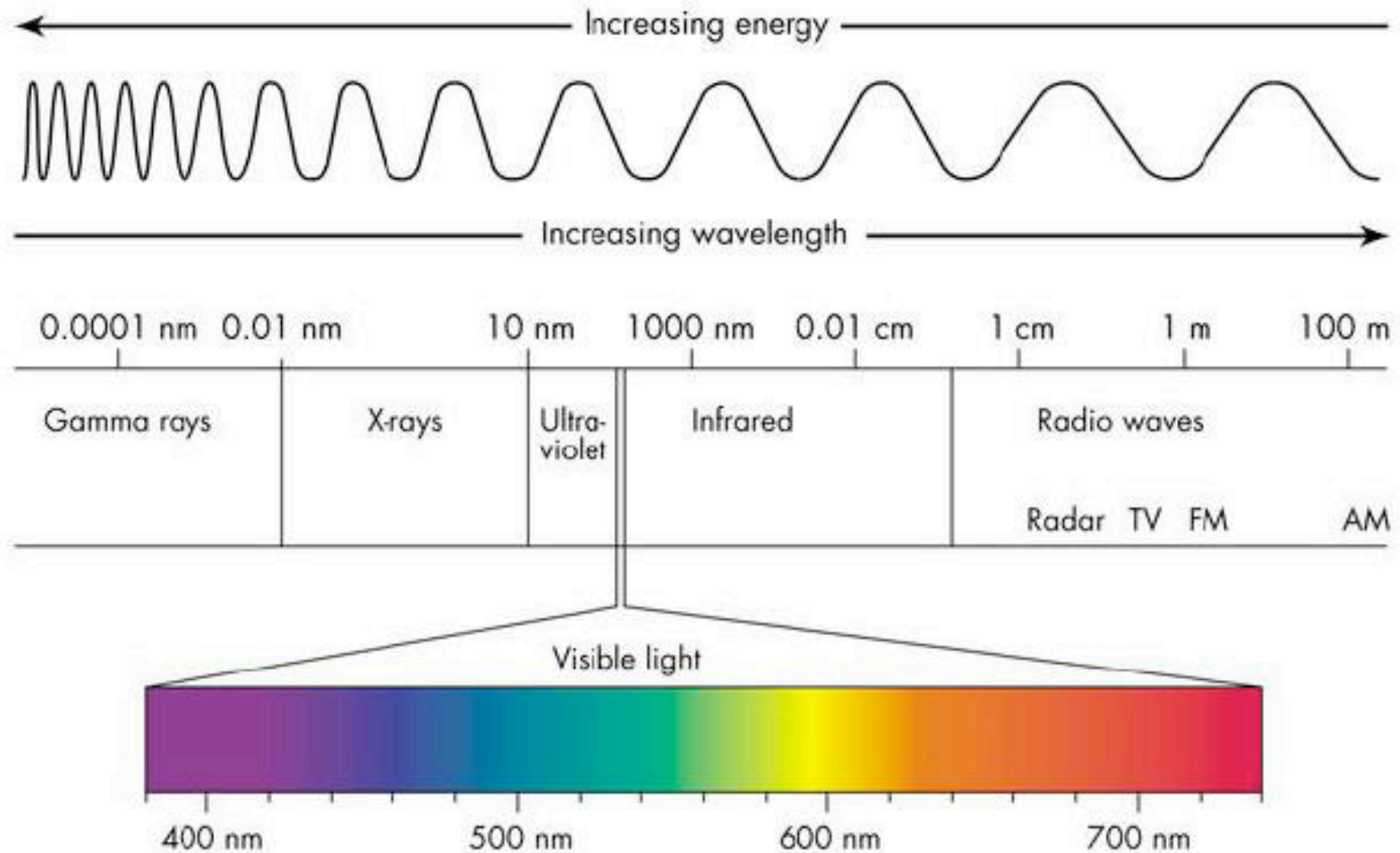
# Domains of remote sensing

- Spatial domain
- Spectral domain
- Temporal domain
- Angular domain
- Polarization domain

# Spectral domain

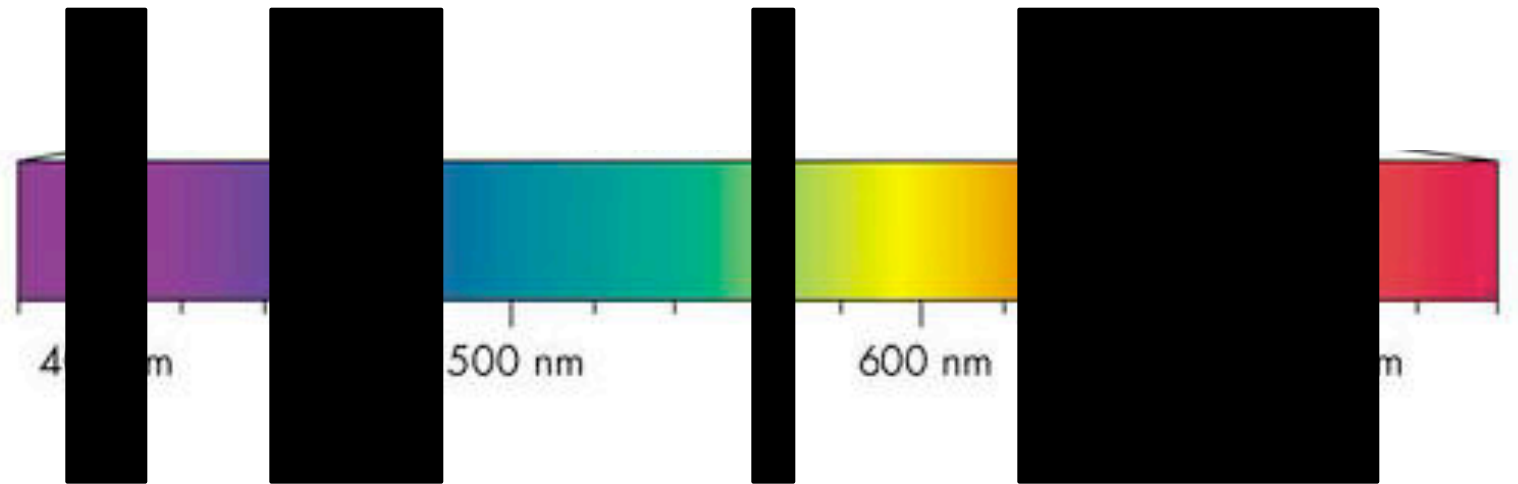
- Spectral location of “bands”
  - i.e. visible, IR, SWIR
- Band width
  - how wide are spectral positions?
- Number and frequency of bands
  - how many and at what frequency?

# Electromagnetic Spectrum



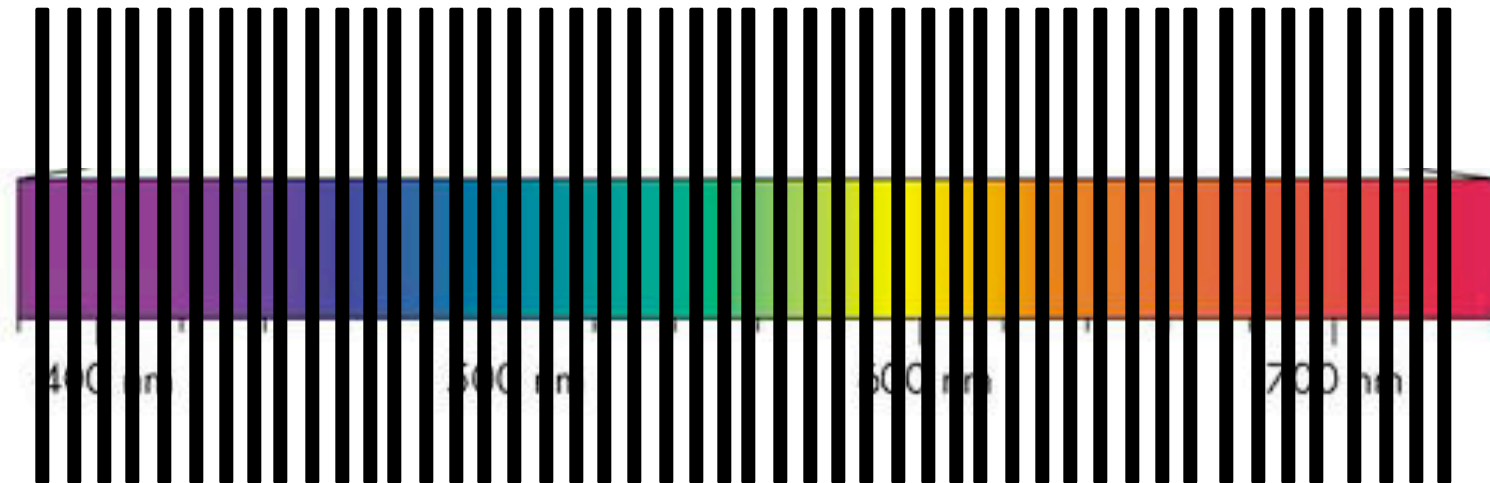
The Sun produces a *continuous spectrum* of electromagnetic radiation ranging from very short, extremely high frequency gamma and cosmic waves to long, very low frequency radio waves

# Spectral frequency (how often do you sample the spectrum)



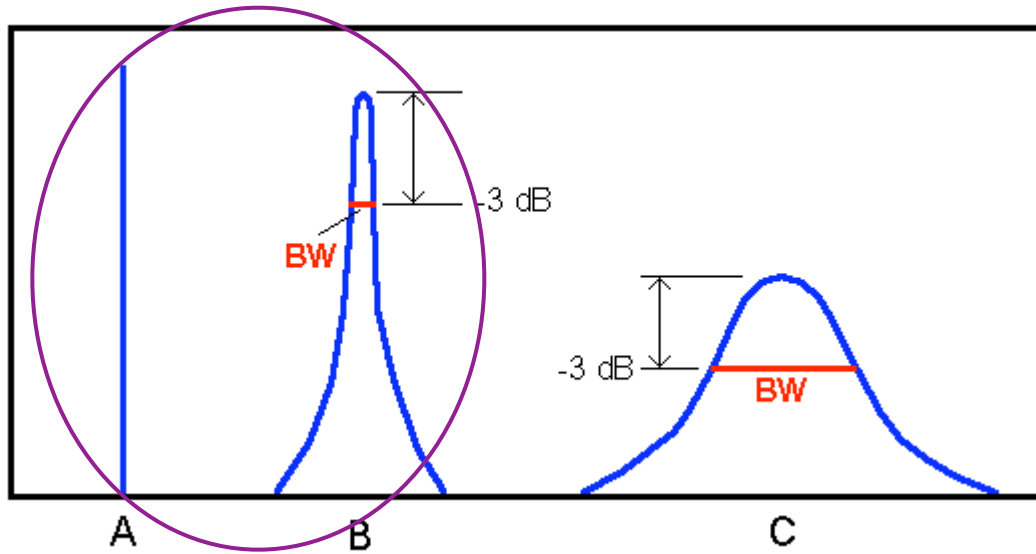
broadband example

# Spectral frequency (how often do you sample the spectrum)

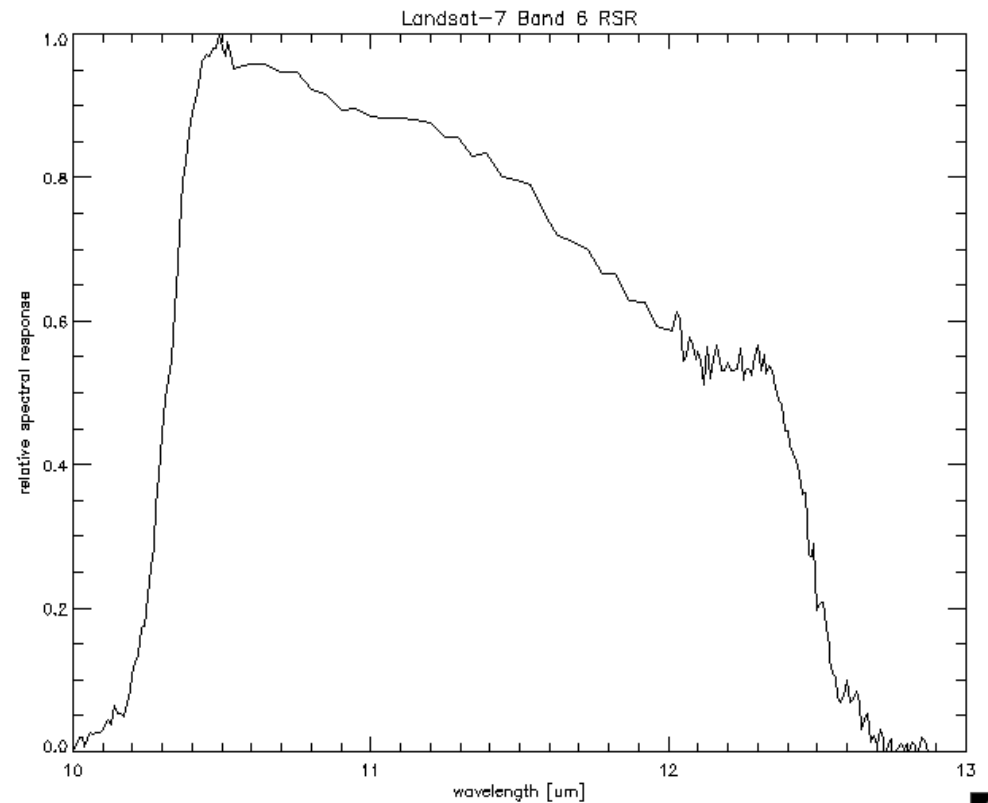


hyperspectral example  
(hyper [many] - spectral)

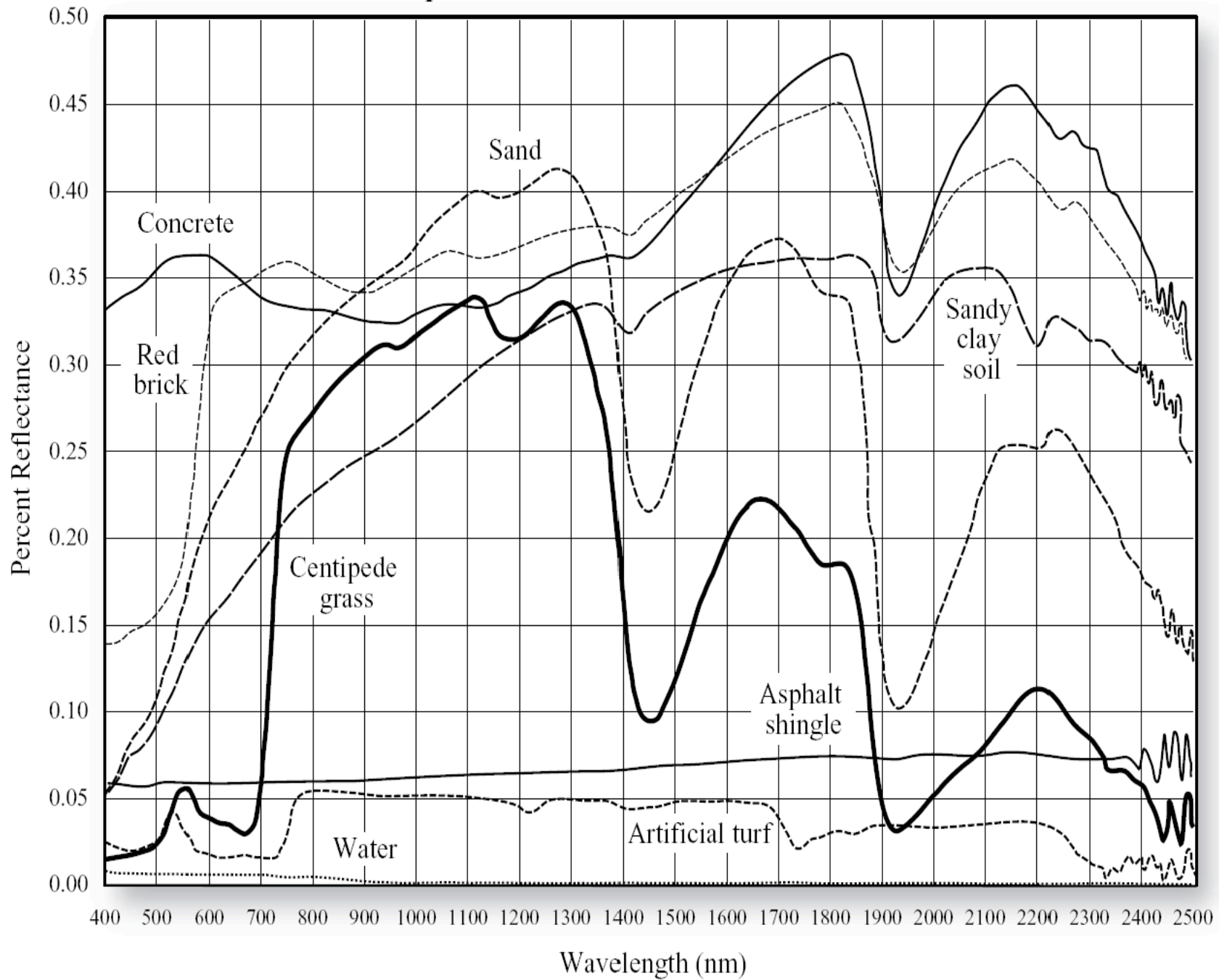
# Spectral bandwidth



Landsat Band 6  
spectral response

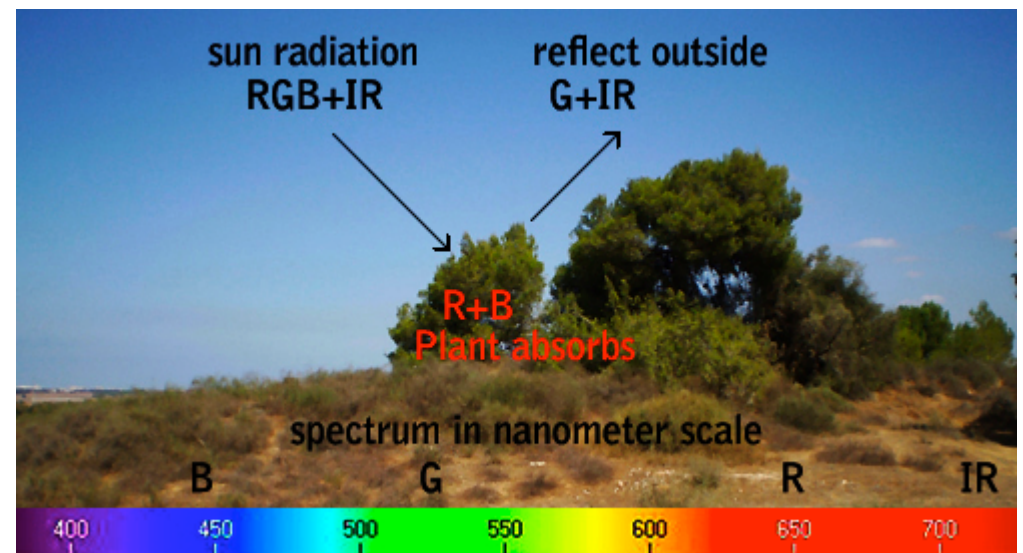
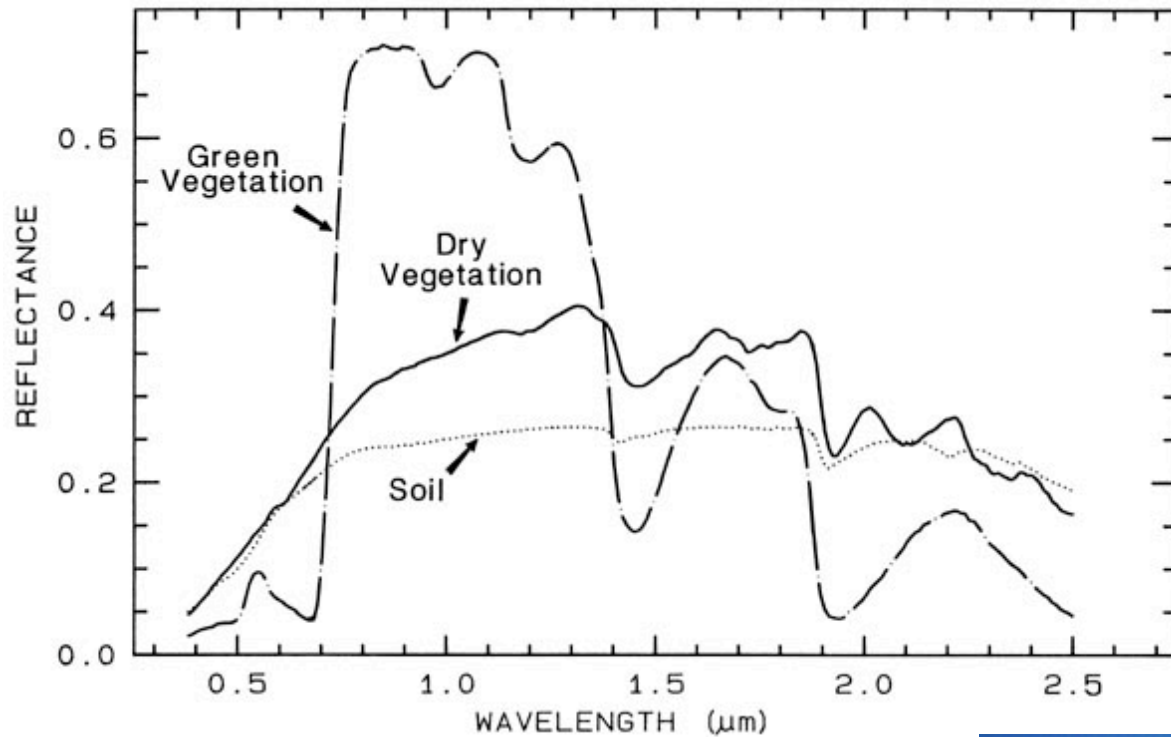


### Spectral Reflectance of Selected Materials

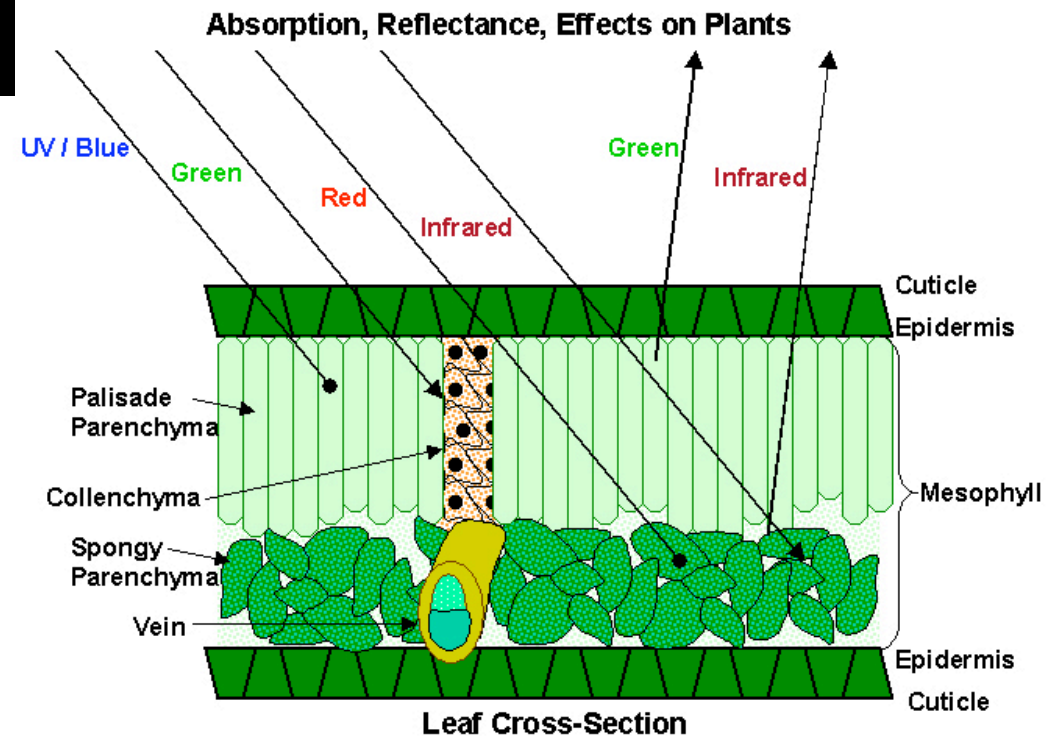
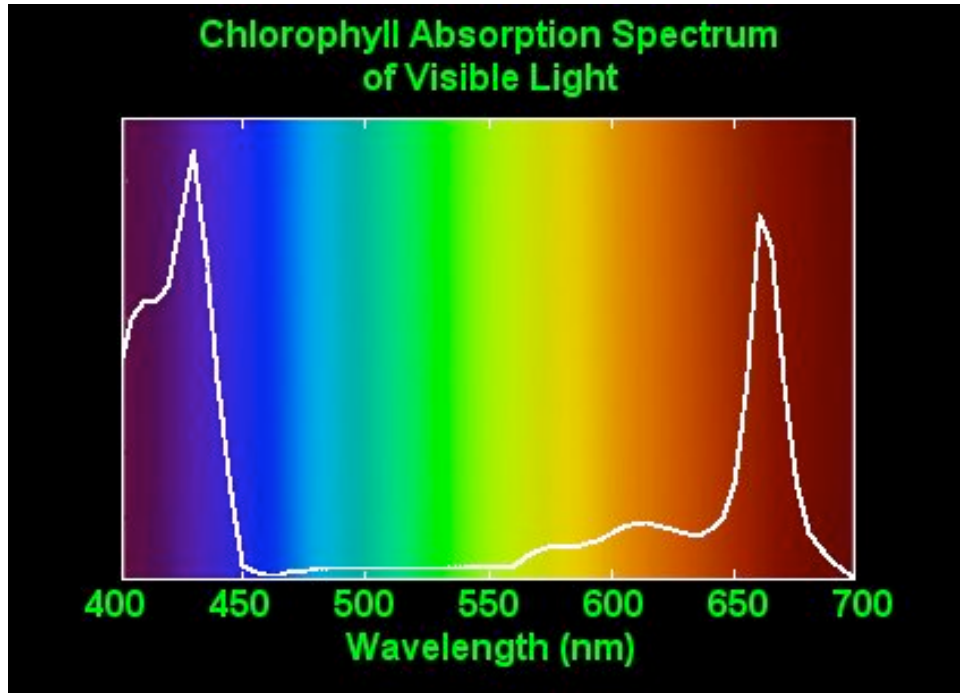




# Dry vs. Green vegetation



# Leaf reflectance and absorption

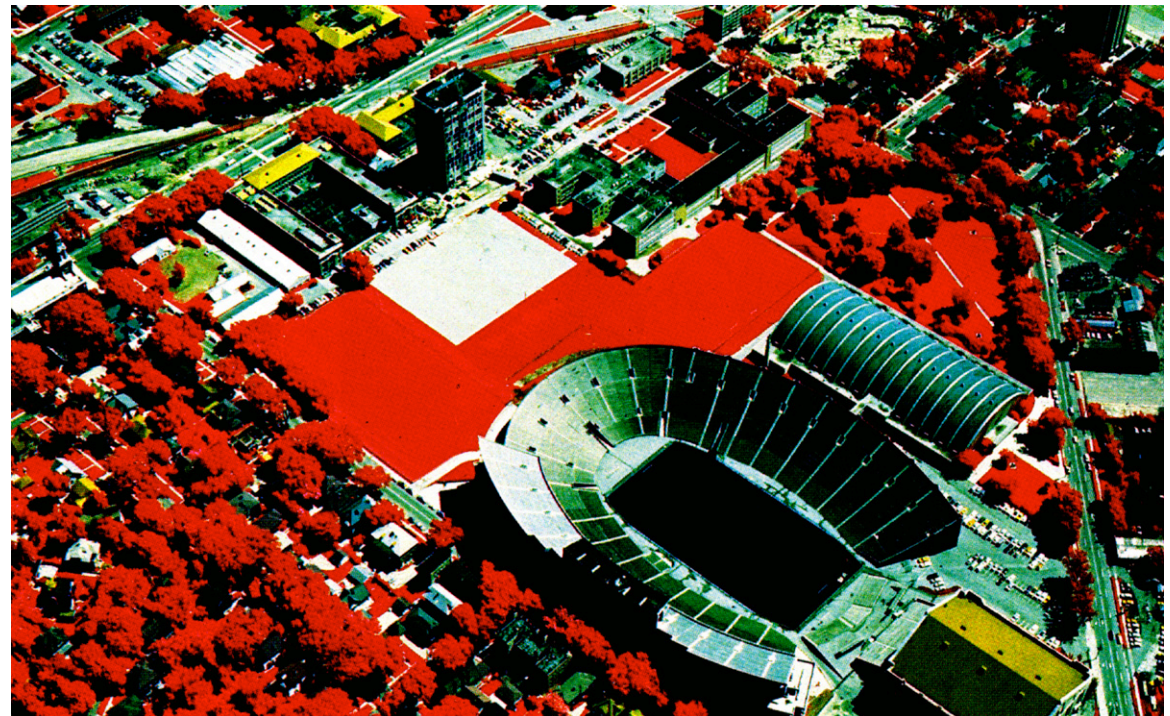




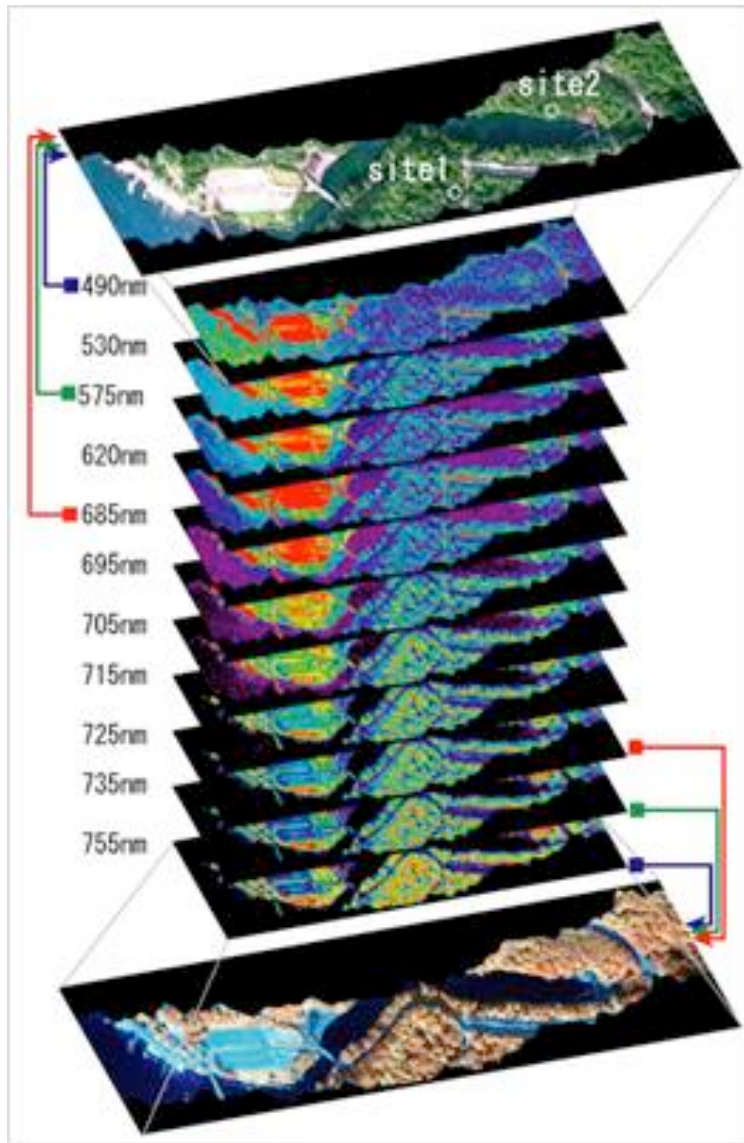


color aerial photo  
visible spectrum

color aerial photo  
NIR spectrum



# Spectral frequency

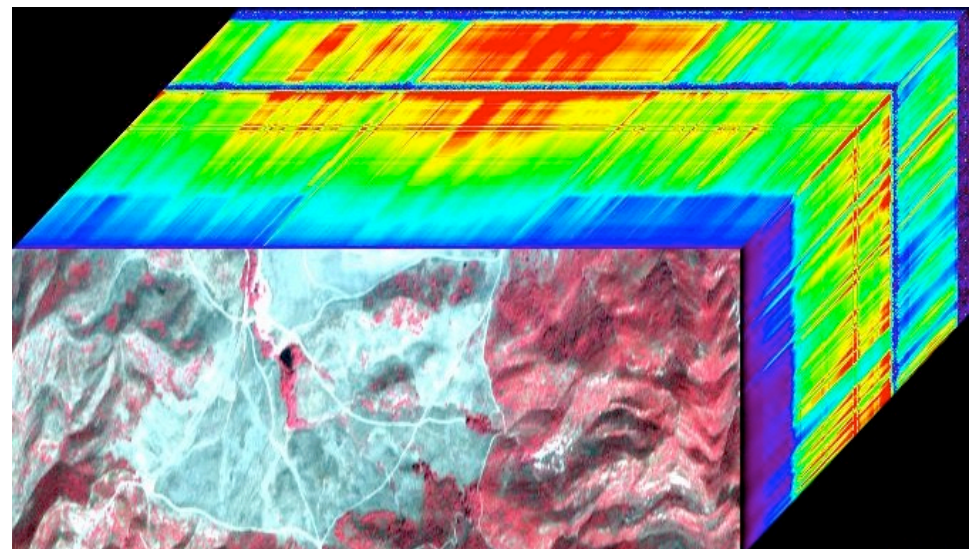


hyperspectral cube

# Imaging spectroscopy

what is imaging spectroscopy?

- systems with **narrow spectral bands** used to obtain a *continuous spectrum* of electromagnetic radiation
- complete characterization of spectral properties
- more detail – reveals surface chemistry, physical properties and geometry
- new capabilities for analysis
- spectral libraries



# Motivation

- Imaging spectrometry provides fundamental spectral information that is not accessible to broad band systems
- Imaging spectrometry provides fundamental measurements that add value to broad band systems
- Imaging spectrometry provides flexibility, enabling the simultaneous solution of numerous remote sensing problems

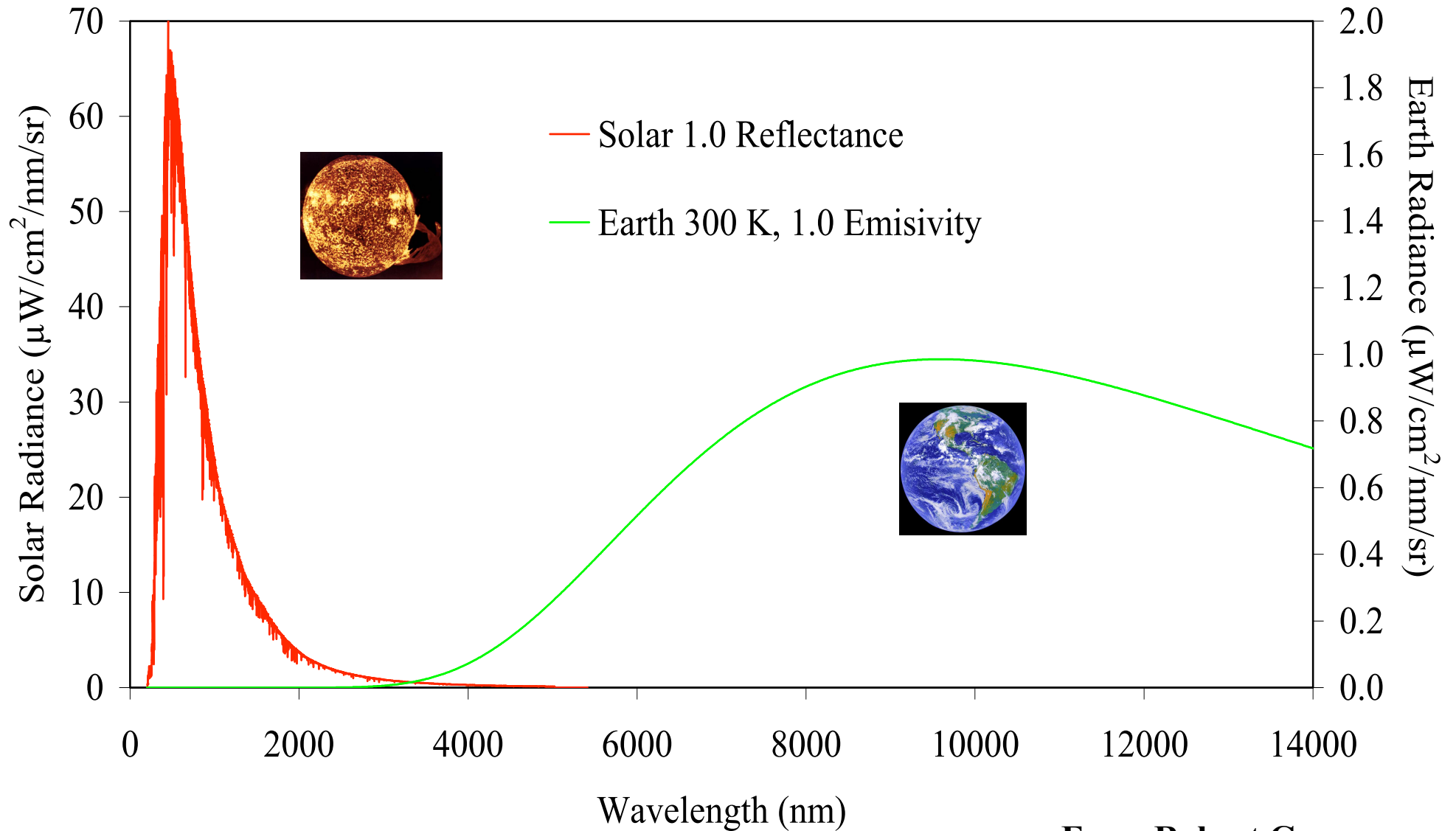
# Applications



# Atmospheres

- The atmosphere imposes its signature upon all remote sensing measurements
- The atmosphere must be characterized to solve for surface reflectance
- Various atmospheric constituents can be mapped using an imaging spectrometer

# Emission Spectra of the Sun and Earth with no Atmosphere



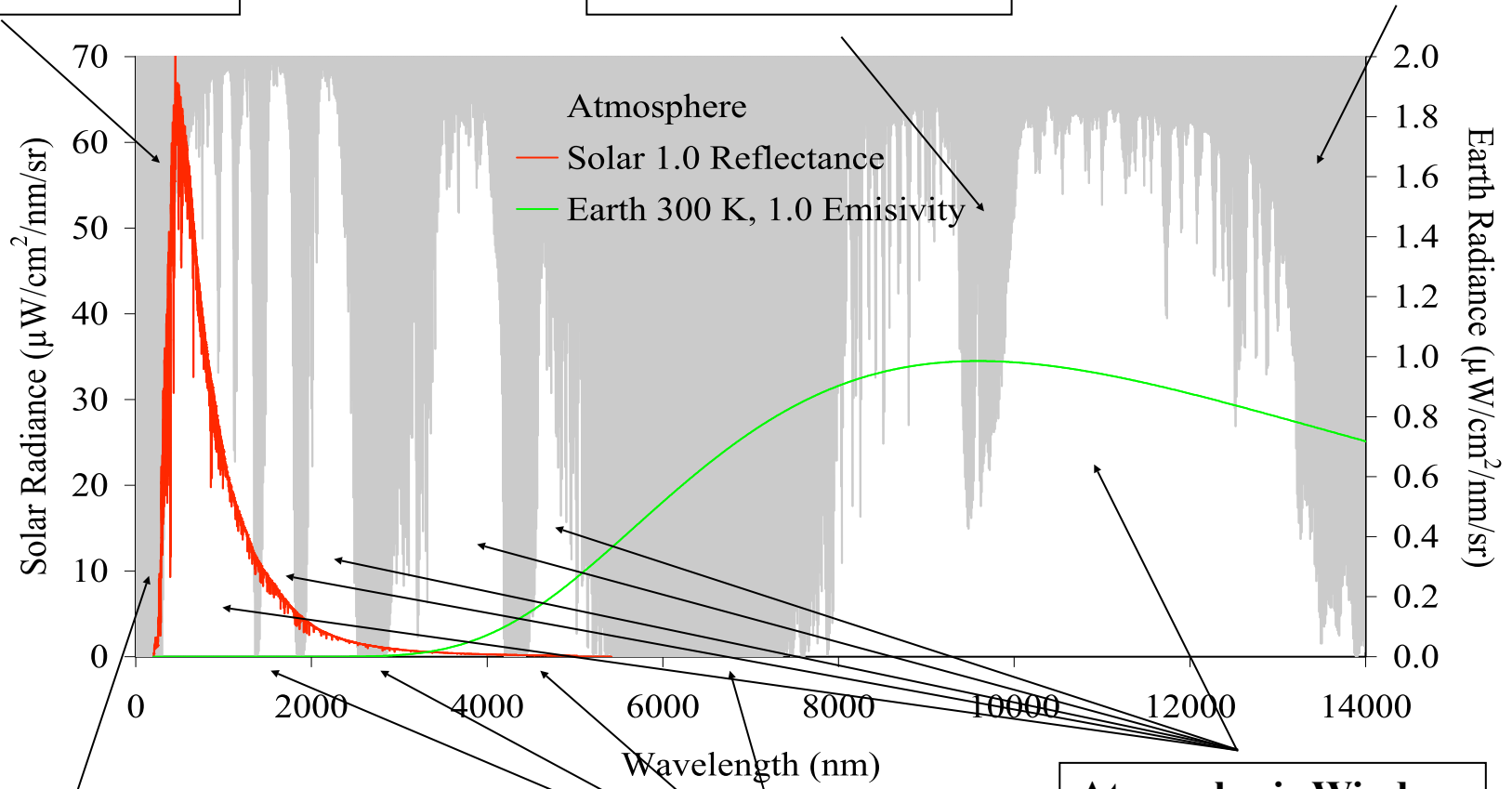
From Robert Green

# Fundamental Processes

**Electronic Absorption**  
**O<sub>3</sub> (UV), O<sub>2</sub> (762 nm)**

**Vibrational/Rotational**  
**O<sub>3</sub> (9.6 μm)**

**Rotational**  
**CO<sub>2</sub>, H<sub>2</sub>O**



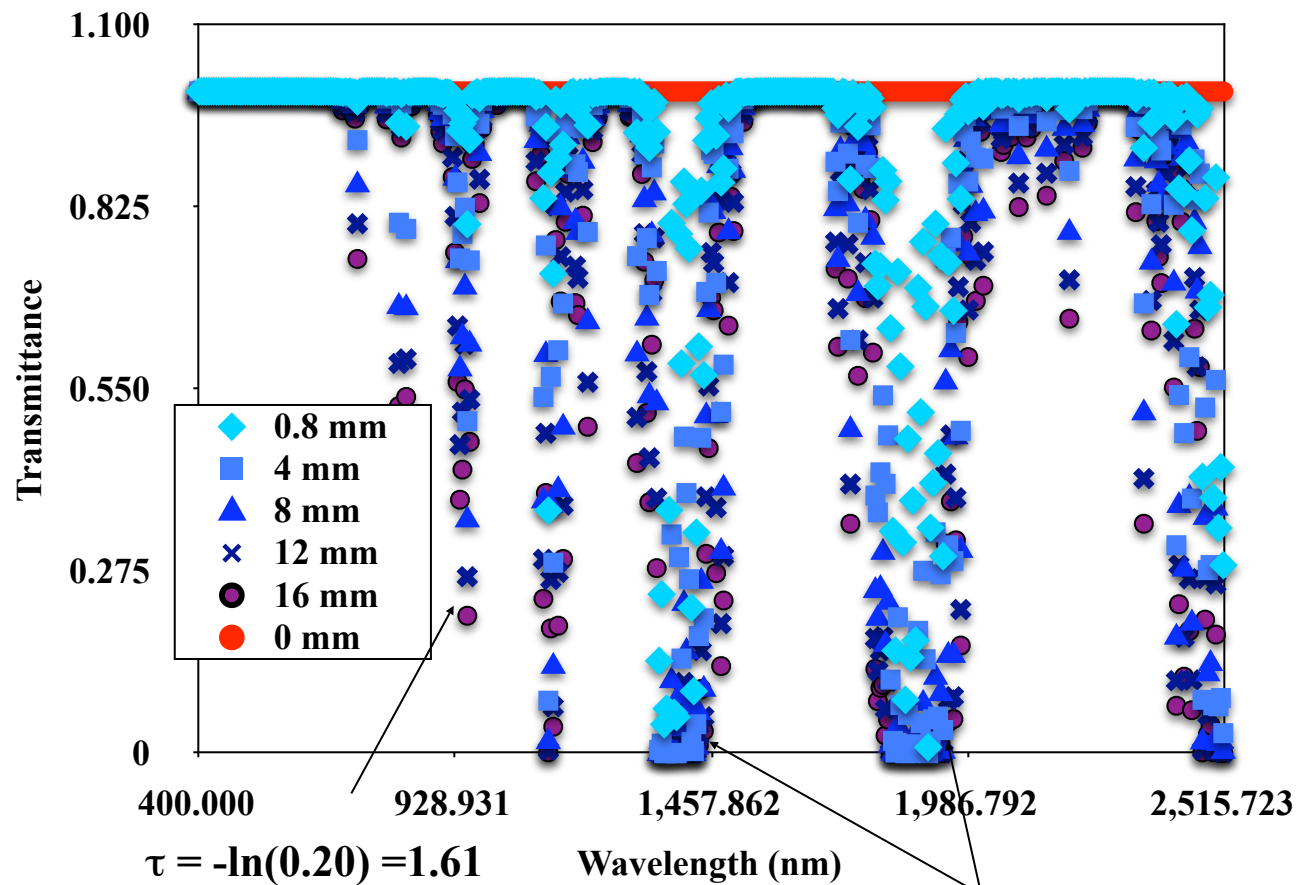
**Scattering: Dominates shortest wavelengths, interacts with atmospheric molecules. At longer wavelengths, cloud droplets or aerosols/smoke**

**Vibrational absorption**  
**H<sub>2</sub>O, CO<sub>2</sub>, CH<sub>4</sub>**

**Modified from Robert Green**

# Impact of Water Vapor

- Water vapor is unique in that it varies considerably over space and time

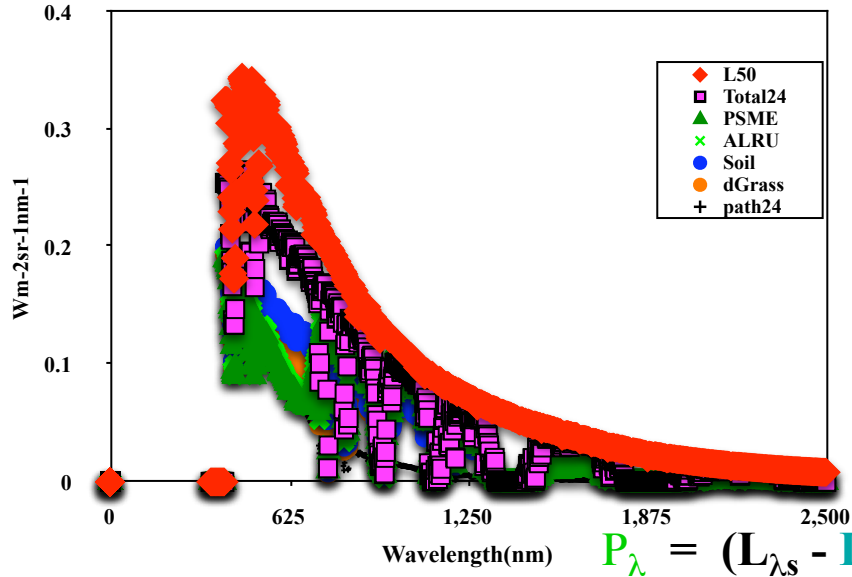


Modtran: March 21, 100 km elev, 1 atm

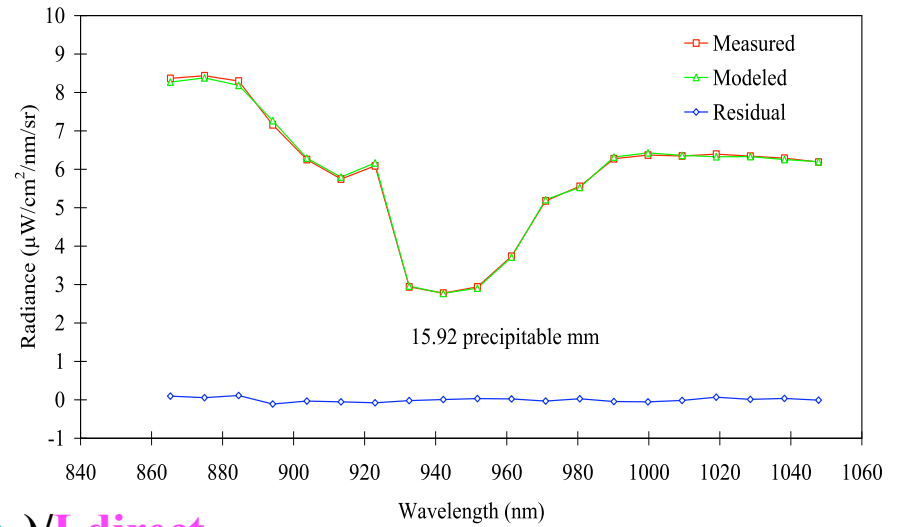
Courtesy of Dar Roberts  
UCSB

# Radiative Transfer Solution for Reflectance

## Models and Measurements

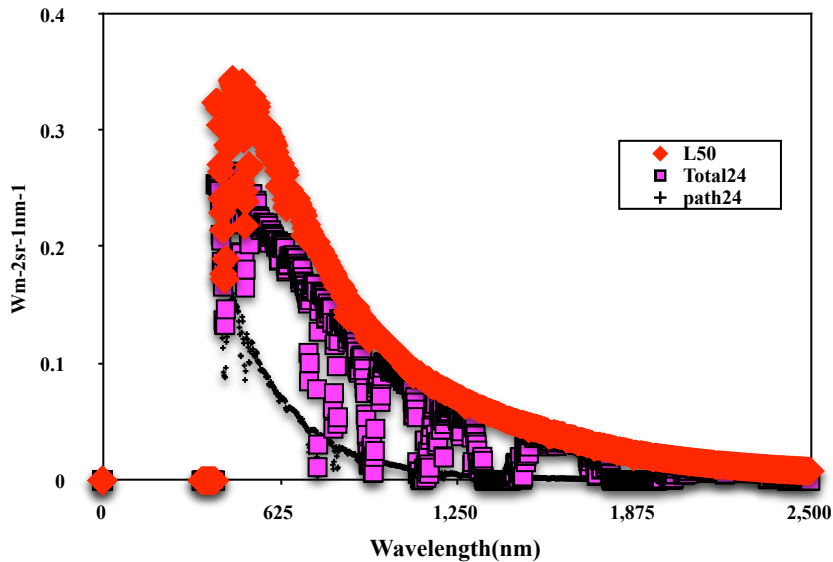


## Spectral Fit in Water Vapor Band

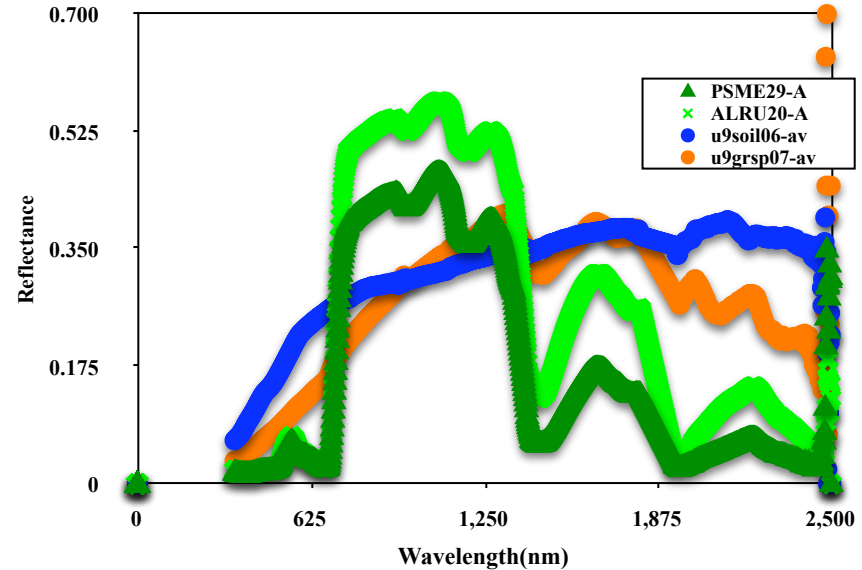


$$P_{\lambda} = (L_{\lambda S} - L_{\text{path}_{\lambda}}) / L_{\text{direct}_{\lambda}}$$

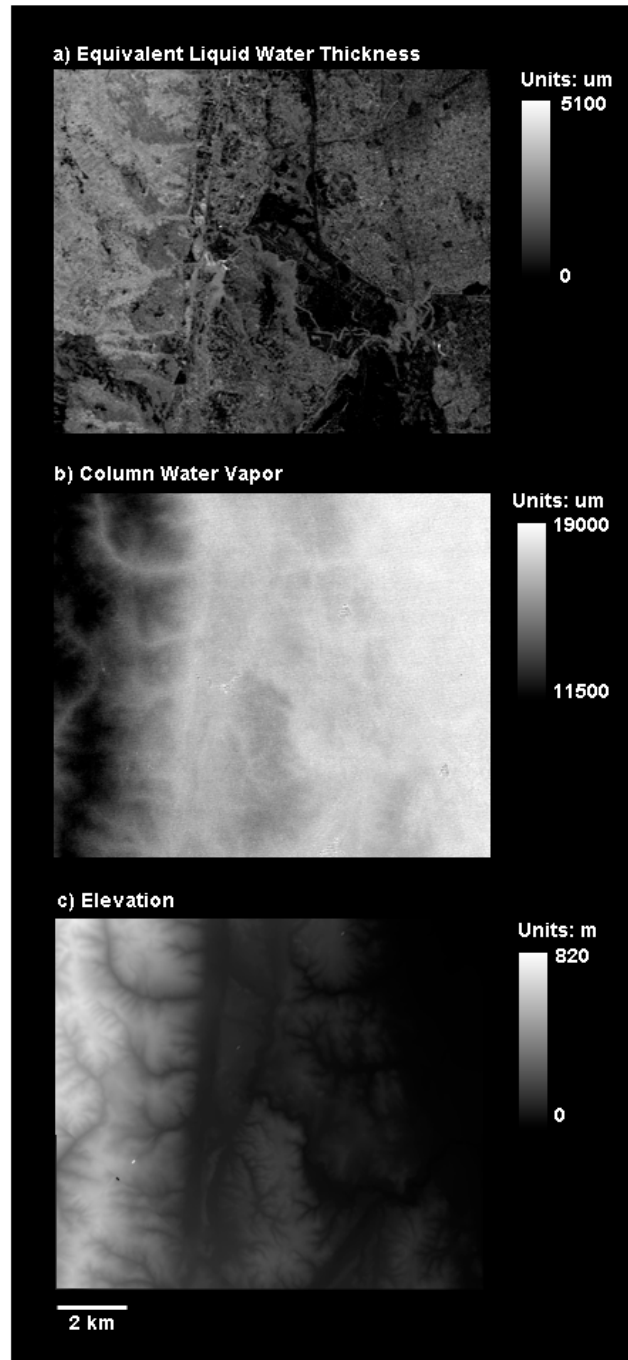
## Modeled Radiance



## Retrieved Reflectance



# Reflectance Product: Water vapor and Liquid water



- **Liquid water**
  - Measures water in leaves
  - Primarily structural
- **Water vapor**
  - Inversely related to topography
  - Varies temporally
  - Related to ET

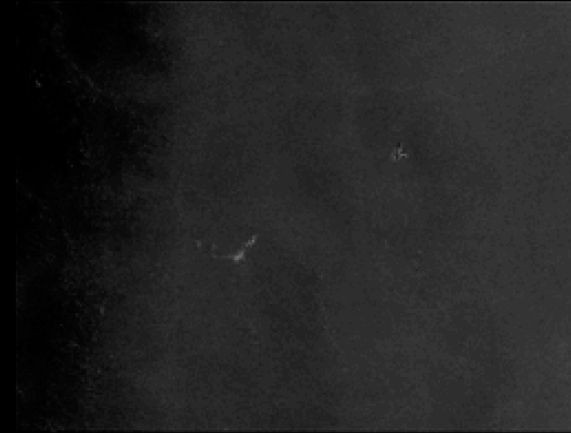
Roberts et al., 1997, RSE

# Temporal Changes in Water Vapor

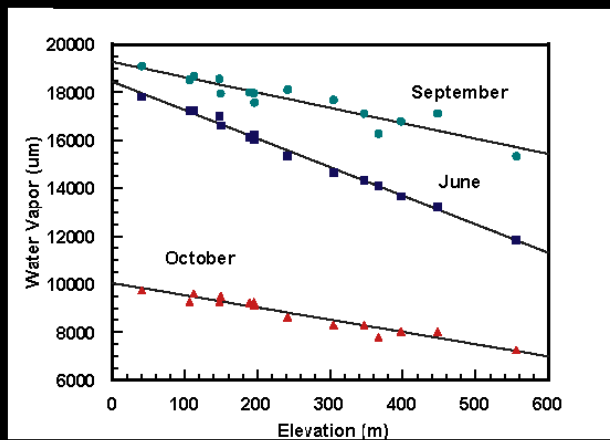
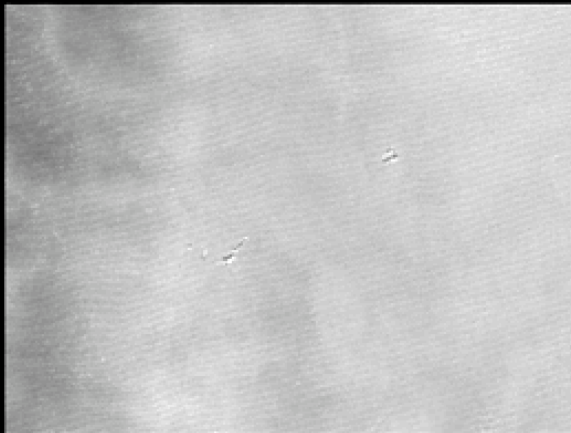
a) June 2, 1992



c) Oct 6, 1992



b) Sept 4, 1992



# Can Methane be Mapped With Hyper-Spectral Sensors?

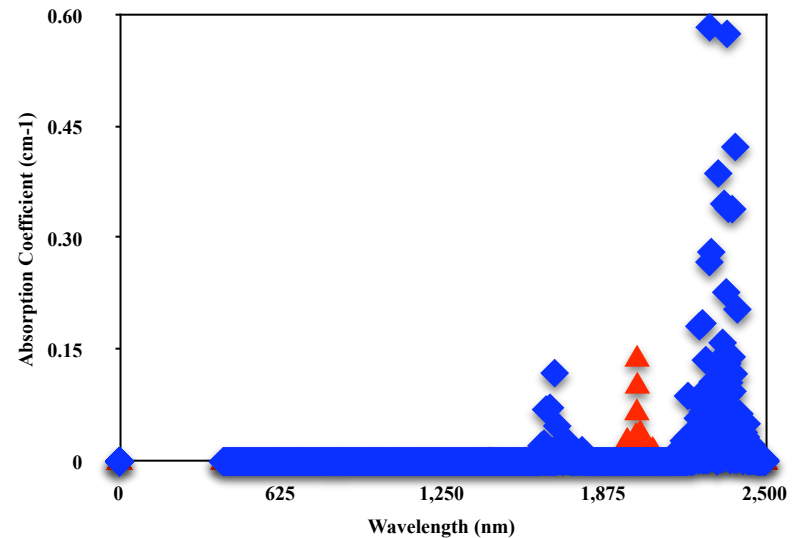
Courtesy of Dar Roberts  
UCSB



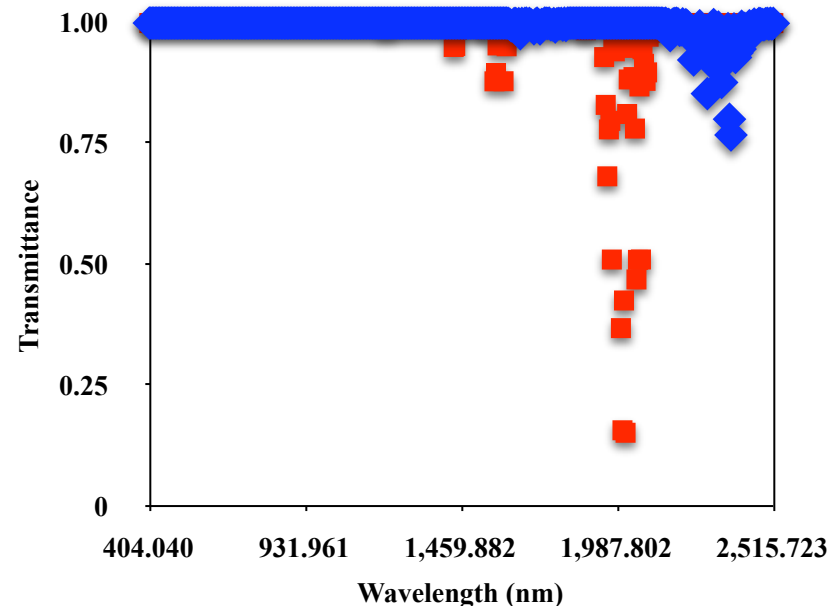
# Why Map Methane?

- Methane is a strong greenhouse gas with large absorption coefficients at ~2300 nm and 1700 nm
- Methane is a far stronger absorber than Carbon Dioxide but has a lower impact because of a much lower concentration in the atmosphere
  - CO<sub>2</sub>: ~ 370 ppm
  - CH<sub>4</sub>: ~ 1.9 ppm

Absorption Coefficients



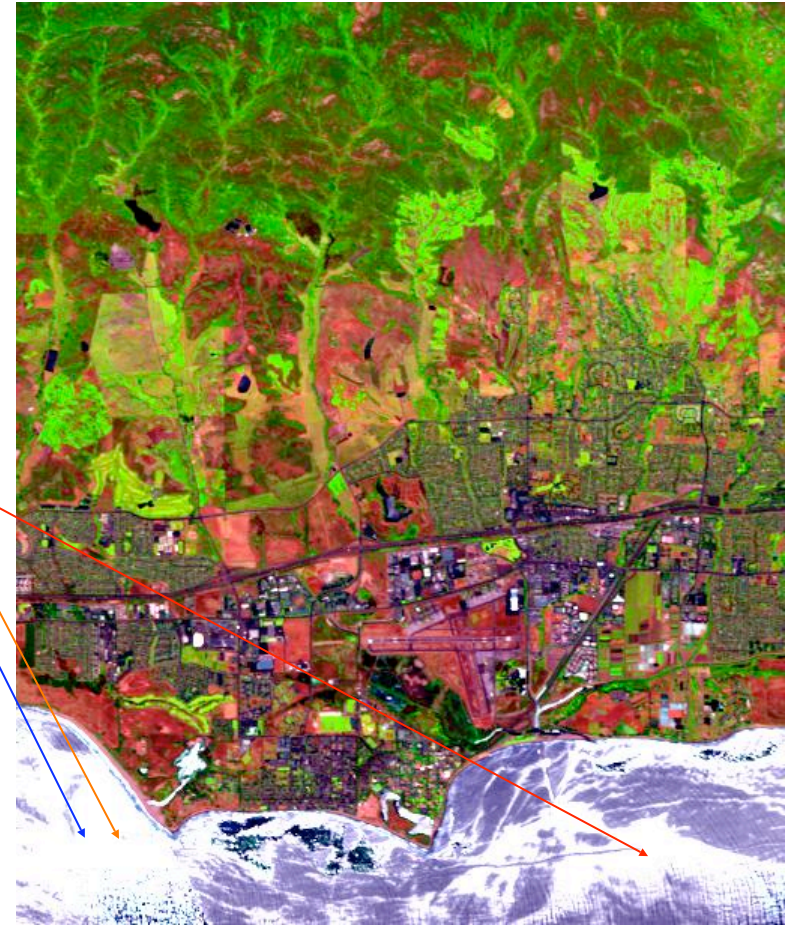
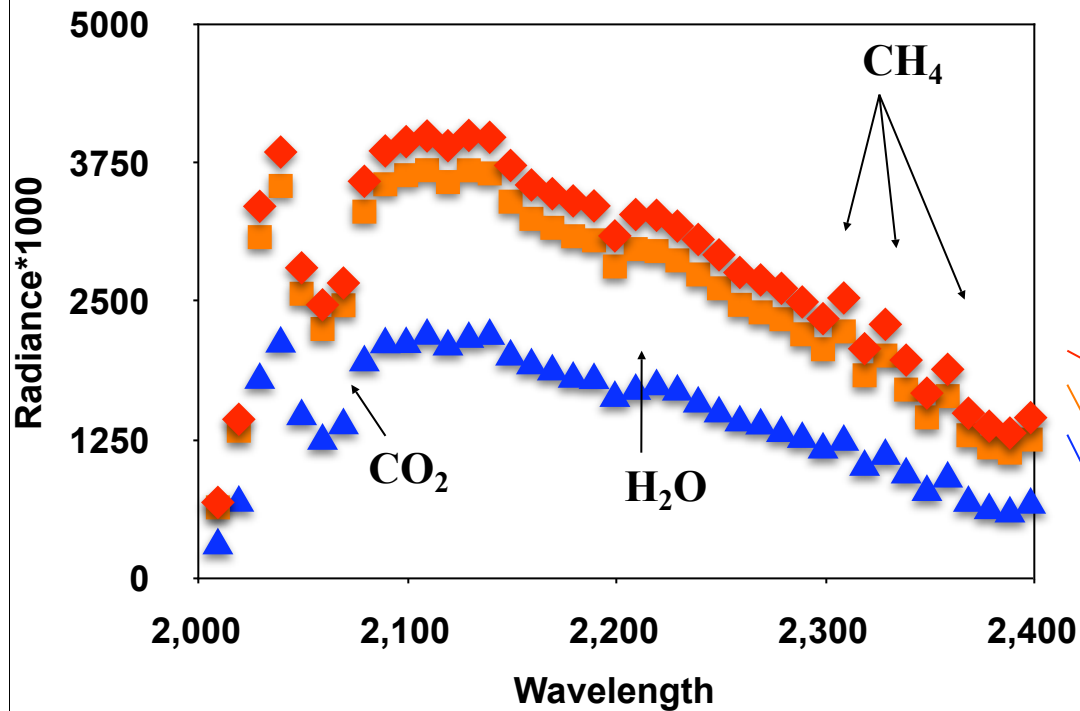
Transmittance, one air mass



Courtesy of Dar Roberts  
UCSB

# AVIRIS Measures of Methane

## 6-14-2001



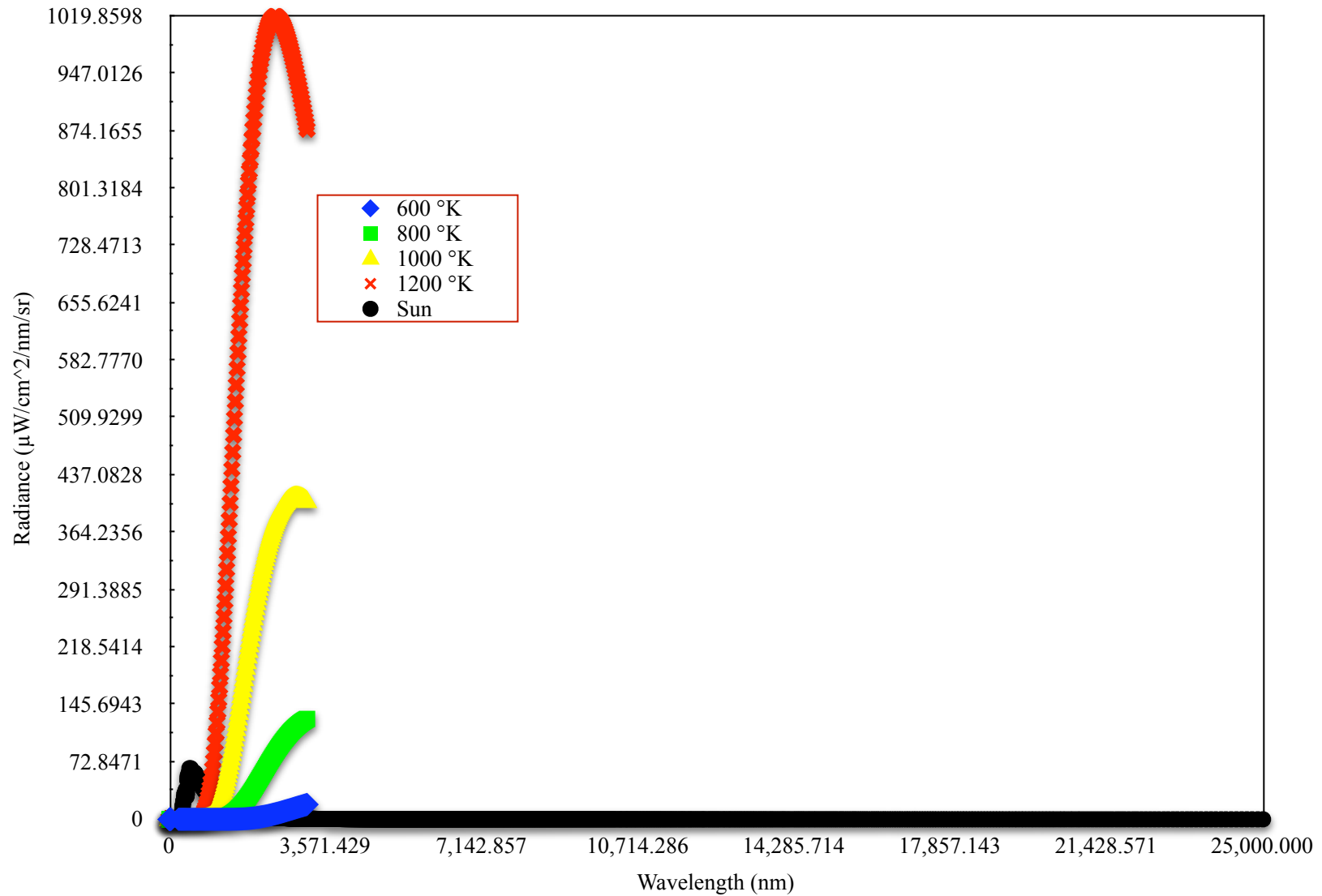
Note differences in surface reflectance  
Note atmospheric background methane is prominent

Courtesy of Dar Roberts  
UCSB

# Fire Temperature Retrievals

- The primary focus on fire temperature retrieval has been in the thermal
- Thermal systems tend to saturate at high fire temperatures
- In imaging spectrometer, similar to AVIRIS provides a wide range of temperature retrievals
  - 500K to over 1500K
  - The system cannot saturate because there is always a signal at shorter wavelengths

# Planck Functions and The Solar Irradiance Spectrum

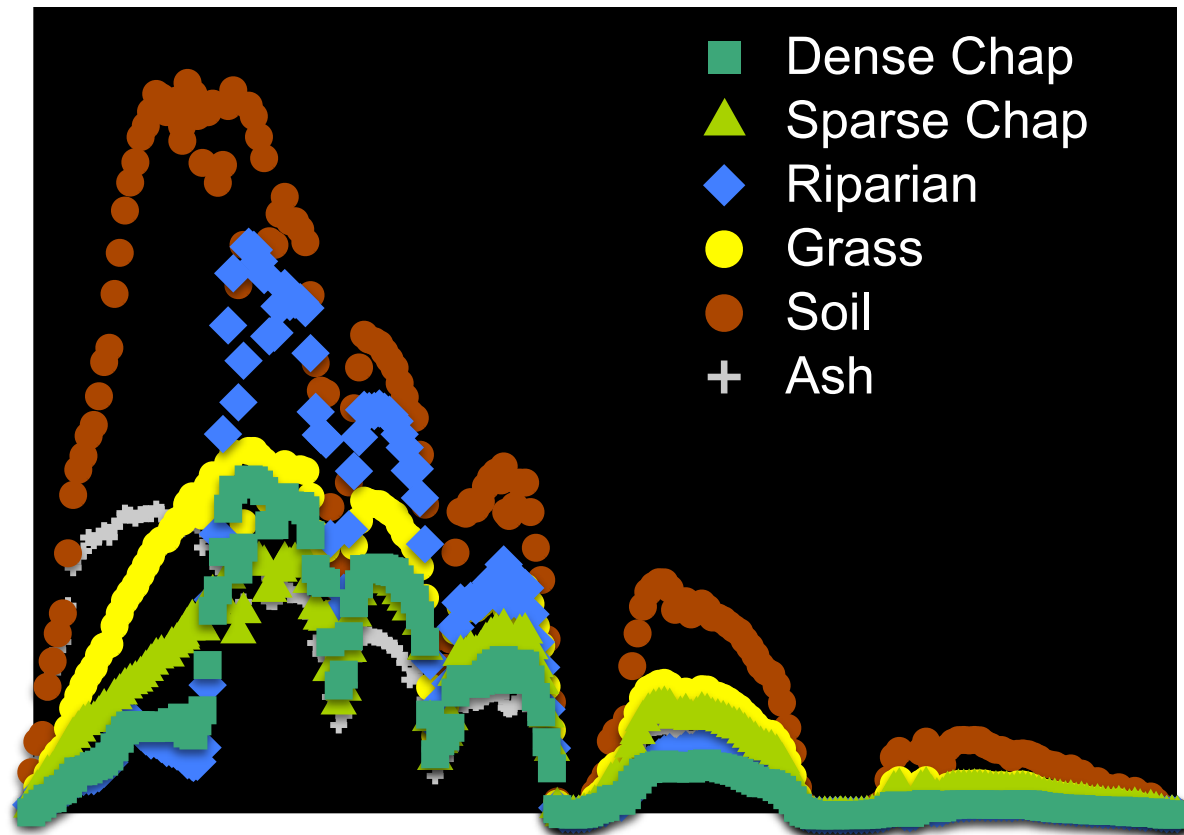


From Robert Green

# Methods

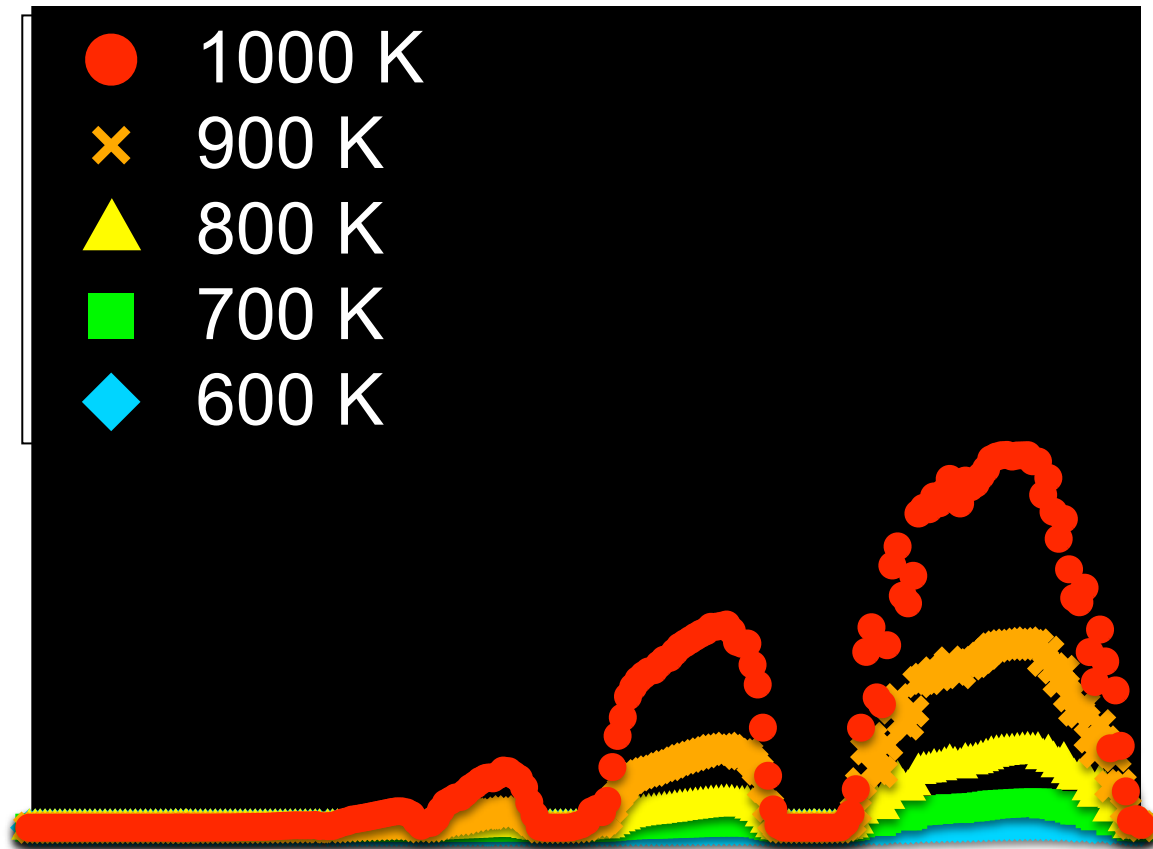
- **Multiple Endmember Spectral Mixture Analysis (MESMA) was used to model each pixel in the AVIRIS image**
- **Each pixel was modeled as a combination of:**
  - 1 emitted thermal radiance endmember
  - 1 reflected solar radiance endmember
  - Shade (zero radiance)
- **Emitted thermal radiance endmembers were modeled using MODTRAN**
  - Ranged from 400-1500 K (260°-2240°F) at increments of 10 K
- **Reflected solar radiance endmembers were selected from the image using Endmember Average RMSE (EAR)**
  - Six possible endmembers: riparian, dense chaparral, sparse chaparral/sagescrub, grass, soil and ash

# Reflected Solar Radiance Endmembers

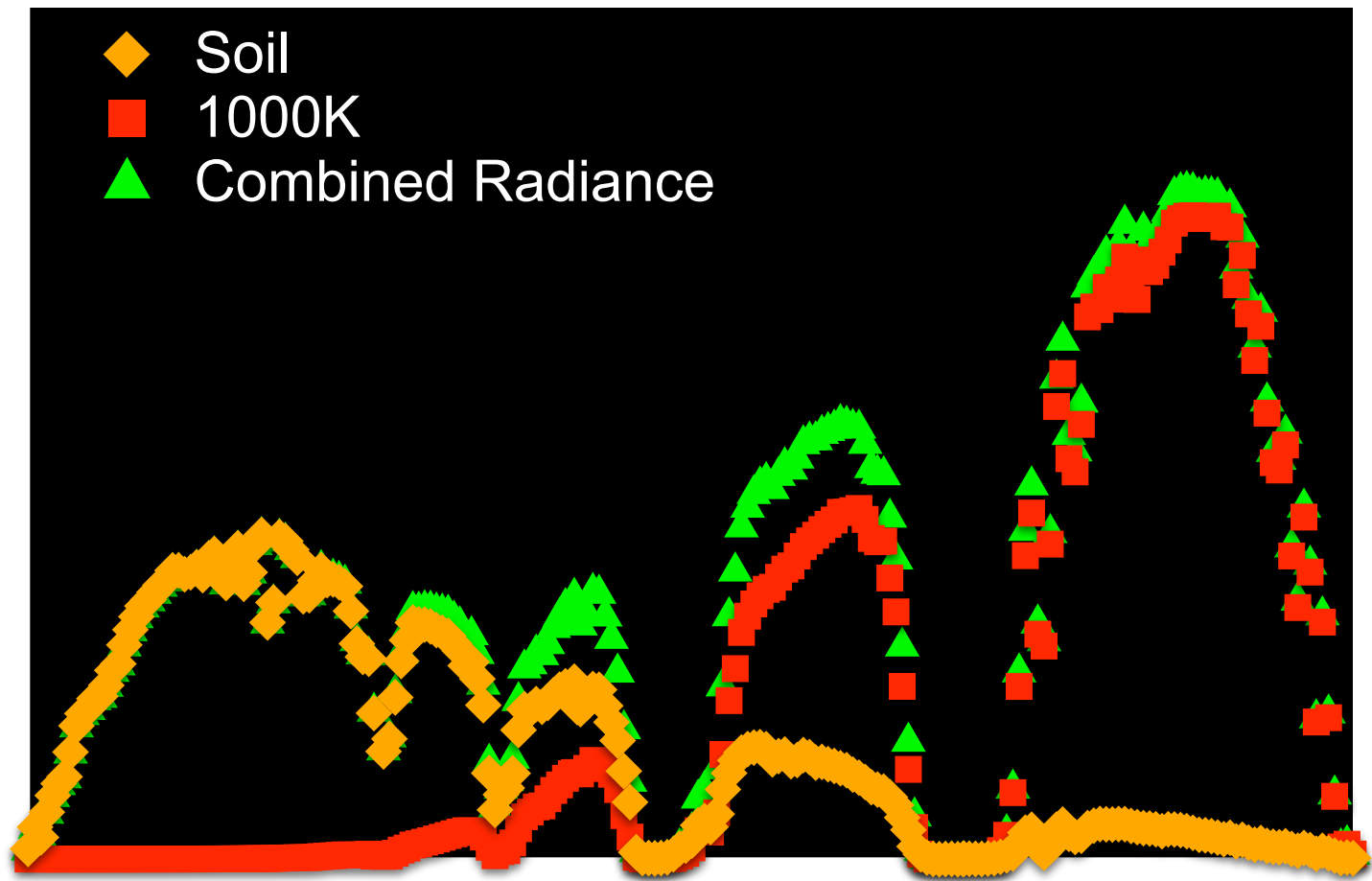


Dennison et al., 2005

# Subset of Emitted Thermal Radiance Endmembers



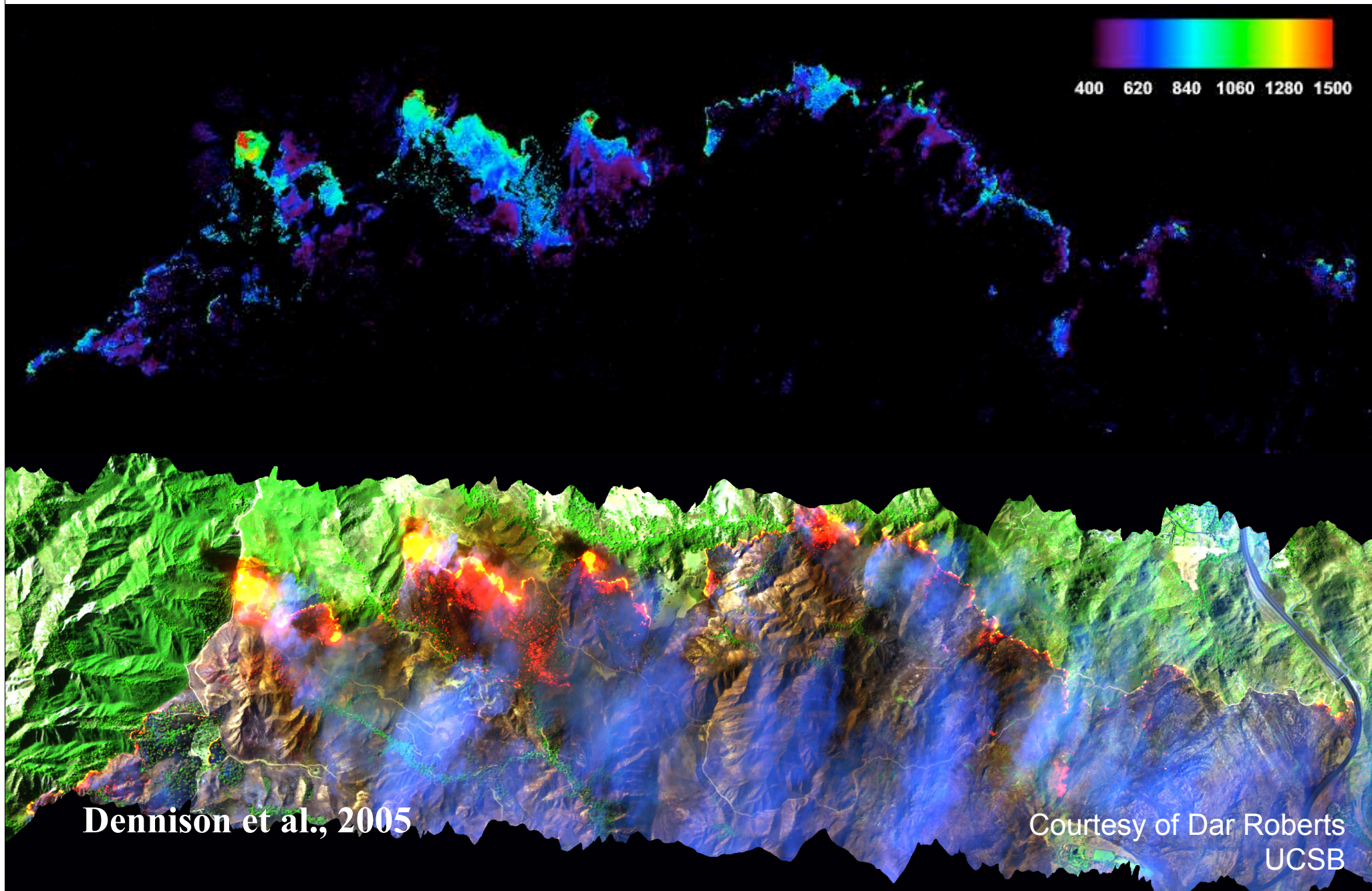
# Example: Mixed Radiance



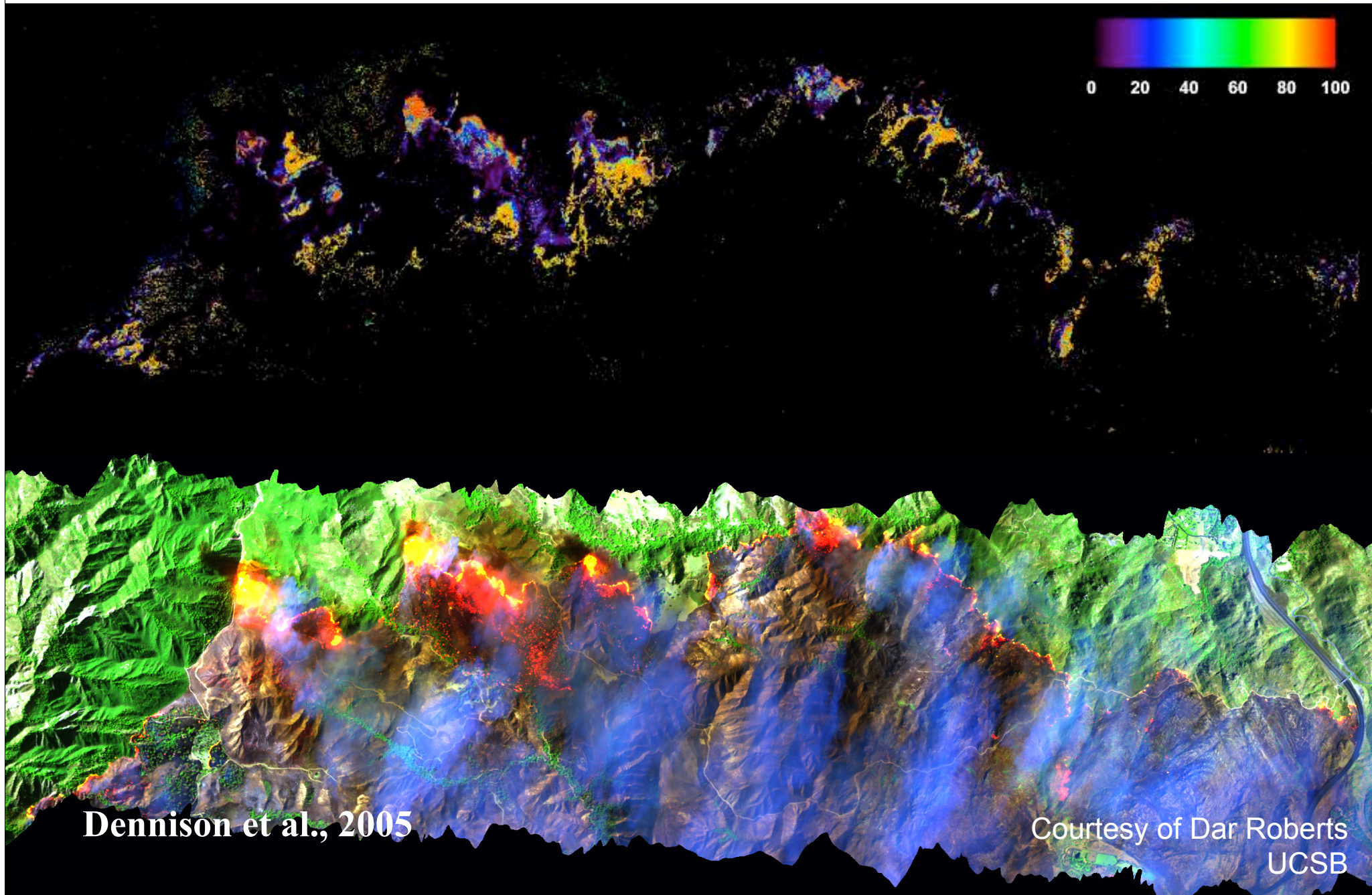
Dennison et al., 2005



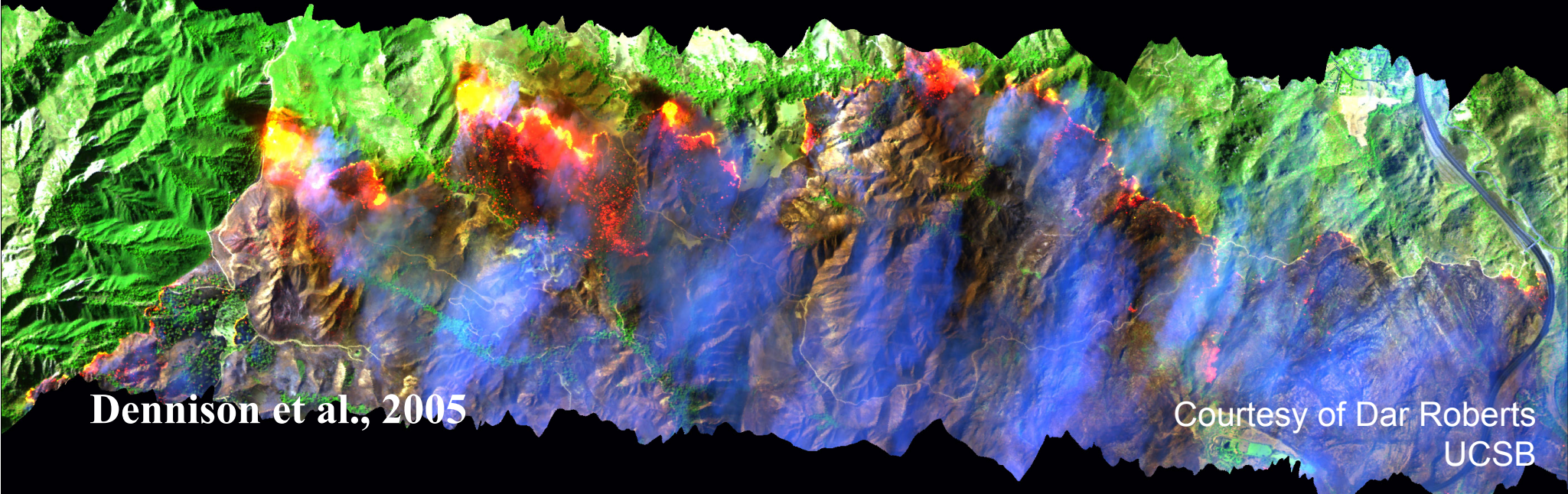
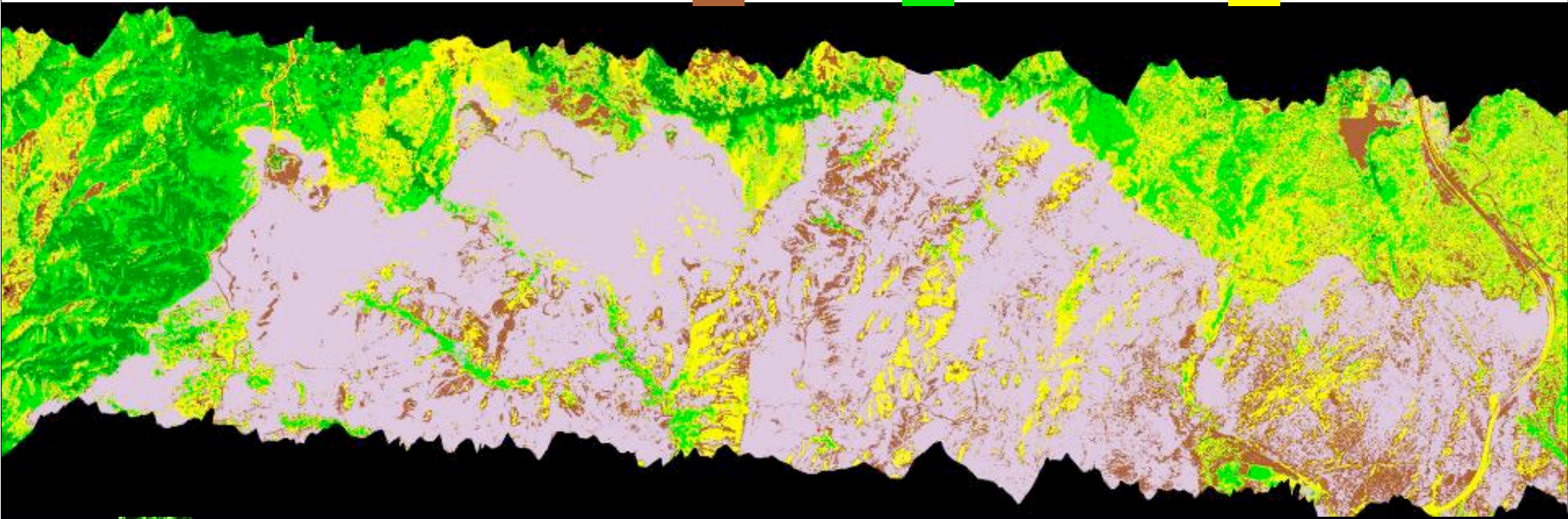
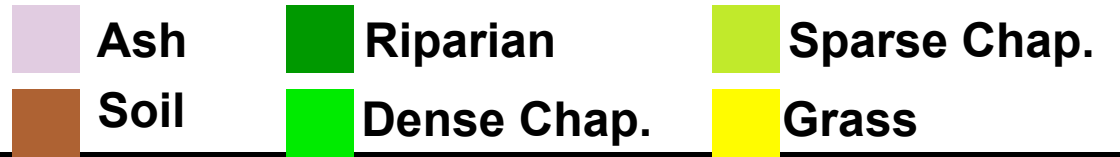
# Retrieved Temperature Endmembers



# Retrieved Temperature Fraction



# Land Cover



Dennison et al., 2005

Courtesy of Dar Roberts  
UCSB

# Motivation for Urban Environments

- Urban Environments are Challenging
  - The diversity of materials is high
  - The scale at which surfaces are homogeneous is typically below the spatial resolution of spaceborne and airborne sensors
- New Remote Sensing Technologies need to be Evaluated
  - Hyperspectral: AVIRIS, Hyperion, HYMAP
  - Hyperspatial: IKONOS Panchromatic
  - LIDAR: Fine vertical resolution
  - SAR: Interferometry

# AVIRIS - Santa Barbara, California

Oct 11, 1999 low-altitude data - 4 meter GIFOV



Red 1684 nm

Green 1106 nm

Blue 675 nm



Courtesy of Dar Roberts  
UCSB

# Each pixel is a spectrum

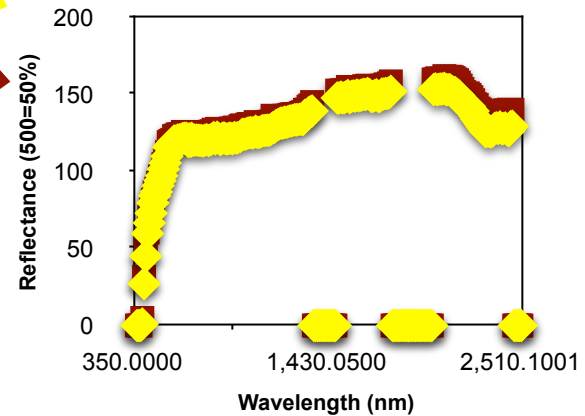
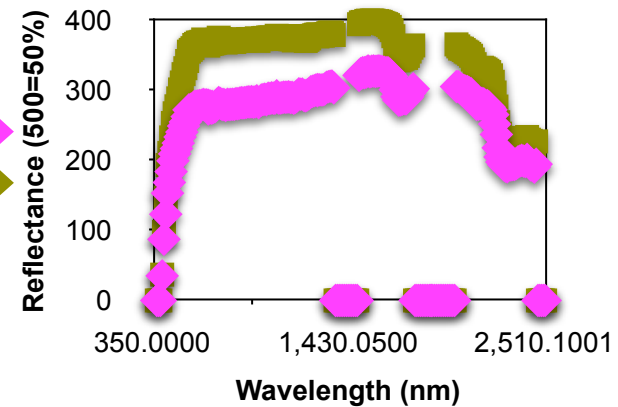
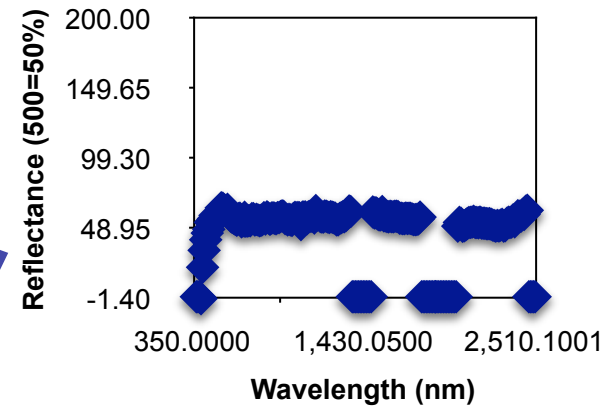
Potential for library development is large



AVIRIS 991011

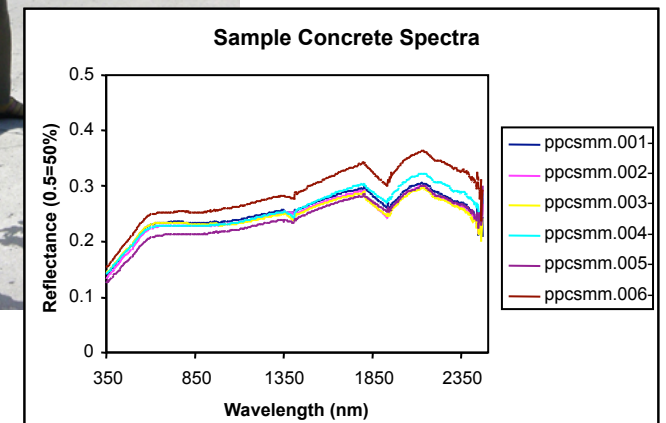
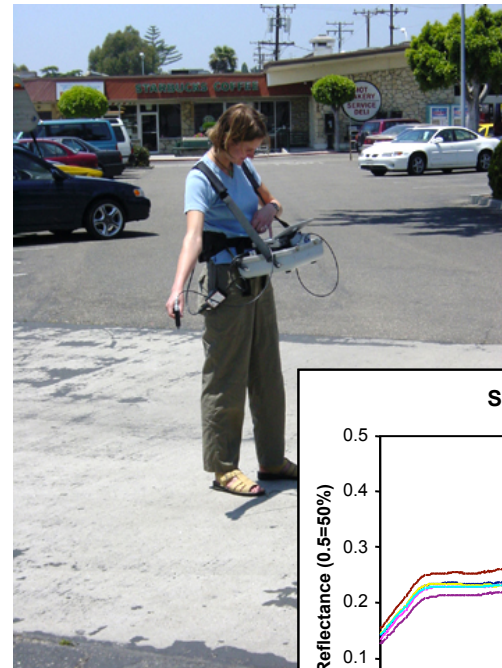
Red = 1684 nm  
 Green = 1106 nm  
 Blue = 675 nm

Courtesy of Dar Roberts  
 UCSB



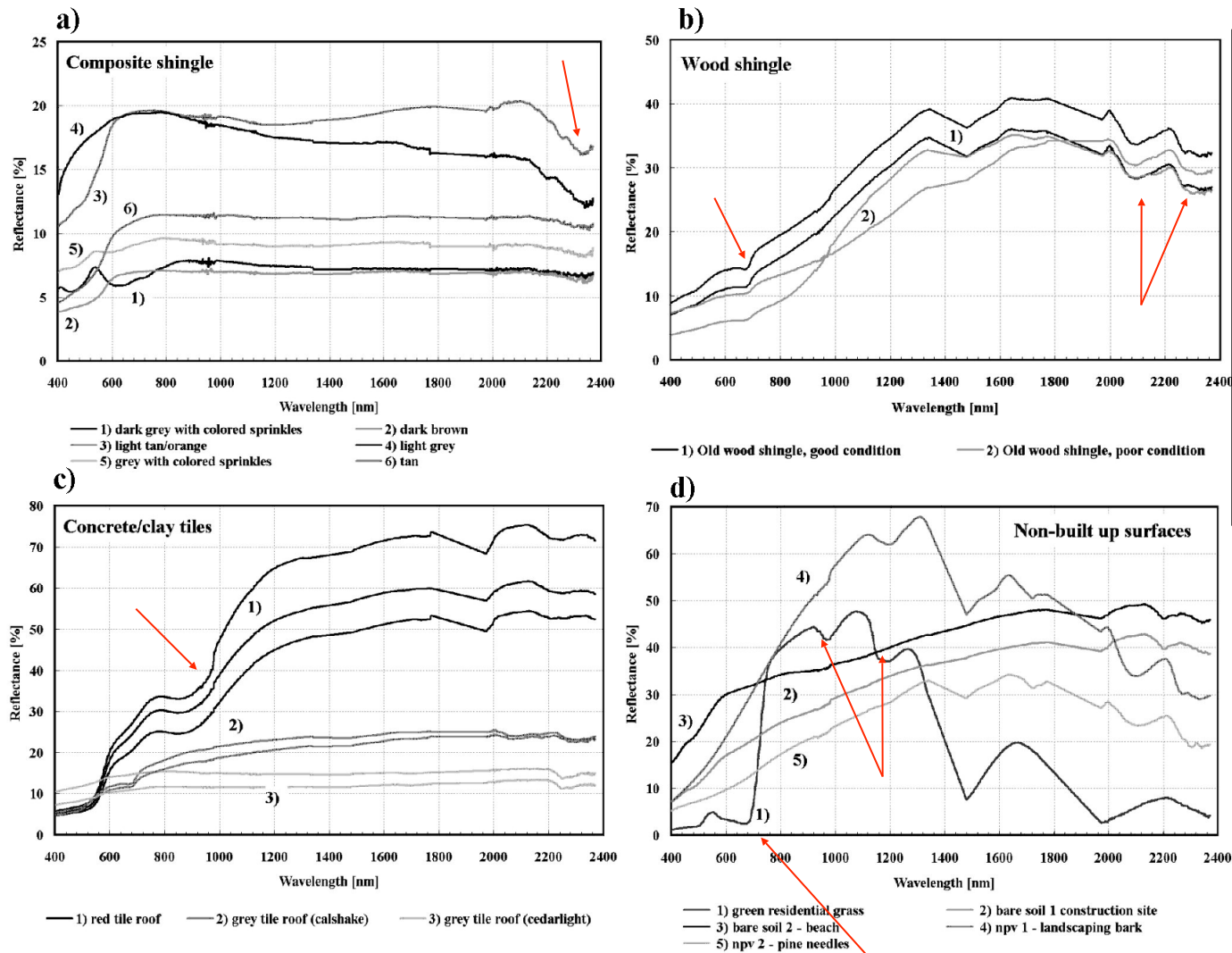
# Field Spectra Summary

- **Over 6,500 urban field spectra were collected throughout Santa Barbara in May & June 2001**
- **Field spectra were averaged in sets of 5 and labeled appropriately in building the urban spectral library**
- **The resulting urban spectral library includes:**
  - 499 roof spectra
  - 179 road spectra
  - 66 sidewalk spectra
  - 56 parking lot spectra
  - 40 road paint spectra
  - 37 vegetation spectra
  - 47 non-photosynthetic vegetation spectra
    - (ie. Landscaping bark, dead wood)
  - 27 tennis court spectra
  - 88 bare soil and beach spectra
  - 50 miscellaneous other urban spectra



Courtesy of Dar Roberts  
UCSB

# Example Spectra: Roofs



**Key Absorptions**

**Composite Shingle:** carbonates, asphalt

**Wood Shingle:** ligno-cellulose

**Tile:** iron-oxides

**Plants:** Liquid water, chlorophyll, ligno-cellulose

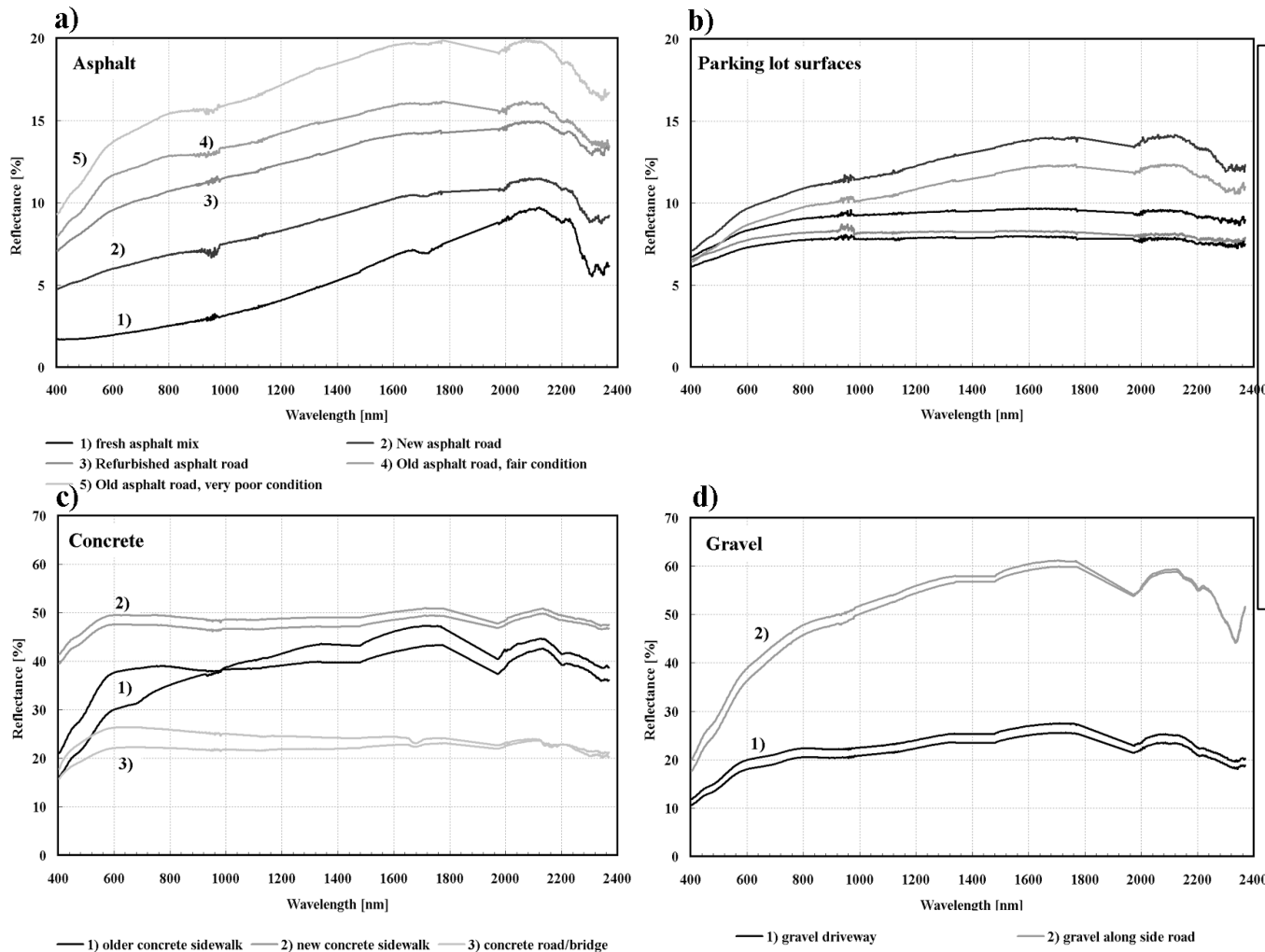
**Note, age is important**

Figure 5

Roberts and Herold, 2004



# Example Spectra: Transportation Surfaces



## Key Absorptions

**Asphalt:** Hydrocarbons, aging

**Parking lots:** featureless, dark

**Concrete:** carbonates?

**Gravel:** depends on source material

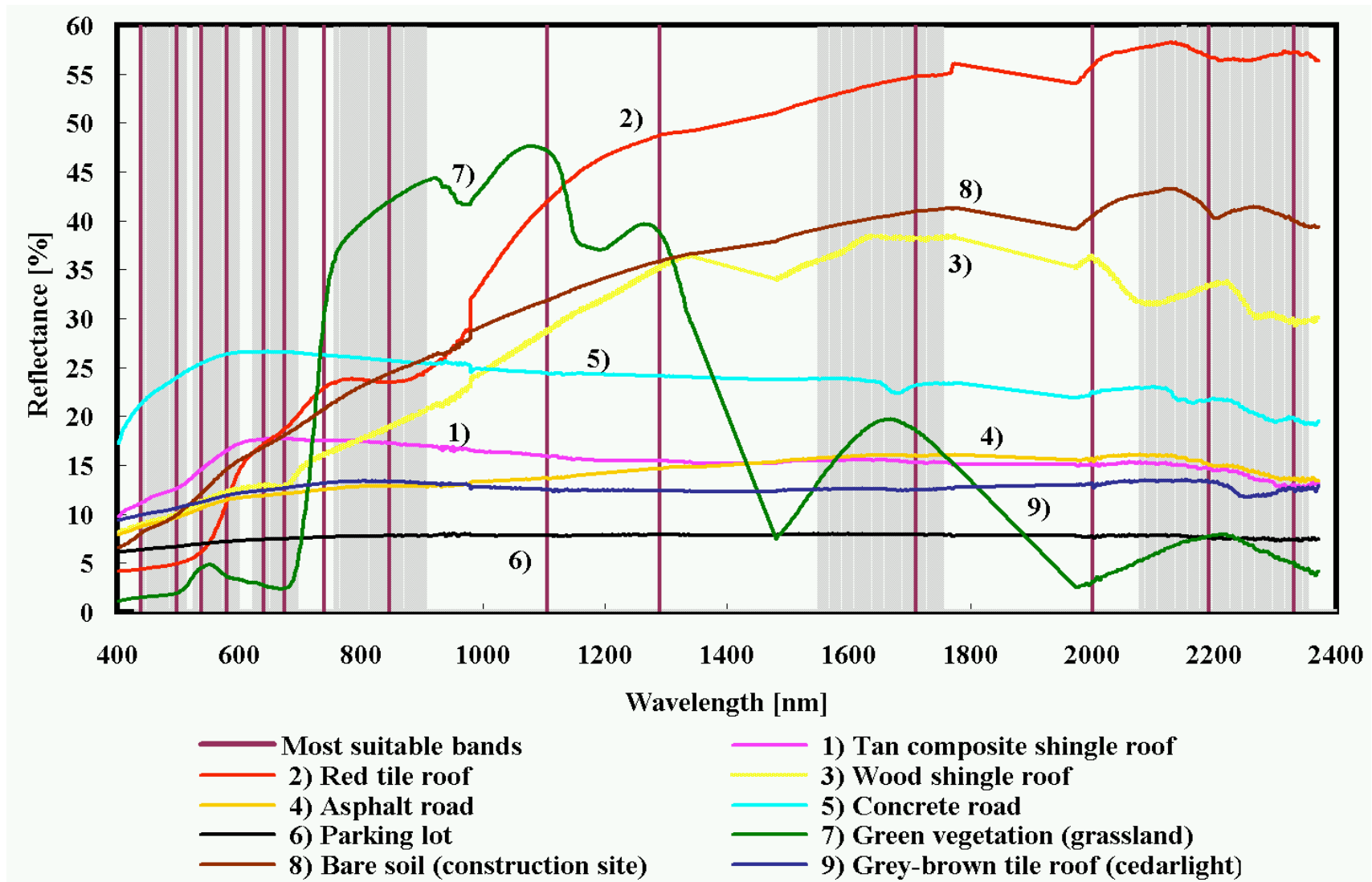
**Concretes darken with age**  
**Pavement gets brighter**

Figure 6

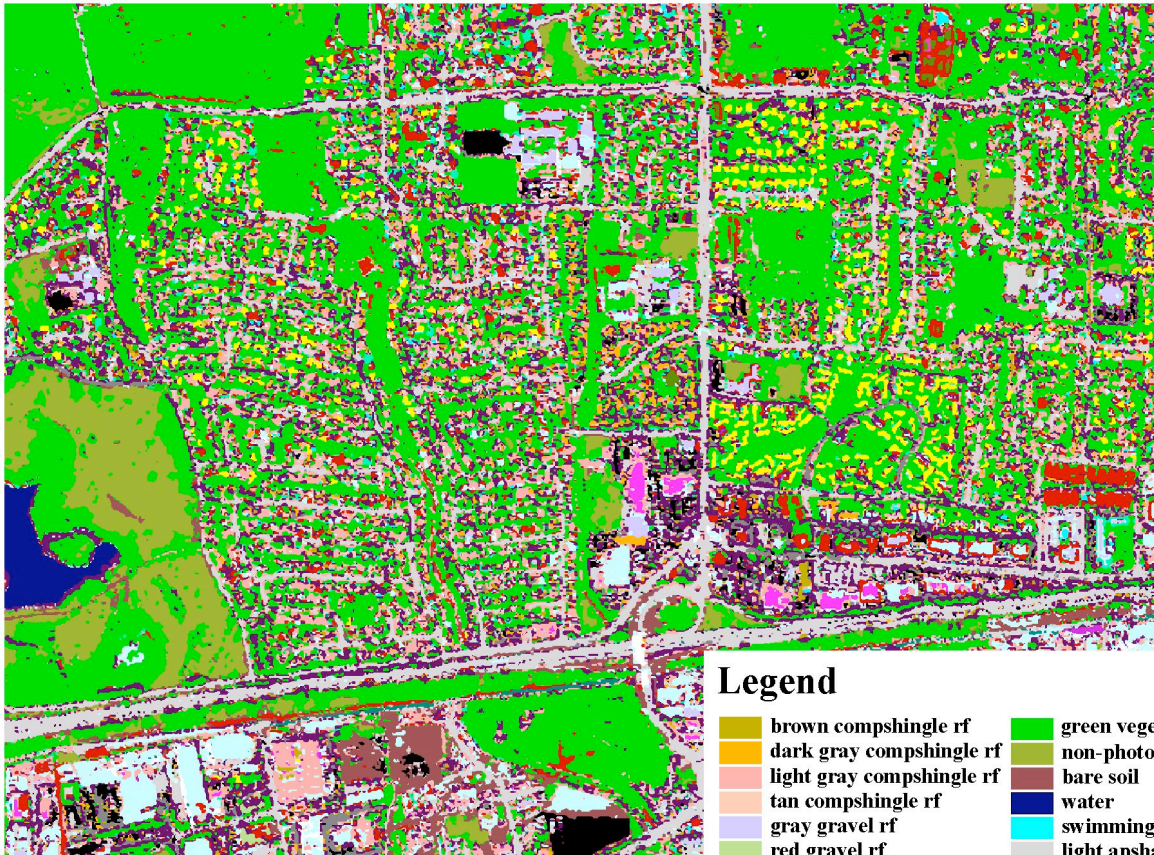
Roberts and Herold, 2004

# Most suitable spectral bands

## Top 14 selected based on Bhattacharyya -distance

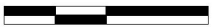


# Land cover mapping



- 14 most suitable bands
- 26 land cover classes
- 22 built up classes
- Inter-class confusion confirms sep. analysis
- Spectral limitations:
  - # and location of bands
  - Narrow vs. broadband

0.25 0 0.25 Kilometers



## Legend

<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFA500; border: 1px solid black;"></span> brown compshingle rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #00FF00; border: 1px solid black;"></span> green vegetation
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FF8C00; border: 1px solid black;"></span> dark gray compshingle rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #90EE90; border: 1px solid black;"></span> non-photosyn. veg.
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFDAB9; border: 1px solid black;"></span> light gray compshingle rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #A0522D; border: 1px solid black;"></span> bare soil
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFC0CB; border: 1px solid black;"></span> tan compshingle rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #00008B; border: 1px solid black;"></span> water
<span style="display: inline-block; width: 15px; height: 15px; background-color: #D8BFD8; border: 1px solid black;"></span> gray gravel rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #00CED1; border: 1px solid black;"></span> swimming pool
<span style="display: inline-block; width: 15px; height: 15px; background-color: #90EE90; border: 1px solid black;"></span> red gravel rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #D3D3D3; border: 1px solid black;"></span> light asphalt road
<span style="display: inline-block; width: 15px; height: 15px; background-color: #40E0D0; border: 1px solid black;"></span> brown metal rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #808080; border: 1px solid black;"></span> dark asphalt road
<span style="display: inline-block; width: 15px; height: 15px; background-color: #ADD8E6; border: 1px solid black;"></span> light gray metal rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFFFFF; border: 1px solid black;"></span> concrete road
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFC0CB; border: 1px solid black;"></span> light gray asphalt rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #4682B4; border: 1px solid black;"></span> gravel road
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FF4500; border: 1px solid black;"></span> red tile rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #000000; border: 1px solid black;"></span> parking lot
<span style="display: inline-block; width: 15px; height: 15px; background-color: #654321; border: 1px solid black;"></span> gray-brown tile	<span style="display: inline-block; width: 15px; height: 15px; background-color: #2E8B57; border: 1px solid black;"></span> railroad track
<span style="display: inline-block; width: 15px; height: 15px; background-color: #800080; border: 1px solid black;"></span> dark gray tar rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #808000; border: 1px solid black;"></span> tennis court
<span style="display: inline-block; width: 15px; height: 15px; background-color: #FFFF00; border: 1px solid black;"></span> wood shingle rf	<span style="display: inline-block; width: 15px; height: 15px; background-color: #FF00FF; border: 1px solid black;"></span> red sport tartan

## Overall Accuracy

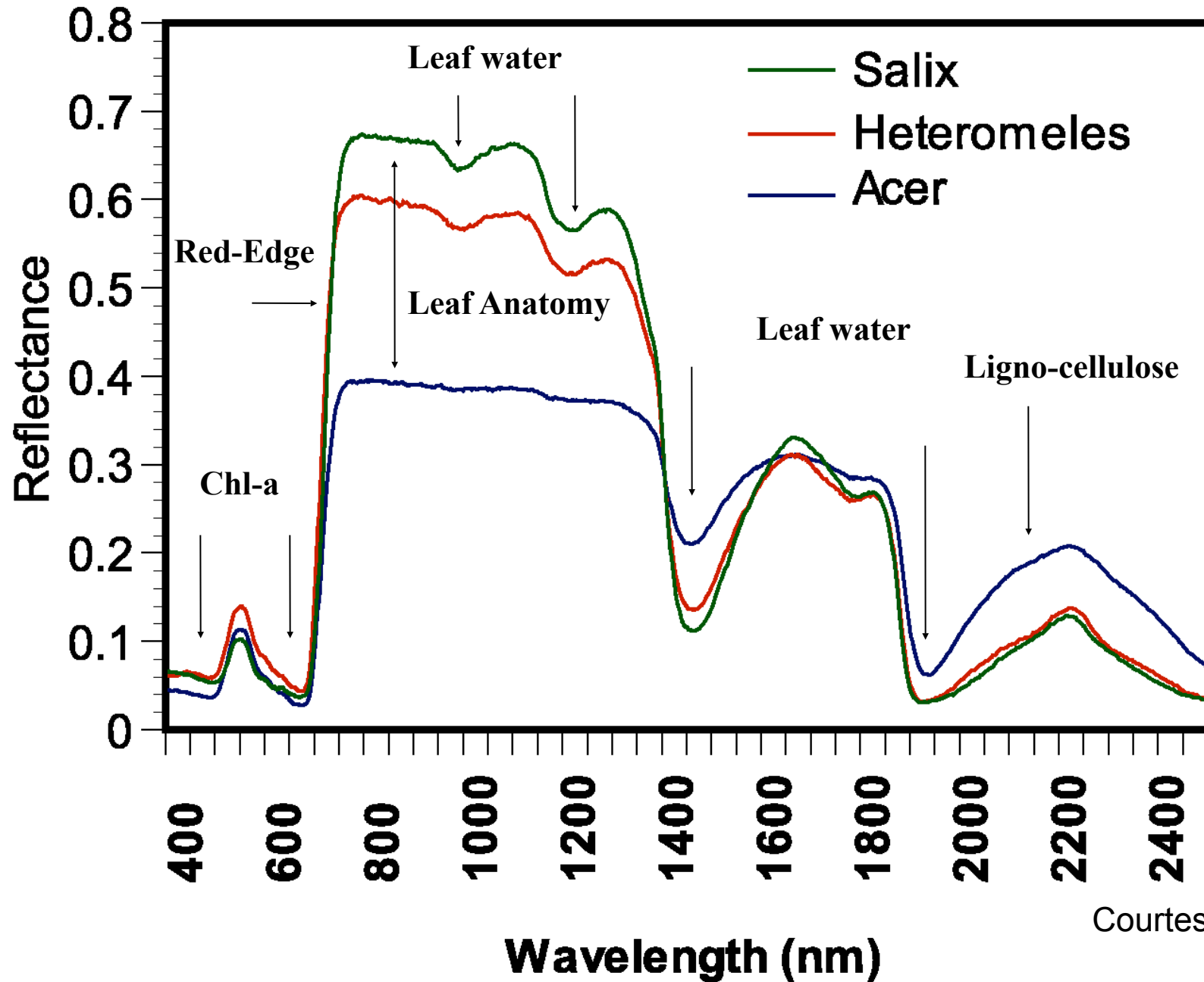
	Mean accuracy	Kappa coefficient	Area weighted accuracy	Built classes accuracy
IKONOS (4 bands)	61.8 %	60.2 %	66.6 %	37.7 %
Landsat TM (6 bands)	68.9 %	67.7 %	75.8 %	53.9 %
AVIRIS (14 bands)	73.5 %	72.5 %	82.0 %	66.6 %

From: Herold M., Gardner M. and Roberts D. 2003. Spectral Resolution Requirements for Mapping Urban Areas, IEEE Transactions on Geoscience and Remote Sensing, 41, 9, pp. 1907-1919

# Plant Stress and Physiology

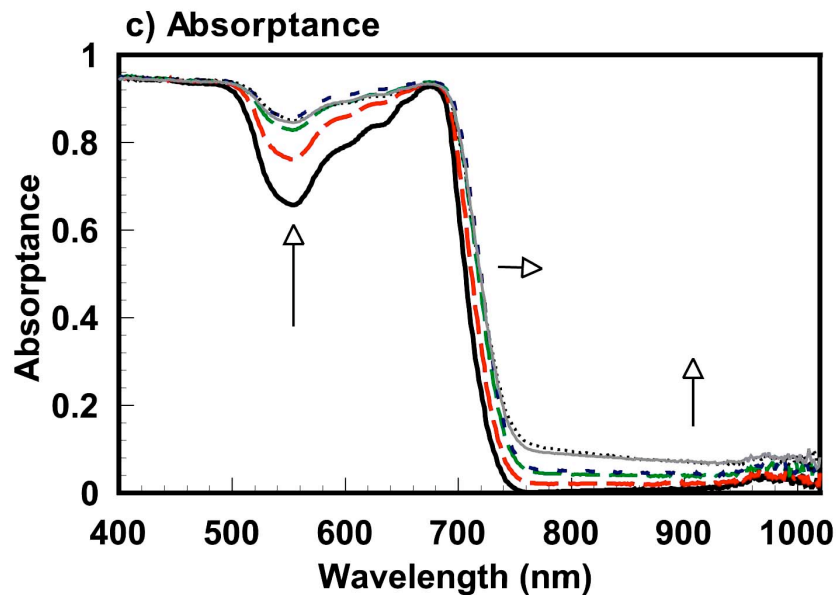
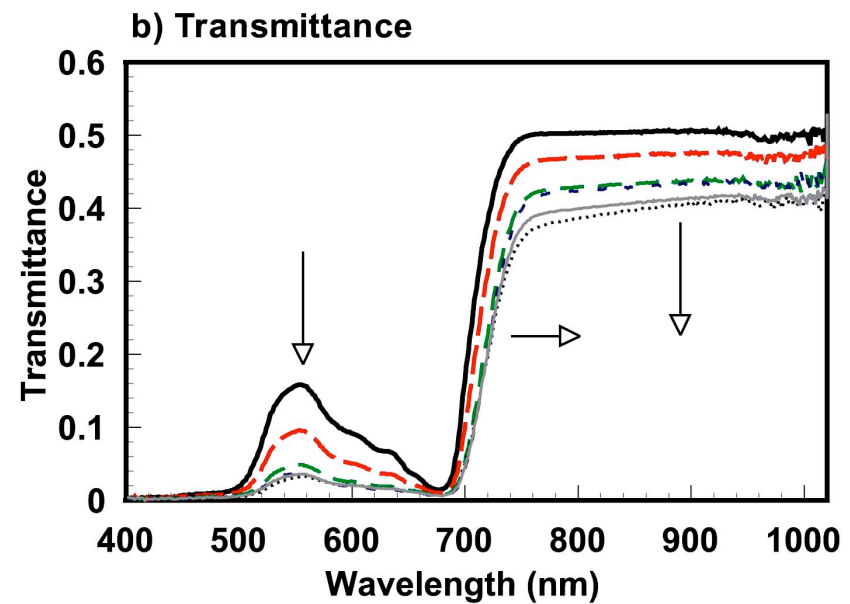
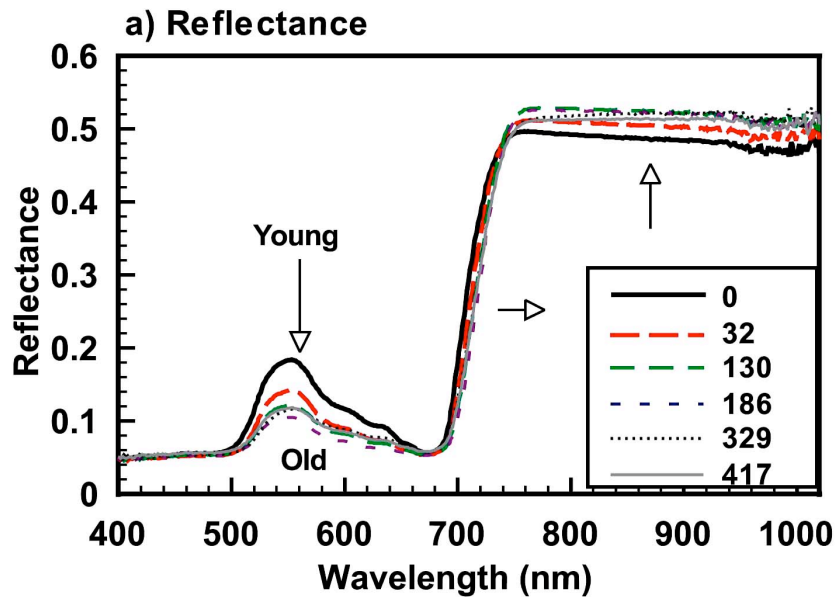
- Plant spectra are a product of multiscale processes
  - Leaf
    - Chemistry (pigments, water, ligno-cellulose)
    - Anatomy (thickness, internal structure)
    - Phenology
  - Branch
    - Density, orientation of leaves (LAI, LAD)
    - Exposed branches, litter and soil
  - Canopy and Stand
    - Crown geometry, leaf/branch density
    - Density, percent cover, species composition
- Imaging spectrometry provides detailed information on leaf/branch scale chemistry, architecture and how they change in response to stress

# Spectroscopy of Leaf Chemistry and Anatomy



Courtesy of Dar Roberts  
UCSB

# Leaf Aging Effects



Visible Reflectance decreases, NIR increases

Transmittance decreases

Absorptance increases

Red edge shifts to longer wavelengths

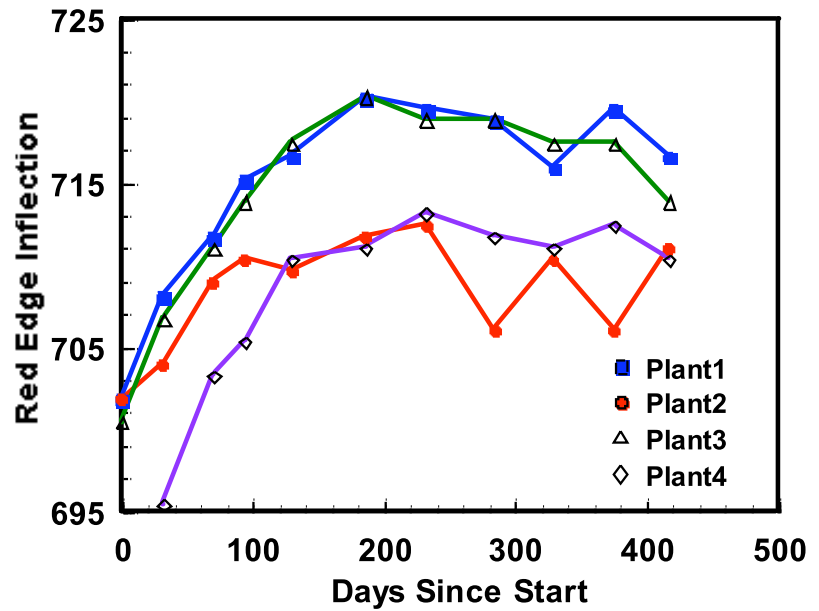
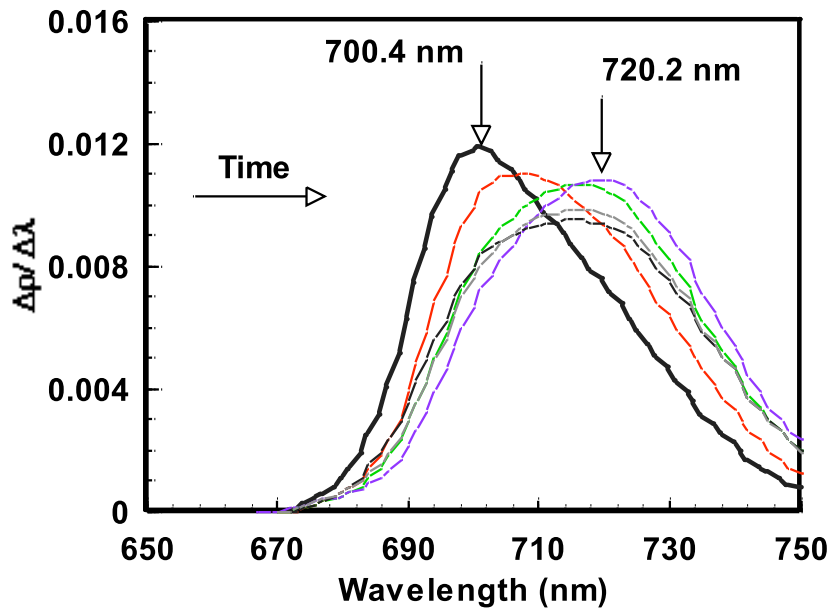
Roberts et al. 1998:  
Trees

# Physiological and Biophysical Measures

- Pigments
  - Non-linear least squares
  - Red Edge
- Stress
  - Red edge position
- Quantum efficiency
  - PRI
- Moisture
  - WI , NDWI , Water Thickness
- Evapotranspiration
  - Column Water Vapor
- Biophysical Measures
  - LAI, canopy cover, albedo

# Red Edge vs Leaf Age

*Aldina heterophylla*



Courtesy of Dar Roberts  
UCSB



# Red Edge and Stress

## NDVI:

$$\text{NDVI} = (R_{830} - R_{660}) / (R_{830} + R_{660})$$

Poor response at 20 m

## RVSI (Merton and Huntington, 1999)

$$\text{RVSI} = ((R_{714} + R_{752}) / 2) - R_{733}$$

Sensitive, 4 and 20 m

## PRI (Gamon et al., 1992)

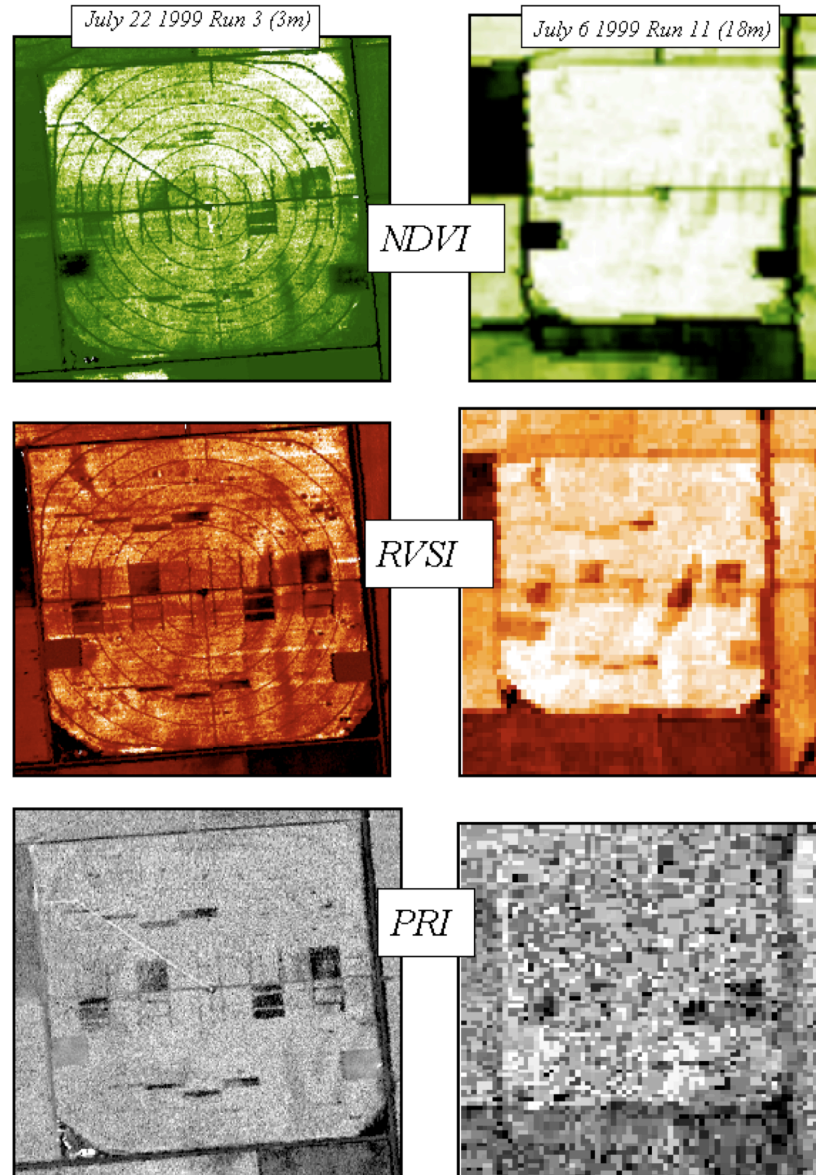
$$\text{PRI} = (R_{531} - R_{570}) / (R_{531} + R_{570})$$

Poor response at 20 m

Perry et al., 2002

Shelton NE

NASA EOCAP program



Courtesy of Dar Roberts  
UCSB

# Summary of Indices: Performance for Nitrogen Stress

Table 7. Ratios of Measured Index Value over Uncertainty<sup>1</sup>

Index	Visibility Uncertainty	1 nm Spectral Shift	2 nm Spectral Shift	View Angles	Reflectance Retrieval
PRI	1.6	0.7	0.4	<b>6.6</b>	1.4
NDVI	0.5	14.7	7.2	0.7	1.5
VI	0.4	13.5	6.6	0.7	1.3
SAVI	2.2	<b>74.1</b>	<b>34.9</b>	1.5	1.6
RVSI	<b>39.8</b>	3.9	1.9	<b>5.7</b>	<b>15.5</b>
GVI	3.7	<b>135.5</b>	<b>89.3</b>	1.3	<b>1.7</b>
Bright	3.7	<b>60.2</b>	<b>39.6</b>	0.4	1.6
Wet	<b>15.4</b>	29.8	18.1	0.6	<b>2.6</b>
NDWI	<b>8.3</b>	<b>83.3</b>	<b>41.3</b>	2.0	0.4
WI	5.9	26.5	12.0	<b>2.1</b>	0.9
Inflection.Pt	<b>11.9</b>	3.5	1.8	<b>5.3</b>	<b>1.7</b>
Liquid Water Thickness	<b>8.2</b>	-	-	2.0	0.7

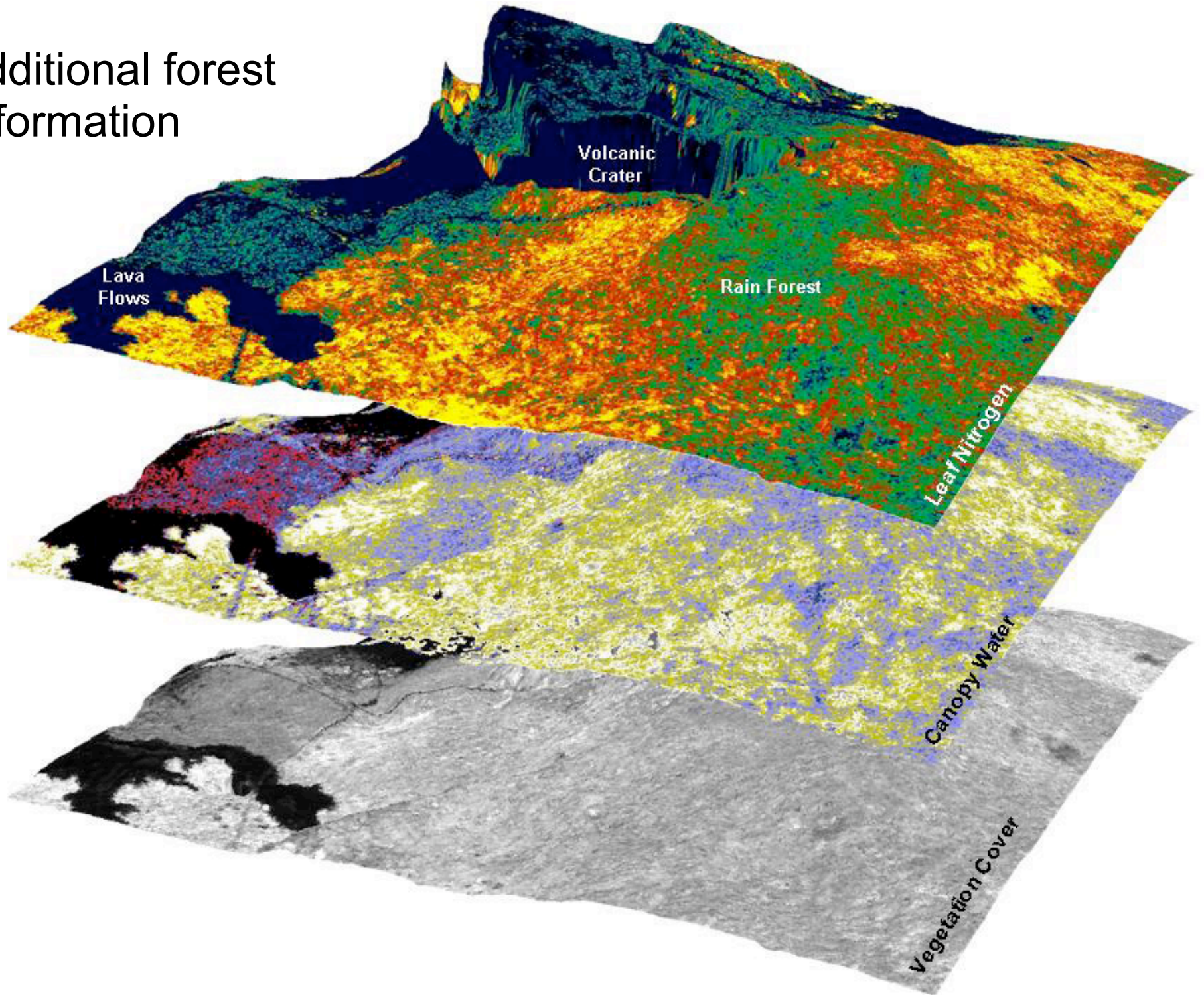
**N Levels 0, 50, 100, 150, 200 kg/ha**

**Calculated as the Signal divided by the Noise**

**High values are good, less than one is bad**

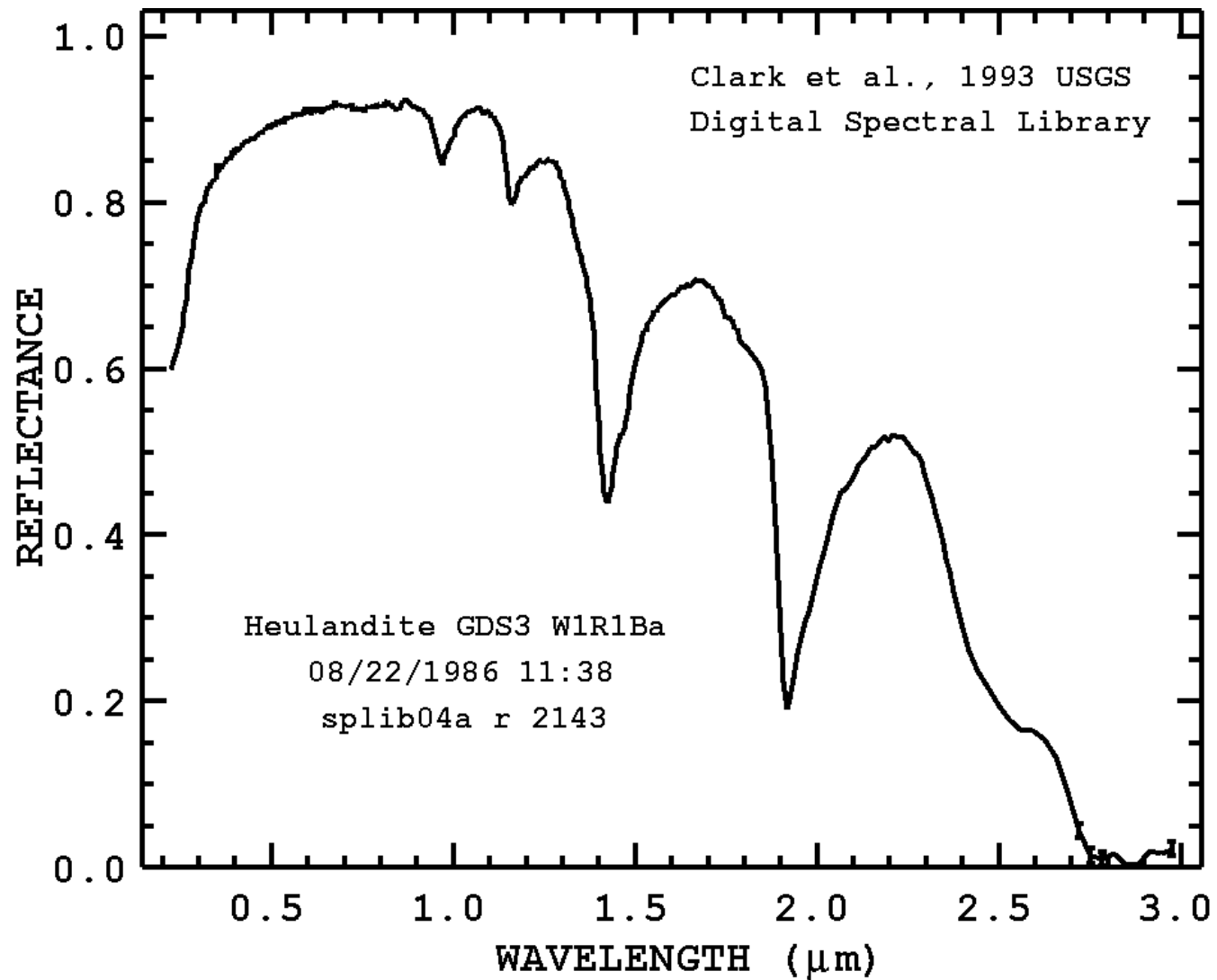
Courtesy of Dar Roberts  
UCSB

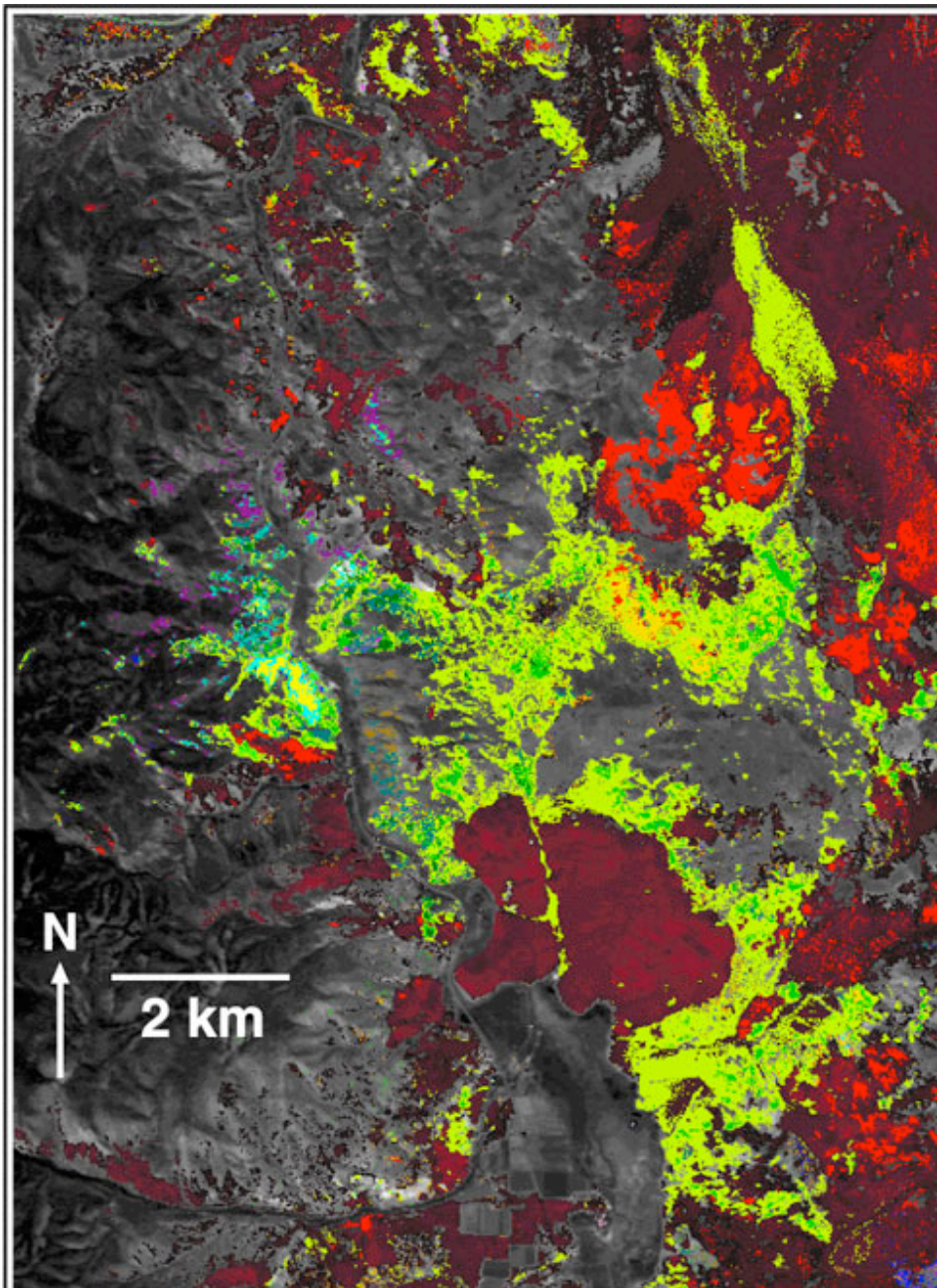
additional forest  
information



**Other applications**

# Mineral end-members?





USGS - EPA Utah AML Project

Rockwell et al., 2000

Fe Minerals and Water

Marysvale/Antelope Range

AVIRIS high altitude data

August 5, 1998

Run 10 subset

Tetracorder 3.6a5 Product

**Iron Sulfate Minerals**

- fine grained jarosite - propylitic zone
- coarse grained jarosite - argillic zone
- goethite + jarosite

**Iron Hydroxide Minerals**

- goethite - thin coating
- goethite - fine grained
- goethite - medium grained
- goethite - coarse grained

**Iron Oxide Minerals**

- hematite - fine grained
- hematite - med. to coarse grained

- Other iron oxides/hydroxides

**Fe<sup>2+</sup>-bearing minerals**

- generic
- with hematite
- with goethite and muscovite

**Piute Reservoir Sediment Load**

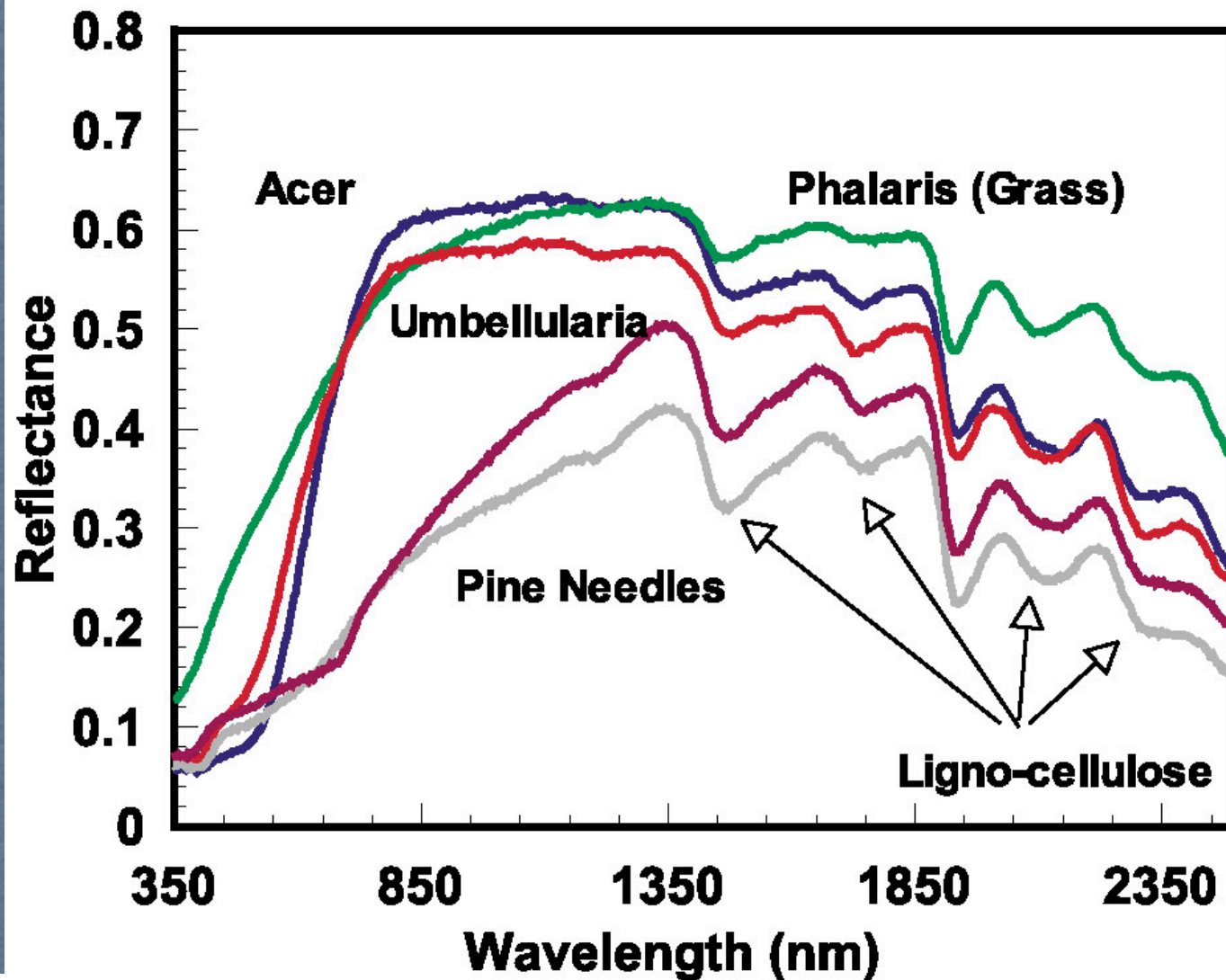


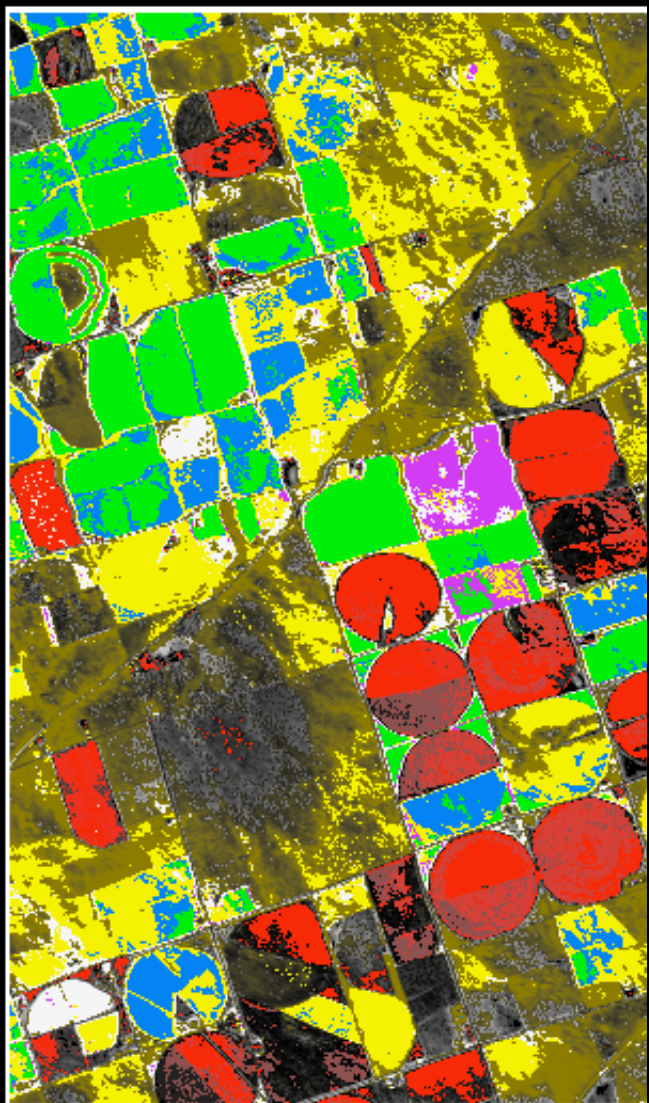
- water + chlorophyll
- water + red algae

- chlorite + muscovite
  - chlorite + goethite
- propylitic alteration**

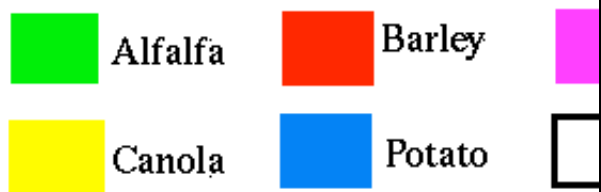
# Applications

non-photosynthetic vegetation (litter)



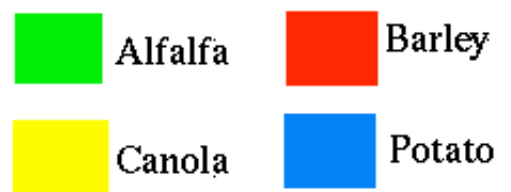


San Luis Valley, CO – V  
AVIRIS Sept. 3, 1993 Data

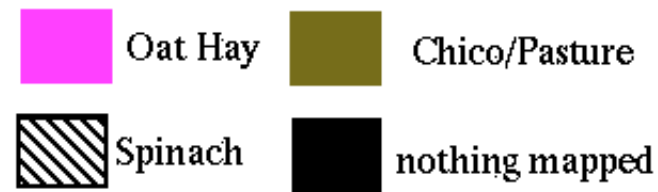


San Luis Valley, CO – Vegetation Distribution Map

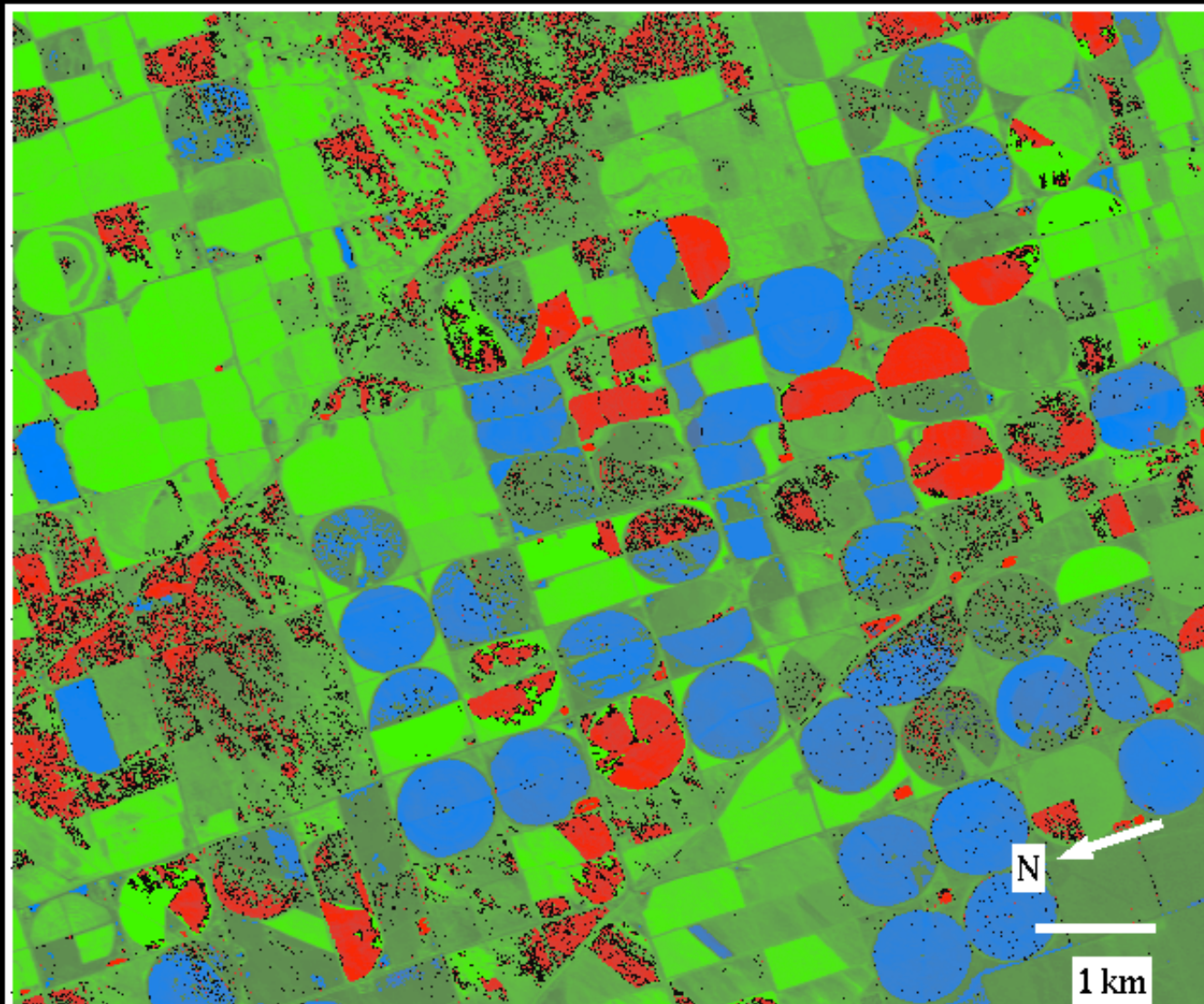
Field Verification Data



U. S. Geological Survey










San Luis Valley, CO – Vegetation Senescence/Stress Map

AVIRIS Sept 3, 1993 Data

U.S. Geological Survey

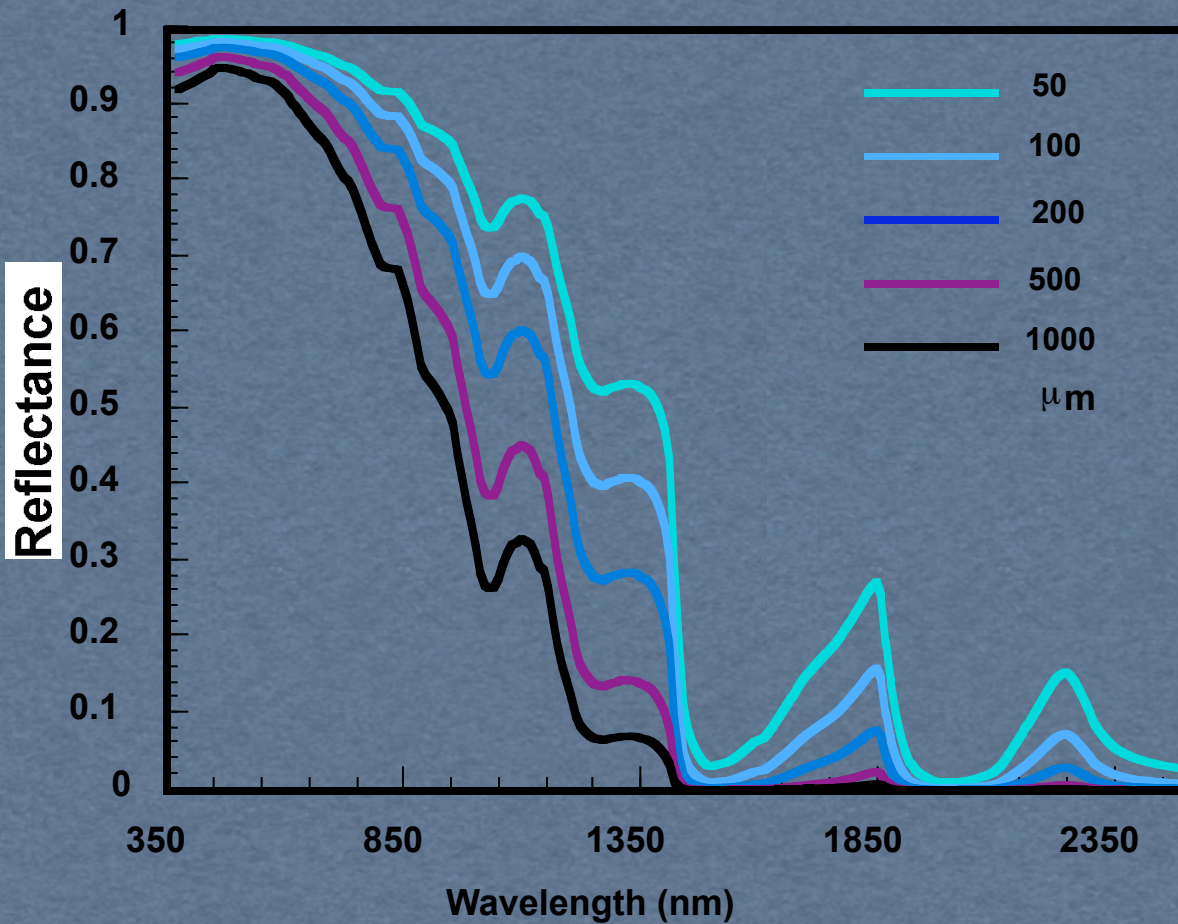
 Stressed Vegetation

 Green Vegetation

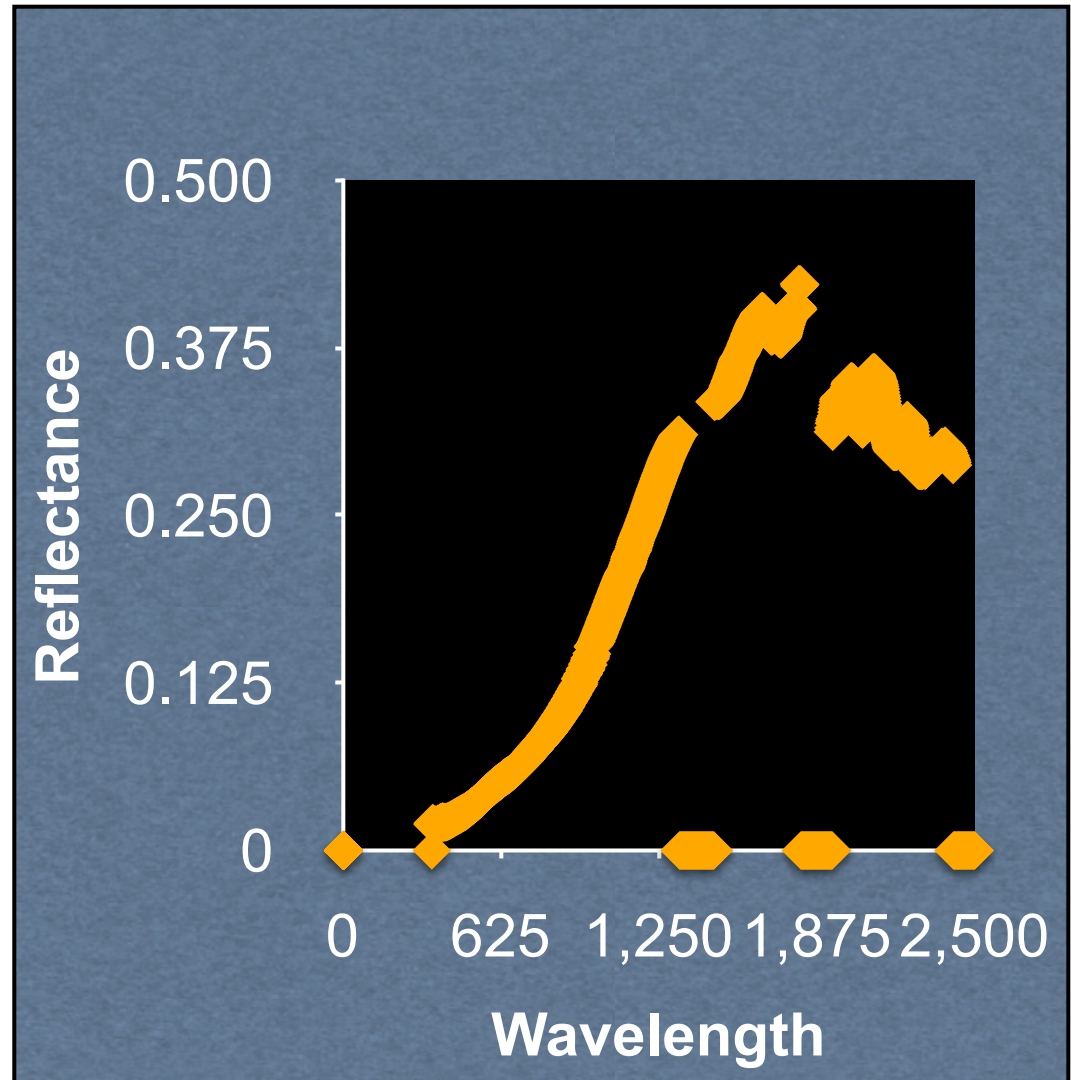
 Dry Vegetation  
and bare ground

# Snow Applications

grain size effects on snow reflectance



# *Gallus gallus* (common chicken)



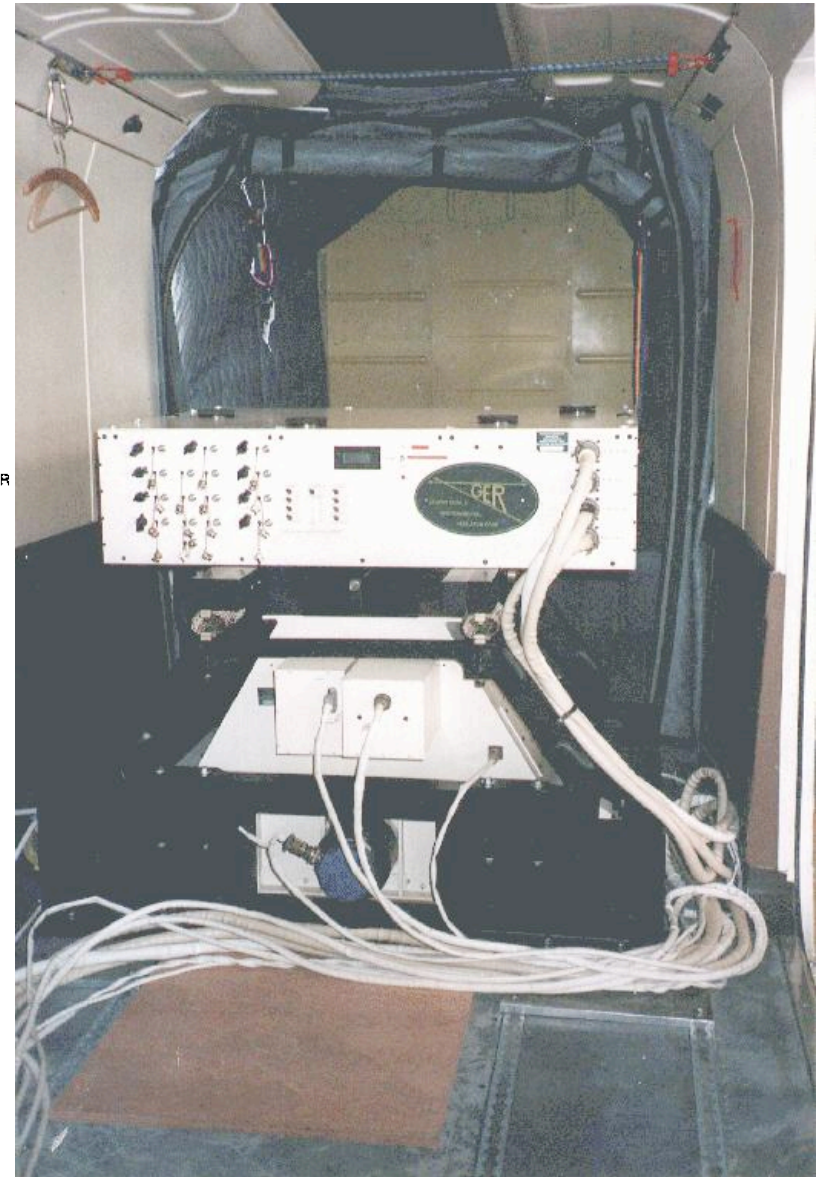
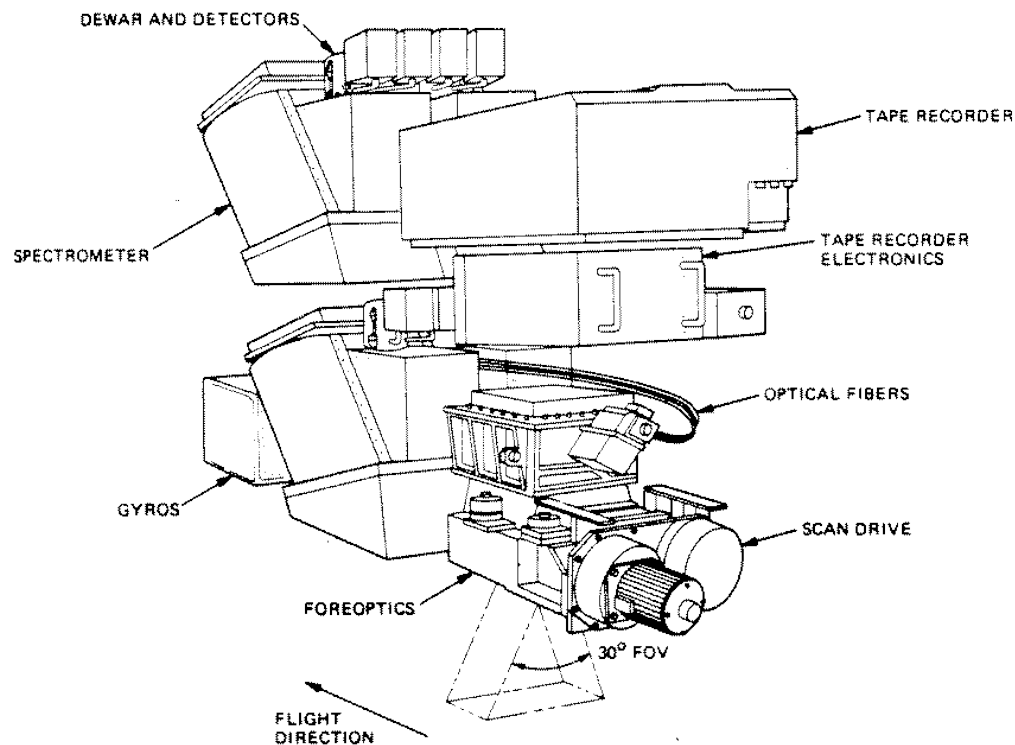
# Summary

- Imaging spectrometry has broad application for many disciplines
- The strength of imaging spectrometry is in its direct link to physical processes and flexibility
- Imaging spectrometry complements broad band systems, does not compete
- Examples shown here, only reveal a small part of the established potential

# Imaging spectroscopy data sources

data availability for imaging spectroscopy?

- mainly ground and airborne sensors



### Airborne Imaging Spectrometers:

<u>Name</u>	<u>Full name</u>	<u># of Bands</u>	<u>spectral coverage</u>
AVIRIS (JPL)	Airborne Visible/Near Infrard Imaging Spectr	224	400 – 2450 nm
CAESAR (NLR)	CCD Airborne Experimental Scanner for Applications in RS	12	520 – 780 nm
CASI (Itres)	Compact Airborne Spectro-graphic Imager	228	430 – 870 nm
DAIS7915 (DLR)	Digital Airborne Imaging Spectrometer	79	400 – 12000 nm
EPS-A	Environmental Probe System	32	400 – 12000 nm
GERIS	Geophysical & Environmental Research Imaging Spectrometer	63	400 – 2500 nm
HyMap	HyVista Australia	126	450 – 2500 nm

## Spaceborne Imaging Spectrometers:

<u>Name</u>	<u>Full name</u>	<u># of Bands</u>	<u>spectral coverage</u>
ASTER (JPL)	Advanced Spaceborne Thermal Emission & Reflectance Radiometer	14	520 – 11650 nm
MERIS (ESA)	Medium Resolution Imaging Spectrometer	15	400 – 1050 nm
MODIS (NASA)	Moderate Resolution Imaging Spectrometers	36	415 – 14240 nm
SPECTRA (ESA)	Optical & Thermal spectrometer - ESA Earth Explorer Mission - to be launched in 2008 (?) - significant Dutch contribution		400 – 14000 nm

# Methods



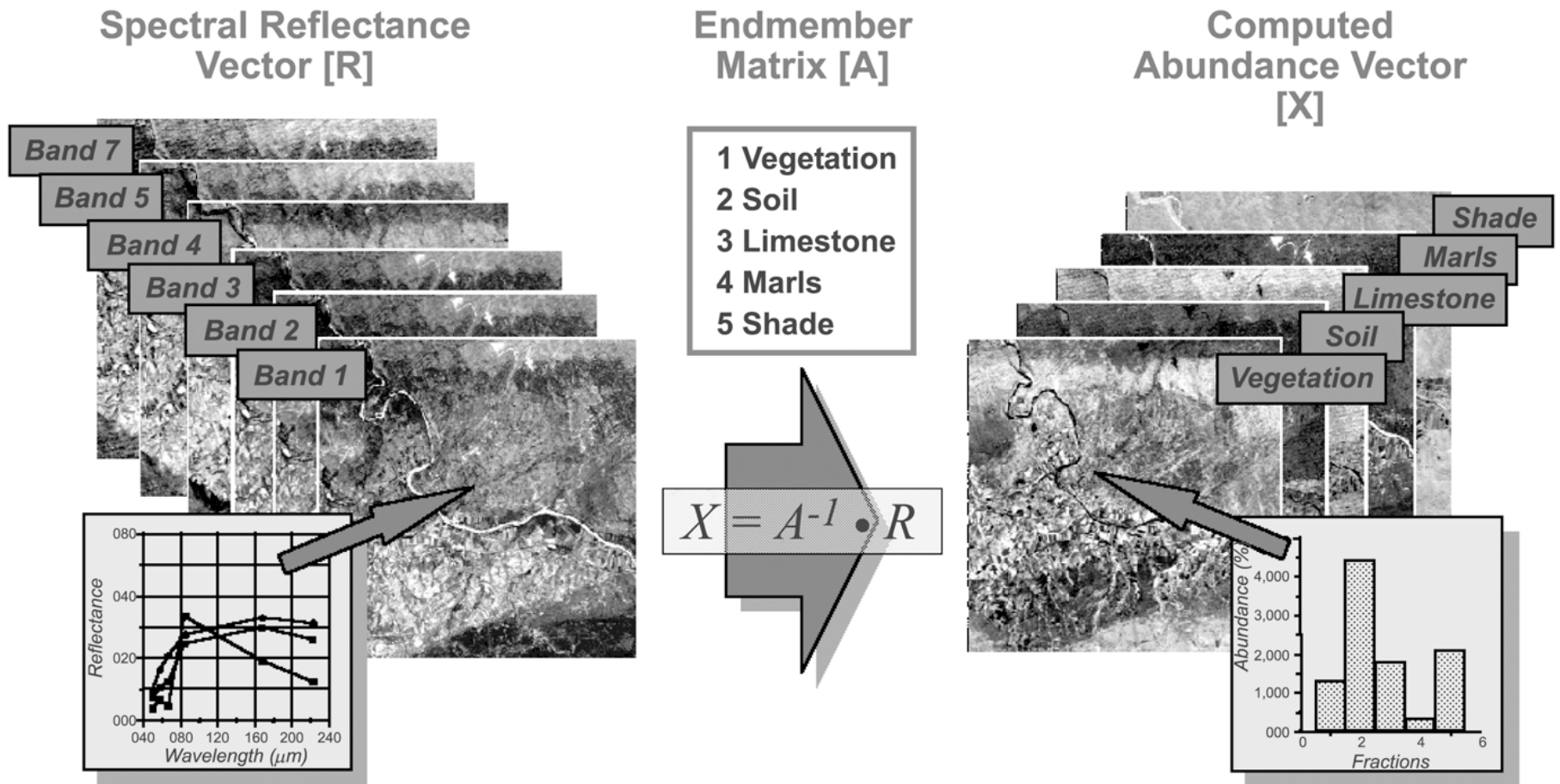
# What is mixture modeling?

- hard vs. soft (fuzzy) information extraction
- classification requires that each pixel be given a hard, unambiguous label especially in homogeneous areas (H-resolution)
- in other instances, especially when pixel size is larger than homogenous objects (L-resolution) the land cover is in essence mixture of different land covers
- The purpose of mixture modeling is to estimate the proportion of individual elements (land cover objects) within individual pixels and it is an L-resolution problem.

# What is mixture modeling?

- Classification - categorical estimation
  - cookie-cutter model
- Mixture modeling - continuous estimation
  - blender model
- there is improved technology and imagery
- there is increased demand for information such as secondary labels for vegetation
- soft (fuzzy) output maps

# Spectral Unmixing



Unmixing accomplished via linear estimation,  
Supervised learning, or automated approaches

# Kinds of mixture modeling

- linear vs. non-linear
- simple vs. probability-based
- supervised vs. unsupervised
- empirical vs. deterministic

Pixel (x,y) as spectral  
measurement

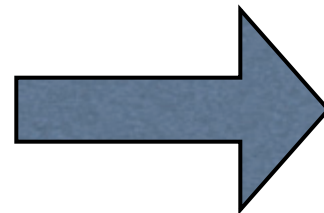
Band 1 52 DN

Band 2 99 DN

Band 3 13 DN

Band 4 25 DN

data



transformation

Pixel (x,y) as fraction  
measurement

Endmember A 0.4

Endmember B 0.6

# Linear mixture modeling

- It can be assumed that the magnitude of a single photon reflected from the Earth's surface into the sensor field-of-view (pixel) is describable in terms of a simple linear model:

$$r_i = \sum_{j=1}^n a_{ij} f_j + e_i$$

we are interested  
in the inverse of  
this equation

$r_i$  = reflectance in  $i$ th spectral band

$a_{ij}$  = reflectance of  $j$ th end-member in  $i$ th spectral band




$f_j$  = proportion of end-member  $j$

$e_i$  = difference between observed and modeled reflectance (error)



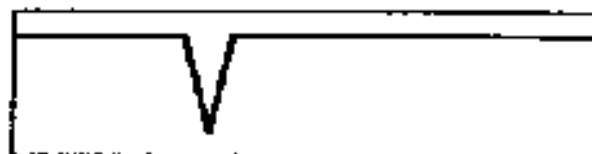
IFOV of pixel

a single pixel with three materials: A B and C

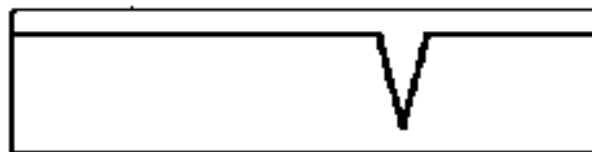
material		fraction
A		0.25
B		0.25
C		0.50

each endmember has a unique spectrum

A



B



C



the mixed spectrum is just a weighted average

$$\text{mix} = 0.25 \cdot A + 0.25 \cdot B + 0.5 \cdot C$$



# Linear mixture modeling

- In order for the components ( $r$ ) to be computed, the number of end-members must be less than the number of spectral bands
- This model simply expresses the fact that the integrated signal ( $r$ ) received at sensor in a given band will be a linear sum of all individual signals from individual land cover types
- The constraint specifies that the individual fractions must take values between 0 and 100 percent and that the fractions for any given mixed pixel must sum to 100 percent or less.

# What are end-members?

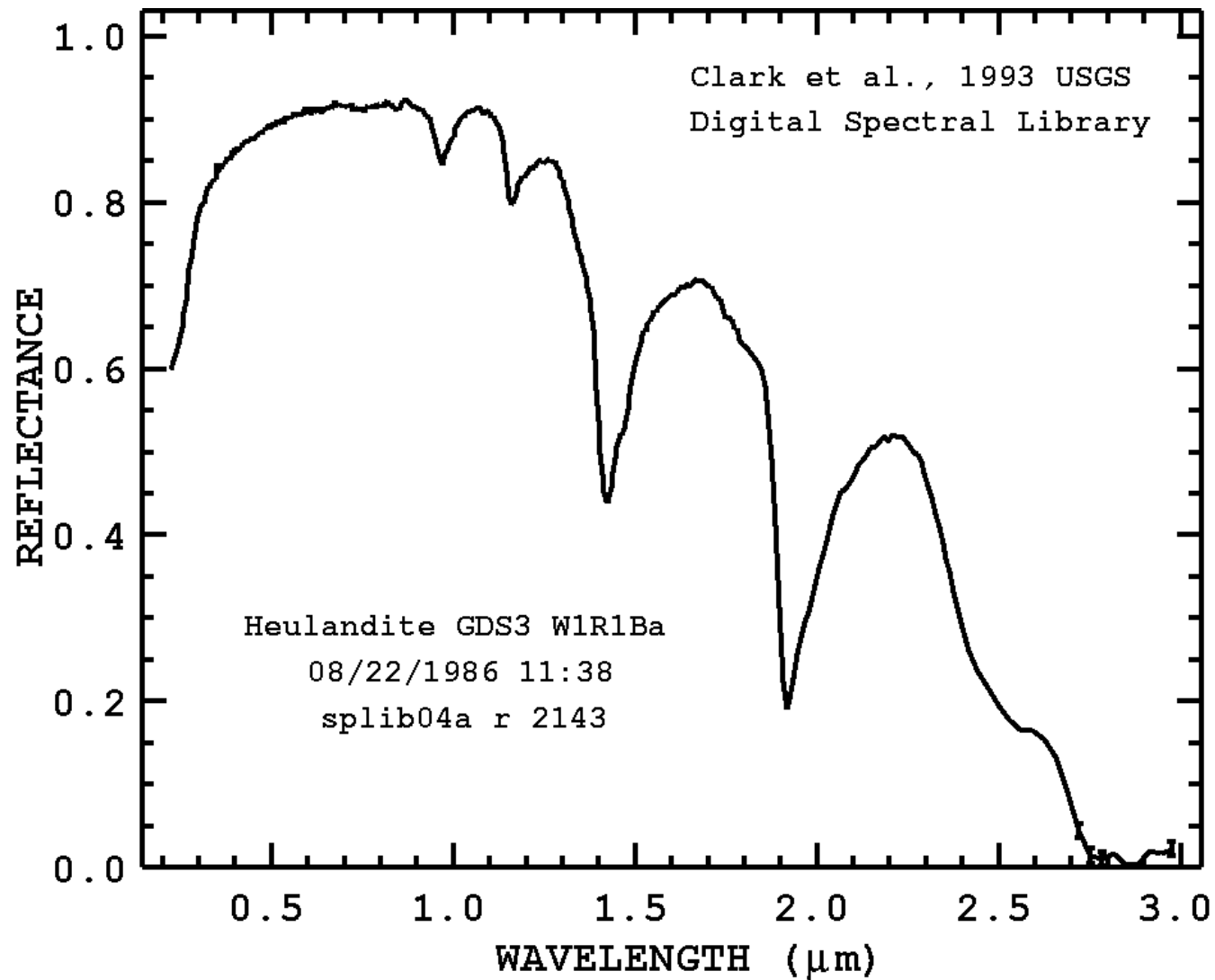
- End-member refers to spectral phenomena where the pure form of the category of interest (green leaves, soils, shade, water etc...)
- End-members are spectral only, and do not represent materials although spectra may represent materials
- End-members in an image refer to pixels (or locations) whose reflectance value corresponds to the reflectance value of the pure spectral sample
- These end-members correspond to the materials with spectra that combine linearly to produce all of the spectra in the image



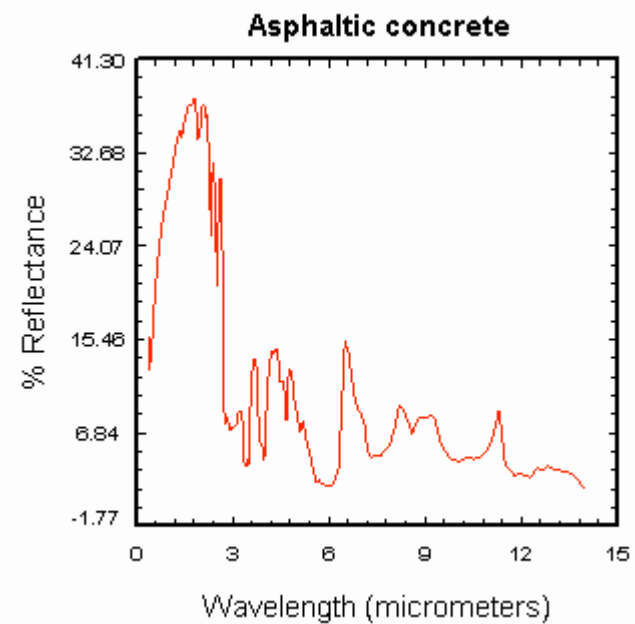
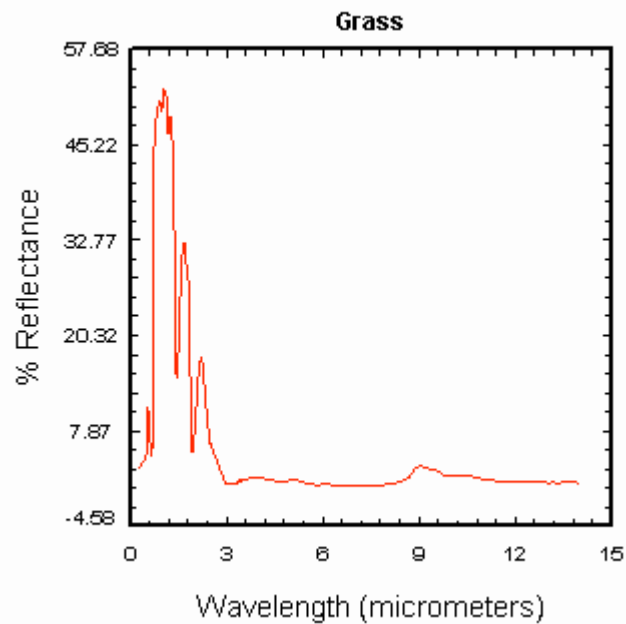
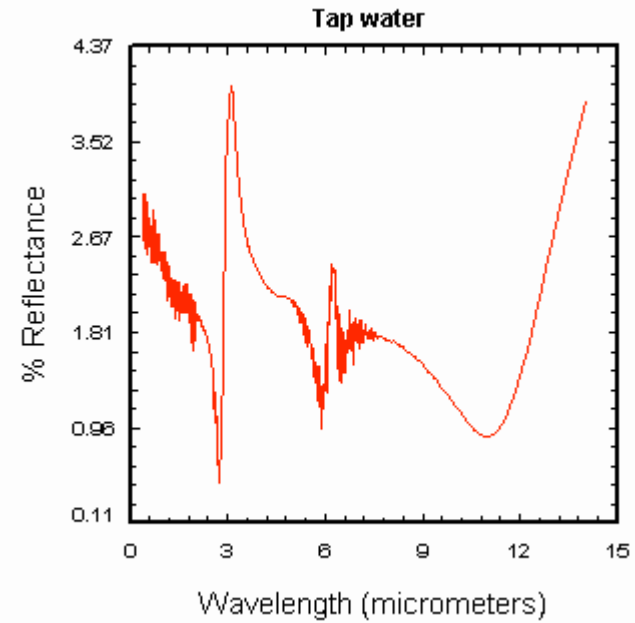
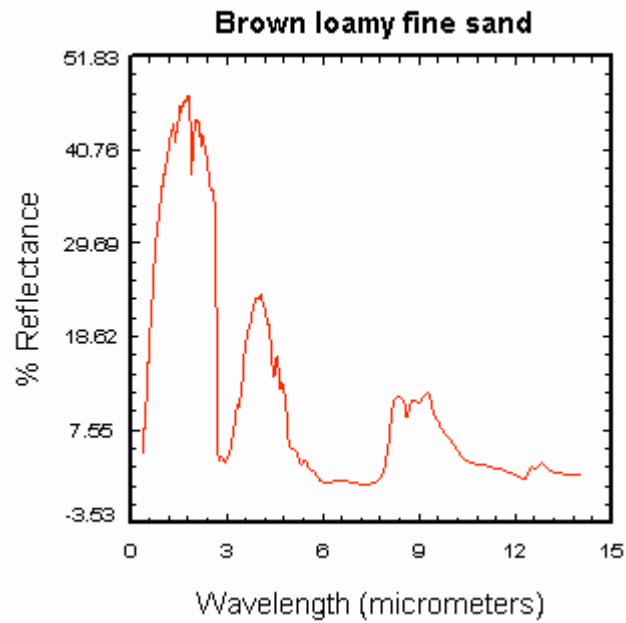
# How do we obtain end-members?

- spectroscopic library matching
  - make own in-situ observations
  - NASA-JPL spectral library  
<http://speclib.jpl.nasa.gov/>
  - USGS spectral library  
<http://speclab.cr.usgs.gov/spectral.lib04/spectral-lib04.html>
- empirical approach
  - extract from imagery at hand
  - extract from another imagery
- probabilistic approach

# How do we obtain end-members?



# How do we obtain end-members?



# How do we obtain end-members?

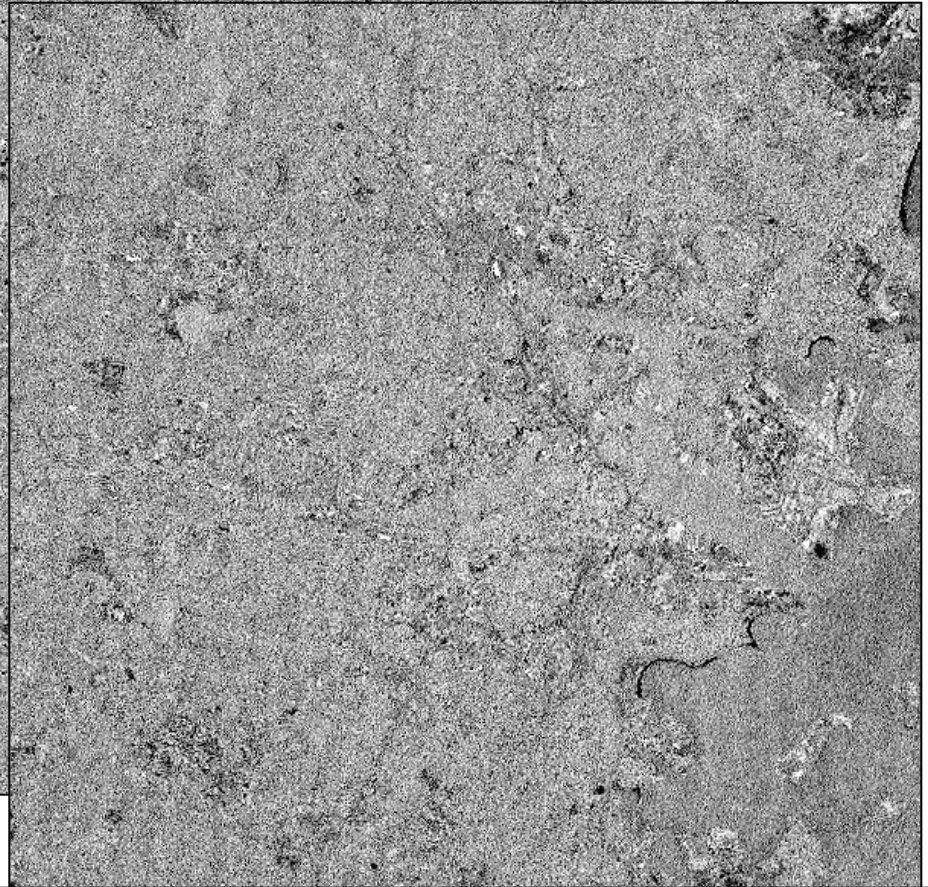
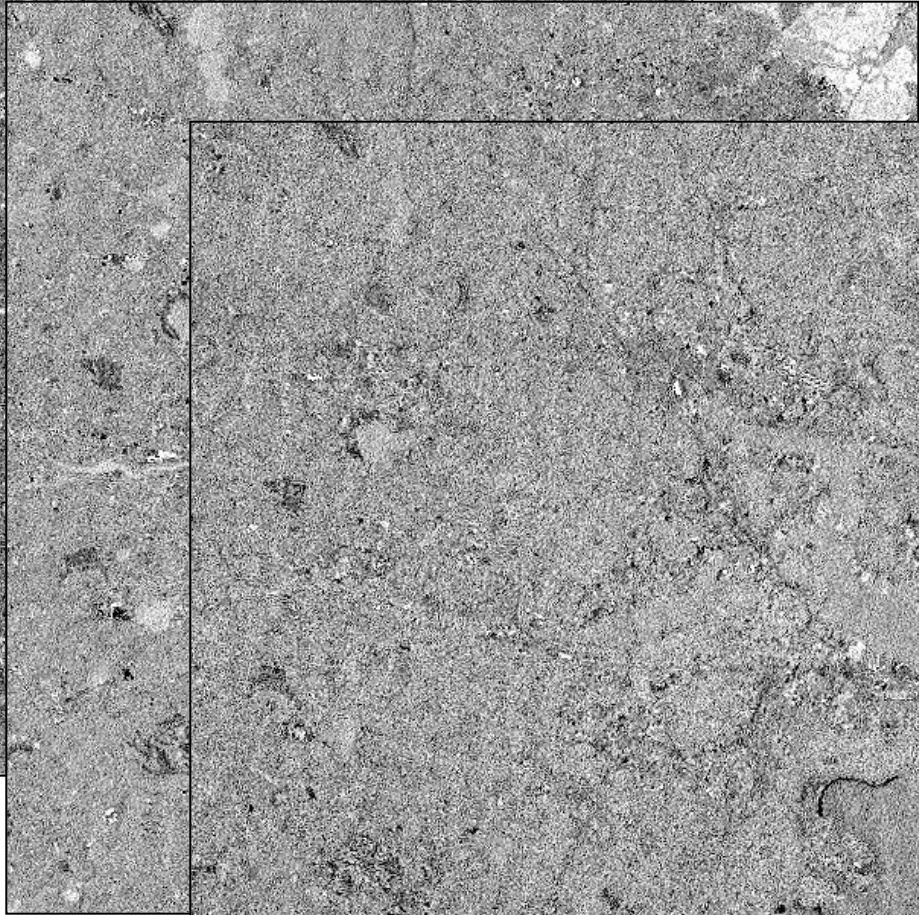
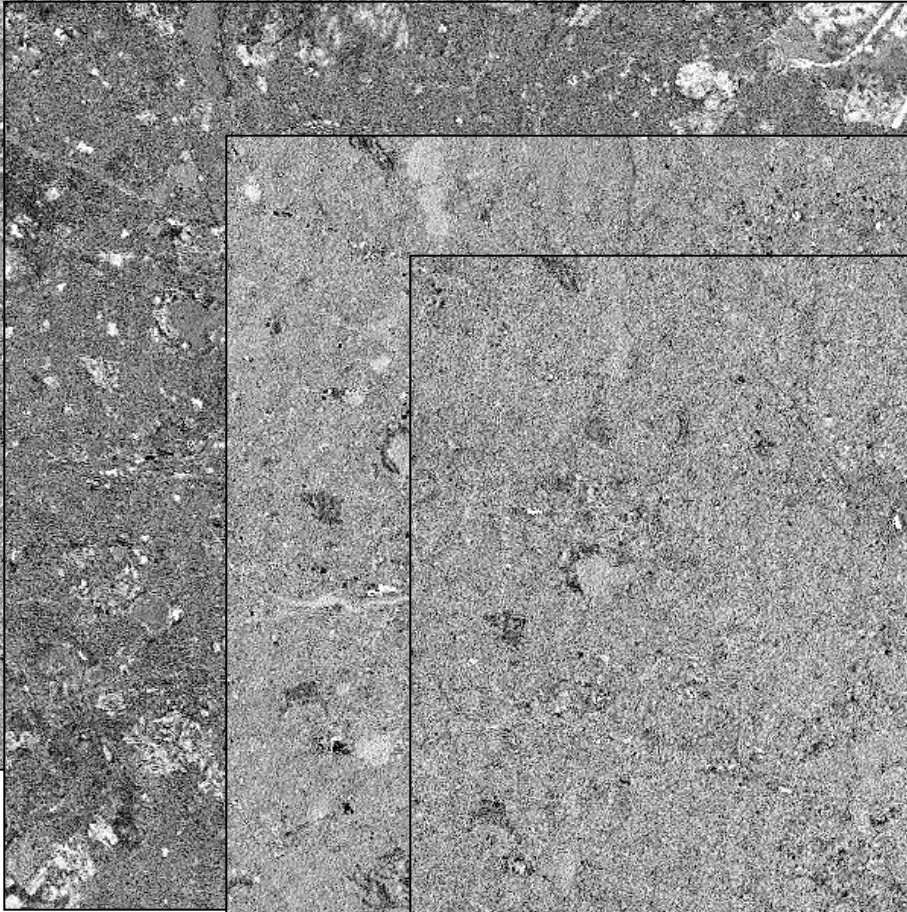
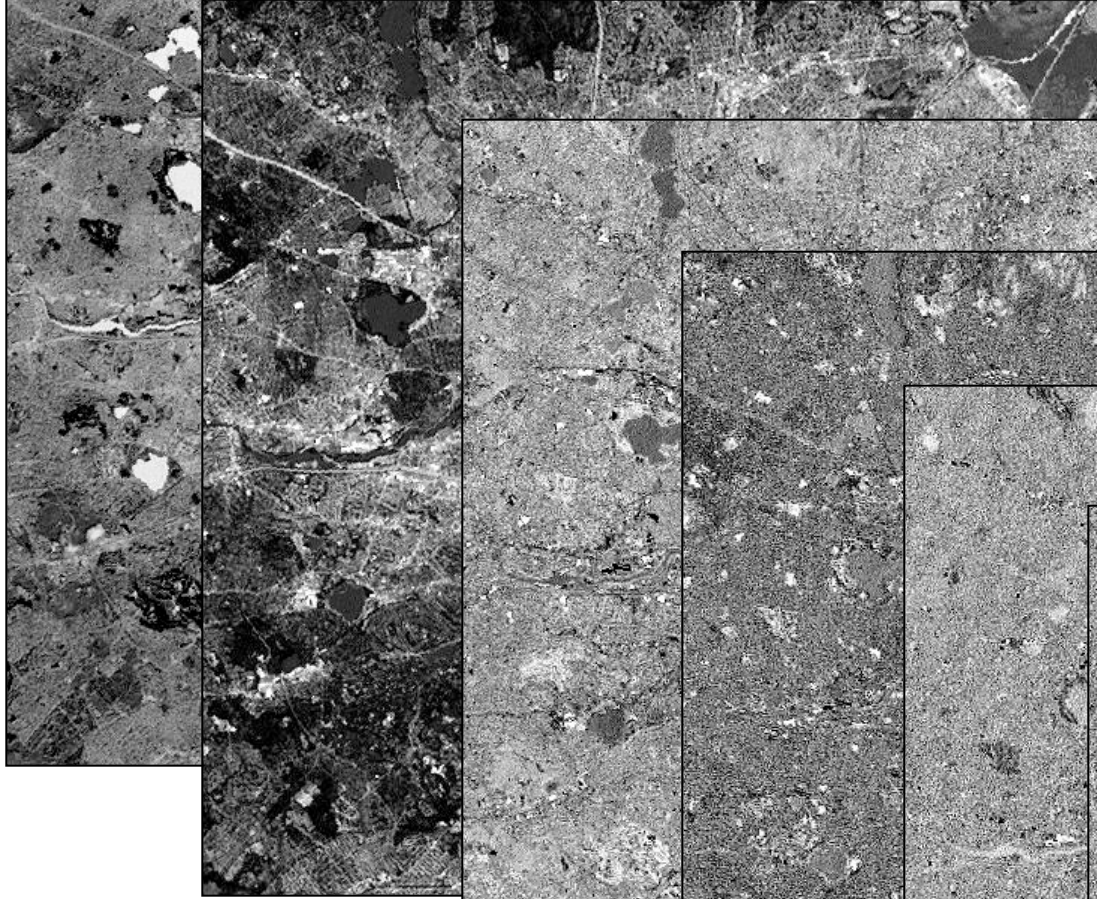
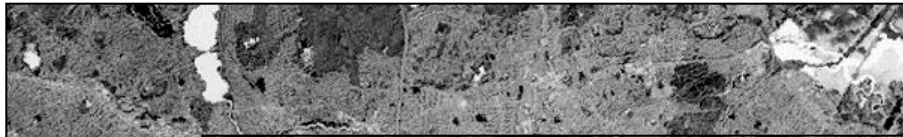
- spectroscopic library matching
  - make own in-situ observations
  - NASA-JPL spectral library  
<http://speclib.jpl.nasa.gov/>
  - USGS spectral library  
<http://speclab.cr.usgs.gov/spectral.lib04/spectral-lib04.html>
- empirical approach
  - extract from imagery at hand
  - extract from another imagery
- probabilistic approach

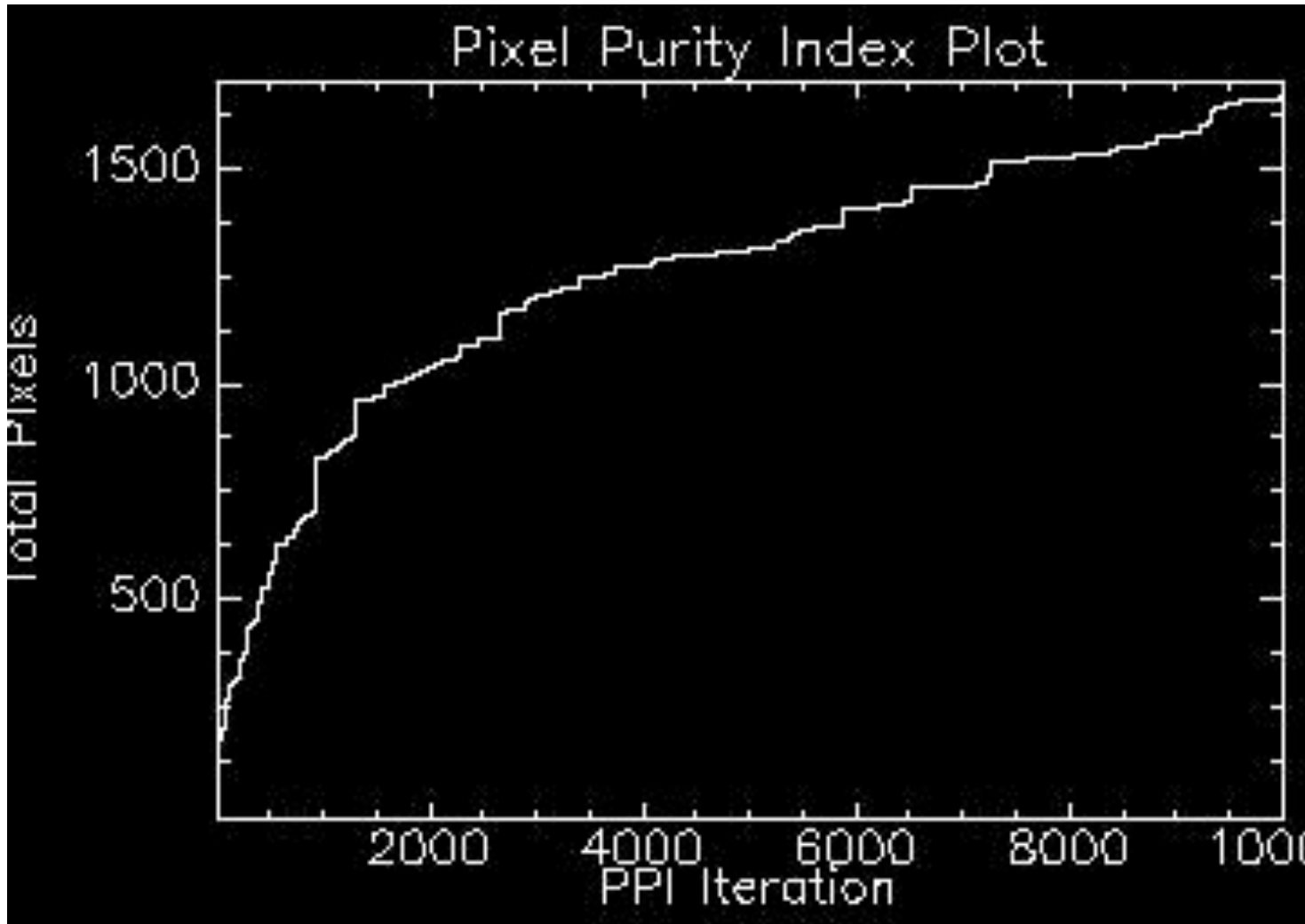
# How do we obtain end-members?

- Pixel Purity Index (PPI)
  - Sometimes, it is difficult to locate end-members because only a few pixels contain pure samples
  - PPI is a rigorous mathematical method to repeatedly project n-dimensional scatterplots to 2-D space and marking the extreme pixels
  - Each time spectral data is projected, we can note the the most extreme (pure) pixels and simply keep track of the number of times a pixel is considered extreme to make PPI image

# How do we obtain end-members?

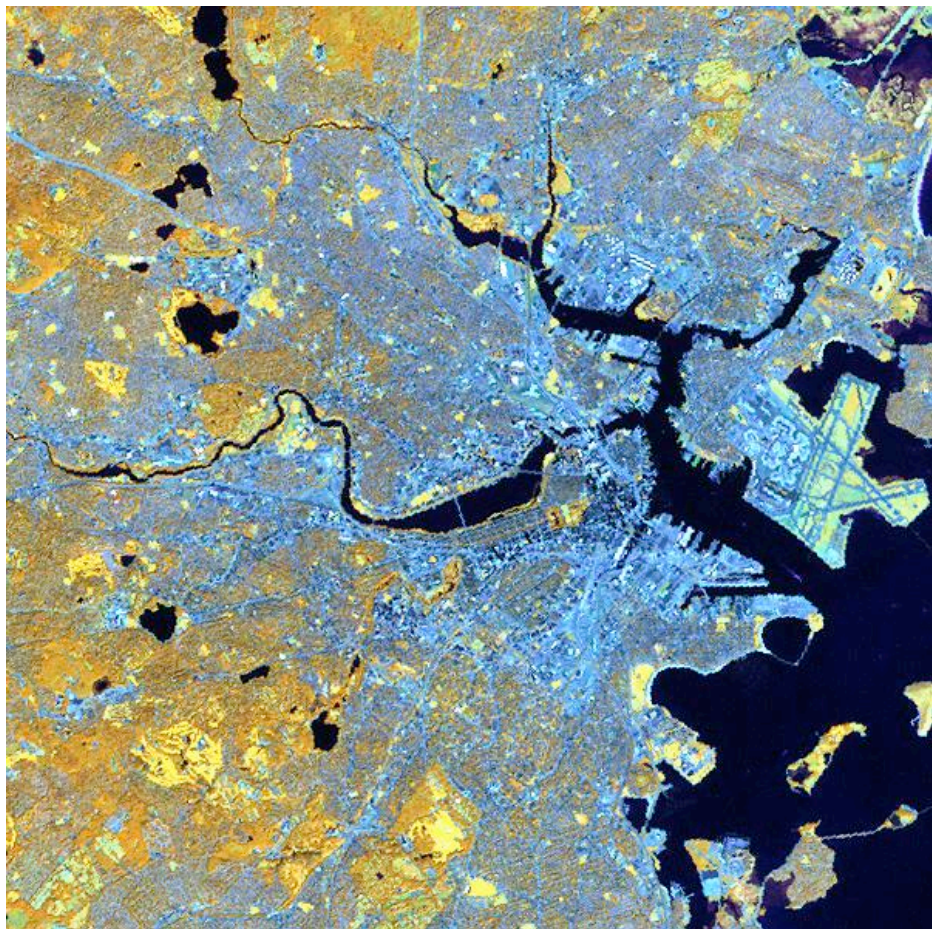
- MNF
  - used to reduce dimensionality and therefore noise in the image data set
  - it is a cascaded PCA analysis approach
  - the first de-correlates and scales noise in the data
  - the second creates MNF eigen images (i.e. PCA)
  - use these images in PPI analysis





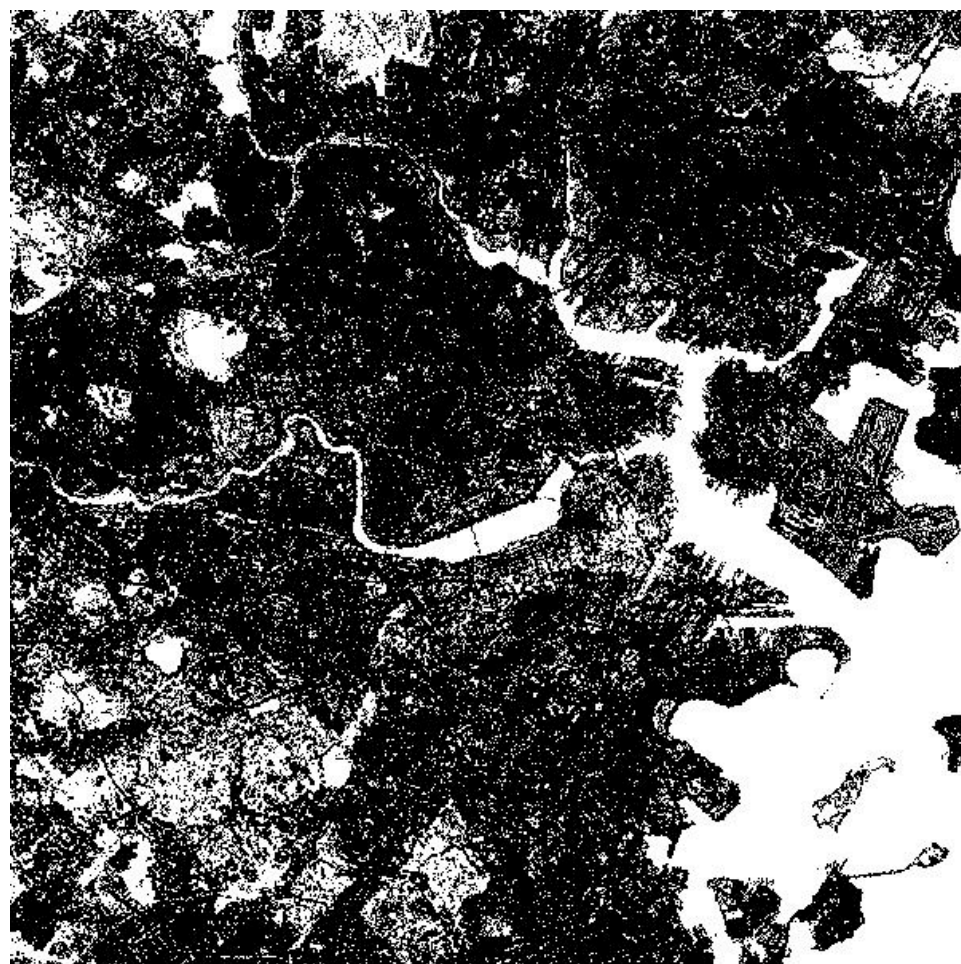
Boston image number of pure pixels after 10,000 iterations





Boston 453 as  
RGB

Boston PPI image



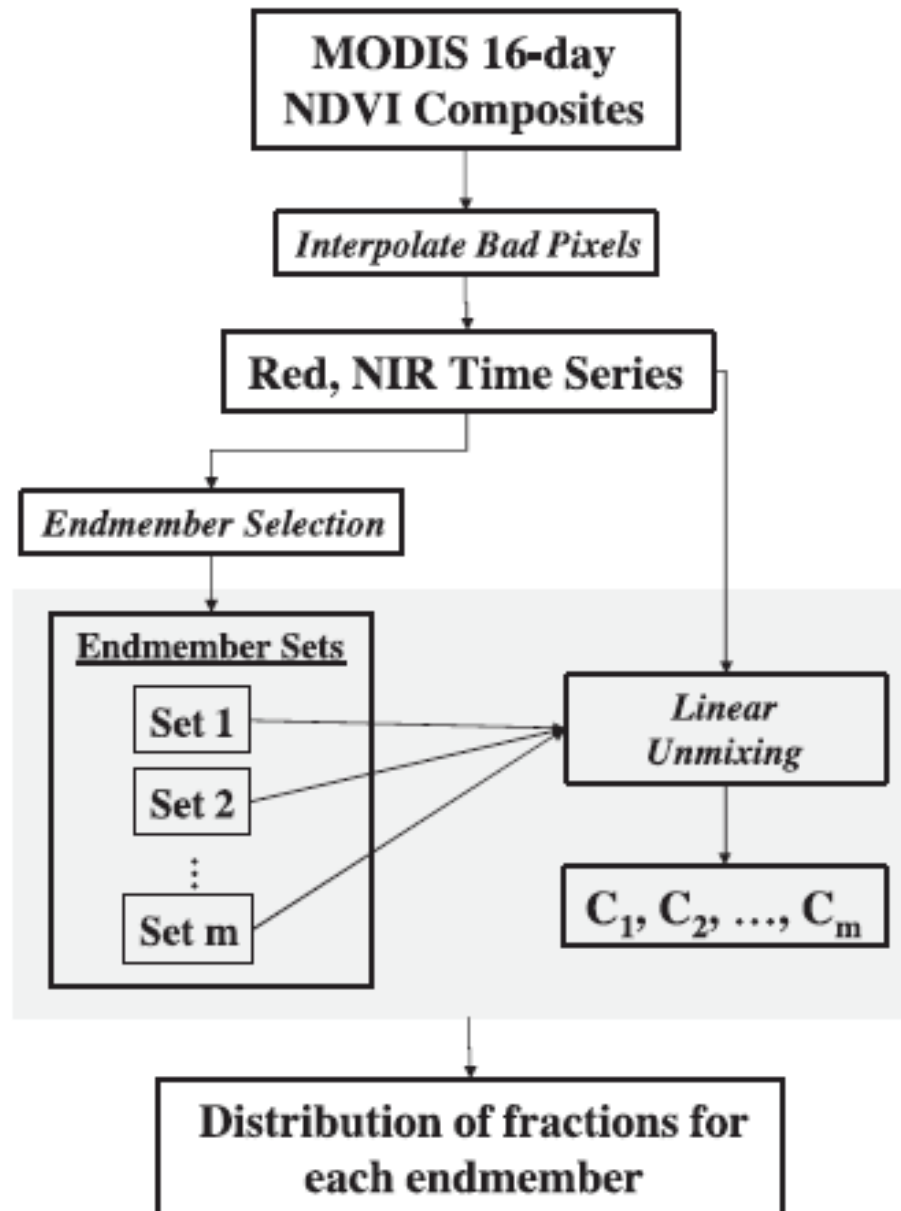
# Issues in mixture modeling

- bad (non-pure) end-member choice
- end-member variability
- fraction overflow
- omitted mixture component (missing important land cover category)
- data may not be able to describe the mixtures
- reflected photon into the sensor pixel has multiple interactions with other surface objects
- non-linear relationships

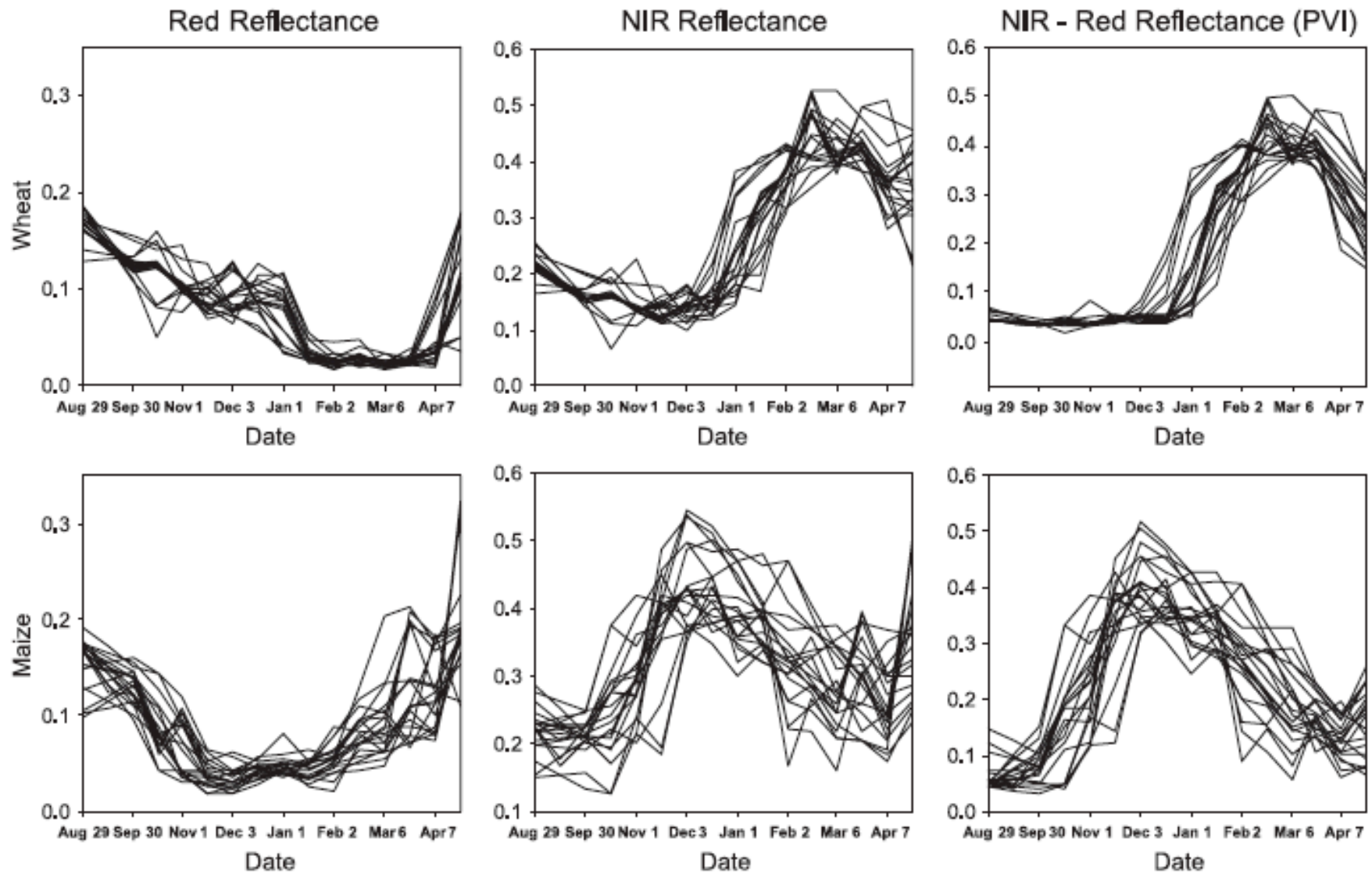
# probabilistic approach

- Linear mixture models assume that the end-member spectra are known exactly for each pixel
- In reality, however, reflectance is likely to vary across space and time, even for a narrowly defined end-members
- So, rather than define end-members with a single spectrum, it is possible to define end-members as a set of spectra which represent the full range of potential variability
- Thus, end-member fractions are not estimated as single values, but rather as a probability distribution that can be used to construct confidence intervals appropriate to the desired application

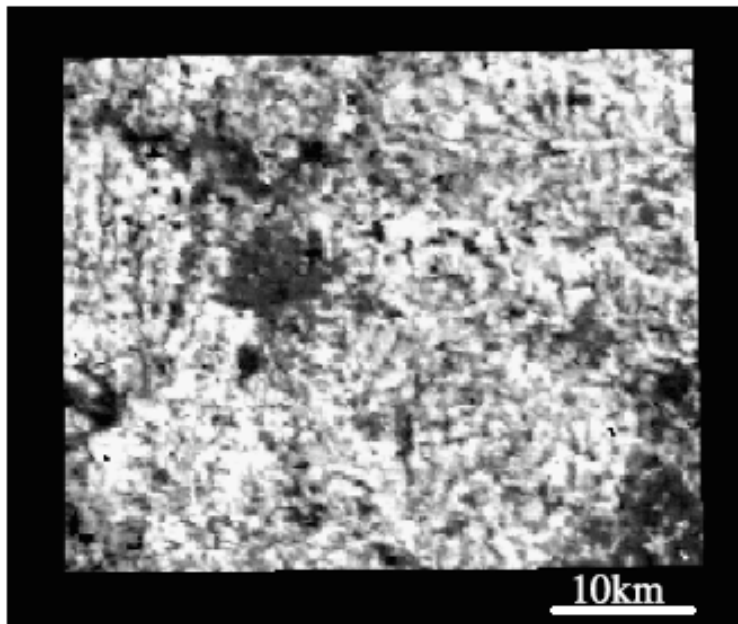
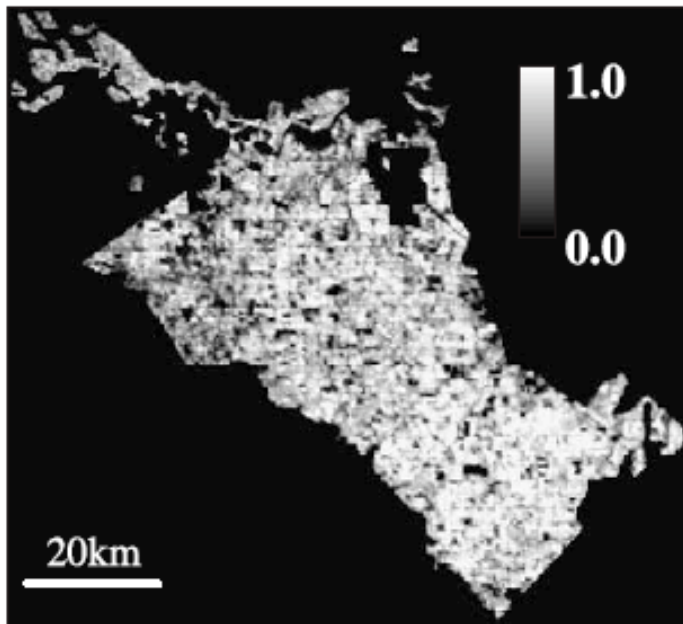
# probabilistic approach



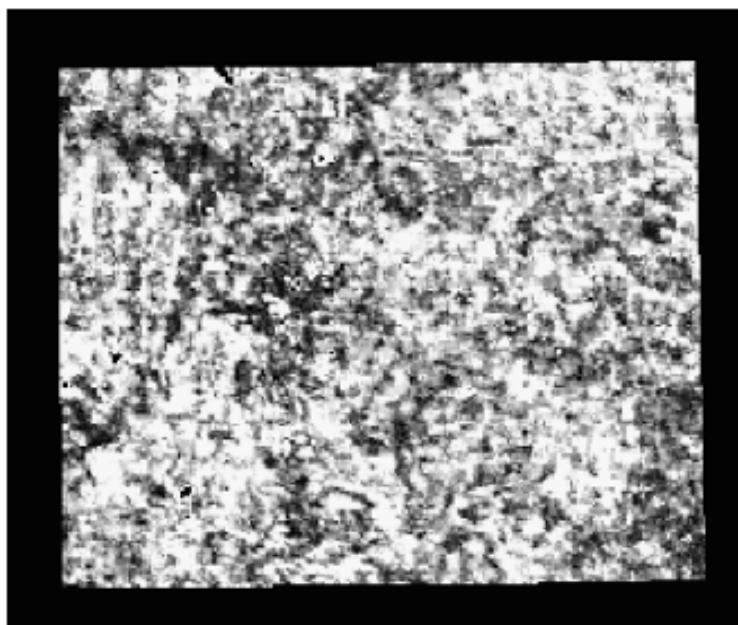
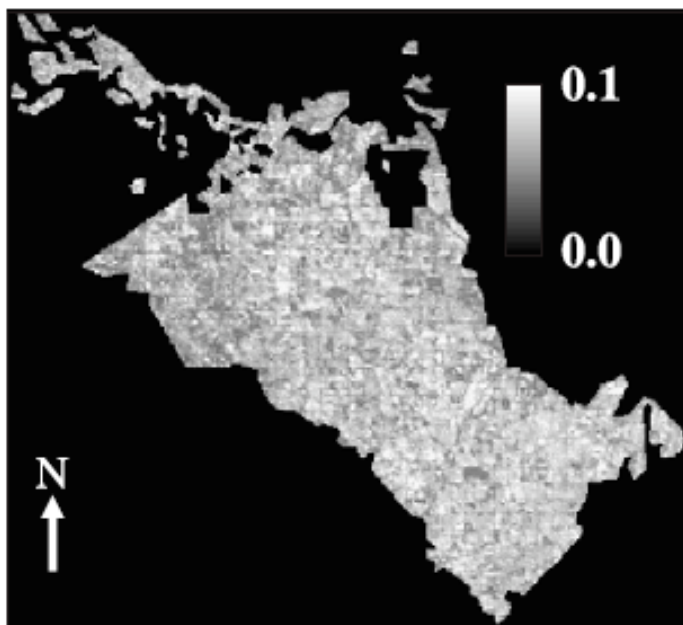
# probabilistic approach



# probabilistic approach



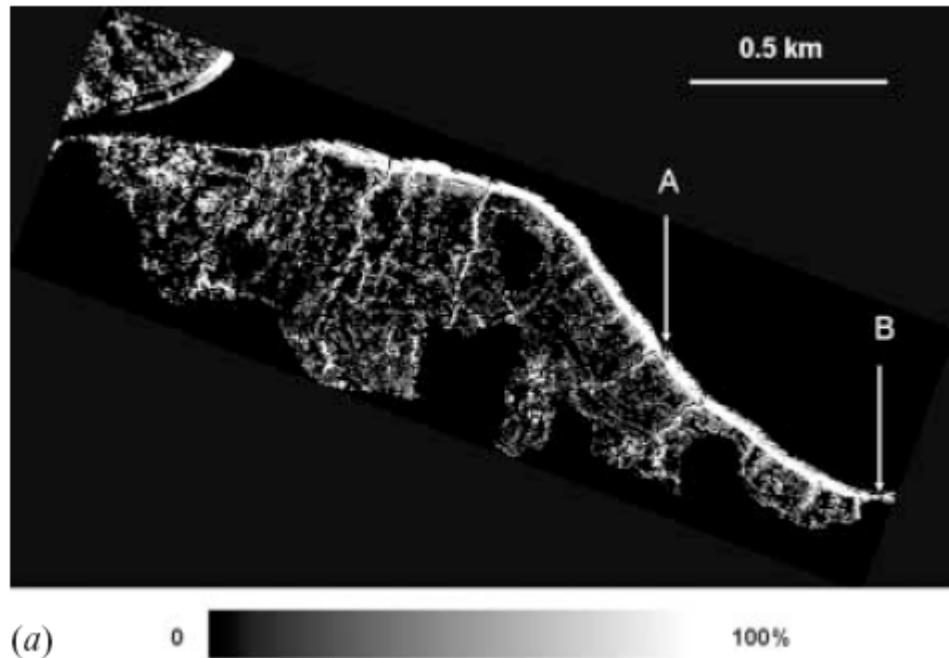
mean  
image



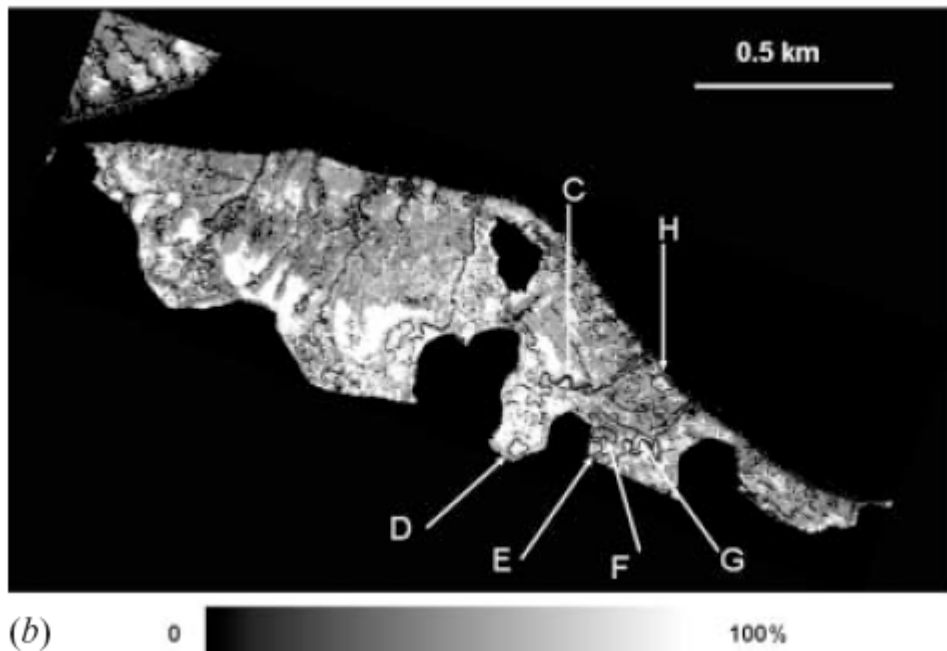
standard  
deviation  
image

# Multi-endmember spectral mixture analysis (MESMA)

- Given the variation in the number of endmembers needed for optimal unmixing, the use of a fixed suite of endmembers can cause large errors in the estimated fractional cover
- MESMA assumes that although an image contains a large number of spectrally distinct components, individual pixels contain a limited subset of these
- MESMA decomposes each pixel using different combinations of possible endmembers, allowing a large number of endmembers to be utilized across a scene and the optimization of endmembers for individual pixels.



Fraction images of two different salt marshes found in the San Francisco Bay area developed by applying the MESMA method to airborne AVIRIS images





# Spectral Angle Mapper (SAM)

- Spectral angle mapping is based on the well-known coefficient of proportional similarity, or cosine-theta approach
- This index defines that the degree of similarity between two objects (spectra in this case) may be evaluated in relation to the proportions of their presence
- For any two spectra, the index is determined from cosine theta which is merely the cosine of the angle between the two row vectors as situated in n-dimensional space
- The index value of 0 means the two spectra are completely dissimilar and index value of +1 means the two spectra coincide

# Spectral Angle Mapper (SAM)

$$\cos \theta = \frac{\sum_{i=1}^N r_i p_i}{\left( \sum_{i=1}^N r_i^2 \right)^{0.5} \left( \sum_{i=1}^N p_i^2 \right)^{0.5}}$$

$r_i$  - reference pixel vector

$p_i$  - any other image pixel vector